Efficient process conformance checking on the basis of uncertain event-to-activity mappings

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Efficient Process Conformance Checking on the Basis of Uncertain Event-to-Activity Mappings

Han van der Aa, Henrik Leopold, and Hajo A. Reijers

Abstract—Conformance checking enables organizations to automatically identify compliance violations based on the analysis of observed event data. A crucial requirement for conformance-checking techniques is that observed events can be mapped to normative process models used to specify allowed behavior. Without a mapping, it is not possible to determine if an observed event trace conforms to the specification or not. A considerable problem in this regard is that establishing a mapping between events and process model activities is an inherently uncertain task. Since the use of a particular mapping directly influences the conformance of an event trace to a specification, this uncertainty represents a major issue for conformance checking. To overcome this issue, we introduce a probabilistic conformance-checking technique that can deal with uncertain mappings. Our technique avoids the need to select a single mapping by taking the entire spectrum of possible mappings into account. A quantitative evaluation demonstrates that our technique can be applied on a considerable number of real-world processes where existing conformance-checking techniques fail.

Index Terms—Business process management, business process monitoring

1 INTRODUCTION

In many organizational contexts, employees are required to execute tasks of business processes in conformance with certain rules. For example, employees of a bank must check the credit history of a customer before granting a loan or the ground staff at an airport must verify the identity of a flight passenger before checking in the passenger’s luggage. So-called conformance-checking techniques play an important role in evaluating such rules [1]. They compare the actual behavior of employees, as recorded by information systems, to allowed process behavior that is specified in a normative process model [2]. In this way, conformance-checking techniques can automatically identify non-compliant actions and prevent potentially negative consequences such as delays in the process execution or fines imposed by authorities.

A fundamental requirement for conformance checking is that observed process behavior, commonly represented in the form of an event log, can be related to the normative process specification. This means that events in an event log must be mapped to the activities of a process model [3]. Without knowing the relations between events and activities, it is not possible to determine if observed behavior conforms to the allowed behavior specified by the process model, which makes conformance checking impossible.

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Typically, however, such a so-called event-to-activity mapping is not readily available [4], [5]. Furthermore, manually obtaining a mapping is often unfeasible because business analysts rarely possess the necessary knowledge on the details of a process implementation [6], whereas automated mapping techniques suffer from the high uncertainty caused by cryptic event names, non-compliant behavior, and noisy data [7]. As a result, existing mapping techniques (cf. [4], [8], [9]) fail to provide a definite solution to the mapping problem. Instead, they represent probabilistic methods that aim to select the best mapping from a number of potential ones, rather than providing a deterministic solution [10]. This comes with the considerable risk that the selected mapping does not capture the true relations between the events and activities. This can be particularly harmful in the context of conformance checking: if the selected mapping is incorrect, conformance-checking results based on this mapping will be incorrect as well.

Recognizing that the problem of mapping uncertainty compromises the successful application of conformance checking in practice, we use this paper to follow up on a proposal for a conformance-checking technique that can be applied in spite of mapping uncertainty [11]. The core idea of our technique is to take the entire spectrum of potential event-to-activity mappings into account and store them in a so-called behavioral space. In this way, we capture the implications of the different mappings in a structured way. Conformance checks based on this behavioral space, therefore, allow us to provide trustworthy conformance-checking results that take all potential mappings into account. Furthermore, by building on a hierarchical decomposition of process models, we are also able to compute conformance-checking results in a more efficient manner.

In comparison to [11], this paper provides several novel contributions. First, while the approach from [11] only
provided conformance insights at a process level, the approach presented here is able to identify the specific parts of a process where conformance issues arise. As a result, the conformance-checking results are much more detailed and, furthermore, provide the foundation for process improvement endeavors. Second, we introduce a novel approach to efficiently perform conformance checks. Whereas the original approach required a full enumeration of all possible worlds implied by mapping uncertainty, we present a computation approach that improves the computational efficiency of the approach by up to 70 percent. Third and finally, this paper presents the results of various additional evaluation experiments that demonstrate the applicability of our approach to a variety of process model types.

The remainder of the paper is structured as follows. Section 2 illustrates the problem of mapping uncertainty using an example. Section 3 introduces basic definitions. Section 4 presents the conceptual basis for our conformance-checking technique using behavioral spaces. Section 5 discusses how to efficiently obtain conformance-checking results using our approach. Section 6 presents the evaluation of our approach with a set of 598 real-world and 650 synthetic process models. Finally, Section 7 elaborates on related work, before Section 8 concludes the paper.

<table>
<thead>
<tr>
<th>Trace ID</th>
<th>Label sequence</th>
</tr>
</thead>
<tbody>
<tr>
<td>τₐ</td>
<td>(O_CHK, O_PRC, L_SM, P_SP, O_ARC)</td>
</tr>
<tr>
<td>τ₅</td>
<td>(O_CHK, O_PRC, L_SM, P_SP, P_NOT, L_SM, O_ARC)</td>
</tr>
<tr>
<td>τ₆</td>
<td>(O_CHK, O_PRC, L_SM, P_SP, P_NOT, L_SM, O_ARC)</td>
</tr>
<tr>
<td>τ₇</td>
<td>(O_CHK, O_PRC, L_SM, P_SP, P_NOT, L_SM, O_ARC)</td>
</tr>
<tr>
<td>τ₈</td>
<td>(O_CHK, O_PRC, L_SM, P_SP, P_NOT, L_SM, O_ARC)</td>
</tr>
</tbody>
</table>
and that, consequently, conformance-checking results based on the selected mapping are incorrect as well.

To illustrate the risks of selecting a single, possibly incorrect, mapping, consider the trace \( t_d \) from log \( L \) in Table 1 and the process model \( M \). By comparing the behavioral relations from the traces in \( L \) to the behavior of model \( M \), behavior-based mapping techniques such as [12], [20] can identify two potential mapping relations for the trace \( t_d \) which differ in their mapping of the \( P, \text{NOT} \) and \( P, \text{SP} \) events. In this case, one mapping (referred to as \( \sim_1 \)) will lead to the corresponding activity sequence \( \sigma_1 = \langle a, c, d, e, f, h \rangle \) and the other mapping (i.e., \( \sim_2 \)) to \( \sigma_2 = \langle a, c, d, f, e, h \rangle \). The task sequence \( \sigma_1 \) conforms to model \( M \), whereas \( \sigma_2 \) does not, because in this sequence, a notification e-mail is sent (event \( f \)) before the invoice (event \( e \)), instead of after. Since the conformance of these two activity sequences differs for this scenario, the assessment of whether or not \( t_d \) conforms to the process model \( M \) depends on the selection of a mapping relation. If \( \sim_1 \) is chosen, conformance-checking techniques will determine that \( t_d \) conforms to \( M \), whereas the opposite holds if \( \sim_2 \) is selected. As a result, the conformance of \( t_d \) fully depends on the ability to select a correct mapping in a situation where it is inherently uncertain what that mapping is.

This example illustrates that conformance-checking results based on the selection of a single, potentially incorrect mapping are not trustworthy. To provide a comprehensive solution to this problem, this paper introduces a conformance-checking technique that eliminates the need to select a single, possibly incorrect mapping and circumvents one of the central issues of alignment problems.

### 3 Preliminaries

The inputs for conformance checking are a process model and an event log. In the following we introduce formal notions for both. Definition 1 first introduces a formalization of a process model, adapted from [21]. It captures the commonalities of widely-used process modeling languages such as the Business Process Model and Notation (BPMN) and Event-driven Process Chains (EPCs). The execution semantics of such a process model are given by a translation into a Petri net following common formalizations, cf. [22], [23]. The process model depicted in Fig. 1 corresponds to this formal notion.

**Definition 1 (Process Model).** A process model is a tuple \( M = (A_M, E, G, N, F, t) \), where

- \( A_M \) is a finite set of activities,
- \( E \) is a finite set of events,
- \( G \) is a finite set of gateways,
- \( N = A_M \cup E \cup G \) is a finite set of nodes,
- \( F \subseteq N \times N \) is the flow relation, such that \( (N, F) \) is a connected graph,
- \( t : G \rightarrow \{ \text{and}, \text{xor} \} \) is a mapping that associates each gateway with a type.

In this paper, we decompose process models into single-exit single-entry (SESE) fragments in order to perform conformance checks. A SESE fragment refers to any part of a process model with exactly one entry and one exit node. The theoretical notions of SESE fragments in the context of directed graphs were developed by Hopcroft and Tarjan [25]. Vanhatalo et al. [26] and Polyvyanyy et al. [27] defined how a respective SESE decomposition can be obtained for process models. Definition 2 formally describes the notion of a SESE fragment we build on in this paper.

**Definition 2 (SESE Fragment).** Given a process model \( M \) with its set of nodes \( N \) and its flow relation \( F \), a SESE (single-entry single-exit) fragment \( S \) has exactly one entry node and one exit node. A SESE fragment is trivial if it is composed of a single flow relation. A SESE fragment \( S \) is canonical if it does not partially overlap with any other SESE fragment \( S' \) that can be derived from \( M \), i.e. \( S \) and \( S' \) are either nested (\( S \subseteq S' \) or \( S' \subseteq S \)) or they are disjoint (\( S \cap S' = \emptyset \)).

In the remainder of this paper, we only consider so-called valid decompositions of process models [28], which is a decomposition in which fragments only share activities or gateways. Any SESE decomposition can be turned into a valid decomposition by using the technique presented in [29]. Fig. 2a provides a decomposition for the running example into a root fragment \( S_0 \) and 9 smaller fragments. This figure also highlights the hierarchy that exists between the SESE fragments in a decomposition. The so-called Refined Process Structure Tree (RPST) can be used to capture
this hierarchy between canonical SESE fragments, as visualized in Fig. 2b, and defined as follows.

**Definition 3 (RPST).** Let $M$ be a process model. The Refined Process Structure Tree of $M$ is the tree composed of the set of all its canonical SESE fragments such that the parent of a canonical SESE fragment $S$ is the smallest canonical SESE fragment that contains $S$. The root of the tree is the entire process model, and the leaves are the trivial SESE fragments. The set of all the nodes of the tree is denoted as $S$.

In the remainder of the paper, we will refer to canonical SESE fragments resulting from the RPST decomposition simply as SESE fragments. Also note that the SESE fragments are defined as a set of flow relations. For simplicity, however, we will use the term SESE fragment to also refer to the fragment of a process model that is induced by those relations. For instance, we shall use $S_1$ to denote the fragment containing the activities $A$ and $B$, the xor-gateway following $B$, and the flow relations that connect these nodes.

Finally, we define event logs and event traces according to notions from [30]. Definition 4 formally defines an event log.

**Definition 4 (Event Log).** Let $C$ be a finite set of event classes. A log $L$ is defined as $L = (E, I, E, I, <)$, where

- $E$ is the set of events,
- $I$ is the set of case identifiers,
- $E : E \rightarrow I$ a surjective function linking events to cases,
- $I : I \rightarrow C$ a surjective function linking events to event classes,
- $< \subseteq E \times E$ a strict total ordering over the events.

Given an event log $L$ according to Definition 4, we shall use the shorthand notation $\tau = \langle e_1, \ldots, e_n \rangle$ in the remainder of this paper to refer to an event trace that consists of $n$ events with an identical case identifier. Furthermore, for any pair of events $e_i$ and $e_j$ with $i < j$, it holds that $e_i < e_j$ according to the strict total ordering of the events in log $L$.

### 4 Conformance Checking Using Behavioral Spaces

This section describes the conceptual basis of our conformance-checking technique. It takes as input an event trace, a process model, and an uncertain event-to-activity mapping. Note that the question of how to obtain an uncertain mapping, which consists of a number of potential event-to-activity mappings, is not the focus of this paper. Potential mappings can be obtained using one or more mapping techniques, such as [4], [8], [9]. In the remainder, Section 4.1 first describes the notion of a behavioral space, which we use to capture the impact of mapping uncertainty on the process behavior described by trace $\tau$. Then, Section 4.2 introduces the conformance-checking metrics that build on the obtained behavioral spaces. Finally, Section 4.3 discusses the diagnostic conformance-checking information that can be obtained for processes with our technique.

#### 4.1 Capturing Mapping Uncertainty Using Behavioral Spaces

Mapping uncertainty results from multiple views on which behavior, in terms of process model activities, is described by a single event trace. This uncertainty manifests itself through the existence of multiple possible event-to-activity mappings. A single event-to-activity mapping captures relations between events in an event trace $\tau$ and the activities in a process model $M$, as defined in Definition 5.

**Definition 5 (Event-to-Activity Mapping).** Let $\tau = \langle e_1, \ldots, e_n \rangle$ be an event trace with a set of events $E_\tau$ and $M = (A_M, E, G, N, F, t)$ a process model. An event-to-activity mapping is a surjective relation $\sim \subseteq E_\tau \times A_M$. Elements of the relations are referred to as correspondences, where a correspondence $e \sim a \in (E_\tau \times A_M)$ denotes a mapping relation between an event $e$ and an activity $a$.

In Definition 5, the relation $\sim$ is defined as surjective, because we assume that each event in a trace $\tau$ is always mapped to an activity. Furthermore, this implies that a N:1 relation can exist between events and activities. This cardinality captures the notion that events are typically more fine granular than activities [31]. As an illustration, consider a trace $\tau = \langle e_1, e_2, e_3, e_4, e_5, e_6 \rangle$ and a mapping $\{e_1 \sim a, e_2 \sim c, e_3 \sim c, e_4 \sim d, e_5 \sim c, e_6 \sim f\}$. Given that both $e_2$ and $e_3$ are aligned to activity $c$, this mapping indicates that the trace $\tau$, consisting of six events, corresponds to a sequence of only five activities: $\{a, c, d, e, f\}$.

Mapping uncertainty leads to the existence of multiple potential event-to-activity mappings. Here, we capture this spectrum in the form of an uncertain event-to-activity mapping $EA(\tau, M)$, as defined in Definition 6.

**Definition 6 (Uncertain Event-to-Activity Mapping).** Let $\tau = \langle e_1, \ldots, e_n \rangle$ be an event trace and $M$ a process model with an activity set $A_M$. An uncertain event-to-activity mapping is a tuple $EA(\tau, M) = (M, \phi)$, with:

- $M$: a set of event-to-activity mappings between $\tau$ and $M$;
- $\phi : M \rightarrow [0, 1]$: a function that assigns a probability to each event-to-activity mapping $M(\tau, M) \in M$. For this function, it holds that the cumulative probability is equal to 1, i.e., $\sum_{M \in M} \phi(M) = 1$.

In this definition, each mapping $M(\tau, M) \in M$ represents a potential way to map the events in $\tau$ to the activities in $A_M$. The probability function $\phi$ assigns a probability $p_i$ to each mapping $M(\tau, M) \in M$. These probabilities generally follow from the confidence of an event-to-activity mapping technique. For instance, a technique based on semantic similarity scores, such as [4], can quantify the probability as the product of the similarity scores associated with each correspondence in the mapping. In this way, mappings with a higher semantic similarity receive a higher probability than the ones with a lower score. If no probabilities are available, the most straightforward solution is to assign an equal probability $\frac{1}{\lvert M \rvert}$ to each mapping.

Given such an uncertain event-to-activity mapping $EA(\tau, M)$, we define the notion of a probabilistic behavioral space as a means to capture all process model behavior conveyed by trace $\tau$ according to the mapping $EA(\tau, M)$, i.e. the sequences of process model activities that follow from the different possible mappings. We shall refer to such a sequence of process model activities as a trace translation of event trace $\tau$, because it represents a translation of the
trace’s events into process model activities. We denote a trace translation of \( \tau \) with \( \sigma(\tau) \).

**Definition 7 (Trace Translation).** Let \( \tau = (e_1, \ldots, e_n) \) be an event trace with a set of events \( E_\tau \), \( M = (A_M, E, G, N, F, t) \) a process model, and \( \mathcal{M}(\tau, M) \) an event-to-activity mapping between \( \tau \) and the activity set of process model \( M \). A trace translation \( \sigma(\tau) \) represents a sequence of activities \( \{a_1, \ldots, a_m\} \) according to the mapping \( \mathcal{M}(\tau, M) \).

Since an uncertain mapping \( \mathcal{E}_A(\tau, M) \) consists of multiple event-to-activity mappings, a mapping \( \mathcal{E}_A(\tau, M) \) results in different trace translations for \( \tau \). For instance in Section 2, we described an example where a single trace had two trace translations, \( \sigma_1(\tau) = \langle a, c, d, e, f, h \rangle \) and \( \sigma_2(\tau) = \langle a, c, d, f, e, h \rangle \), which resulted from two possible mappings.

Together, the translations of a trace represent the spectrum of process behavior potentially conveyed by \( \tau \), i.e., the behavioral space of an event trace. Since each mapping can be associated with a probability, we include a probabilistic component in our definition of a behavioral space, as captured in Definition 8.

**Definition 8 (Probabilistic Behavioral Space).** Let \( \tau = (e_1, \ldots, e_n) \) be an event trace with a set of events \( E_\tau \), \( M = (A_M, E, G, N, F, t) \) a process model, and \( \mathcal{E}_A(\tau, M) \) an uncertain event-to-activity mapping between \( \tau \) and the activity set of process model \( M \). We define a probabilistic behavioral space as a tuple PBS\(_t\) = \( (\Sigma(\tau), \phi) \), with:

- \( \Sigma(\tau) \): the set of trace translations of trace \( \tau \) over the activity set \( A \) as given by the event-to-activity mappings in \( \mathcal{E}_A(\tau, M) \);
- \( \phi : \Sigma \to [0, 1] \): a function that assigns a probability to each trace translation in \( \Sigma(\tau) \). For this function, it holds that the cumulative probability is equal to 1, i.e., \( \sum_{\sigma \in \Sigma} \phi(\sigma) = 1 \).

The set \( \Sigma(\tau) \) comprises potential trace translations of trace \( \tau \) over the activity set \( A_M \), where each translation \( \sigma_\tau \in \Sigma(\tau) \) is based on a mapping \( \mathcal{M}(\tau, M) \) contained in \( \mathcal{E}_A(\tau, M) \). This set, together with the probabilities provided by the function \( \phi \), provides the basis for the probabilistic conformance metric described next.

### 4.2 Probabilistic Conformance

The goal of conformance checking is to determine if observed behavior in a trace \( \tau \) is allowed by the behavioral specification of a process model \( M \). Since uncertain event-to-activity mappings lead to multiple views on the process model behavior described by a trace (i.e., its trace translations), all these views need to be checked against the model \( M \). In this section, we demonstrate how to perform a conformance check given a probabilistic behavioral space in order to obtain insightful conformance results and diagnostic information.

To perform this conformance checks, we build on the approach for decomposed conformance checking defined by Munoz-Gama et al. [29]. It splits up a process model into a set of canonical SESE fragments \( S_i \) as described and depicted in Section 3, and then determines for each fragment in \( S \) whether it conforms to a given activity sequence or not. We use this approach as the basis for our conformance checks of an entire behavioral space against a model. We kindly refer the interested reader to [29] for an in-depth explanation of the conformance checks between a single activity sequence and a SESE fragment and proofs of the guarantees it provides regarding the correctness of decomposed conformance-checking results.

Building on the approach from [29], we introduce a probabilistic conformance metric that quantifies the conformance of a probabilistic behavioral space to a SESE fragment. The metric combines the conformance assessments for individual trace translations with probabilistic information. Specifically, the metric corresponds to the total probability associated with the trace translations that conform to a certain SESE fragment \( S \in S \). In this way, the metric defined in Definition 9 represents the probability that \( \tau \) conforms to fragment \( S \).

**Definition 9 (Behavioral Space Conformance).** Let \( \tau \) be a trace with a probabilistic behavioral space PBS\(_t\) = \( (\Sigma(\tau), \phi) \), \( M \) a process model, and \( S \) a fragment of the SESE decomposition of \( M \). Then we define:

- \( \Sigma_S(\tau) \subseteq \Sigma(\tau) \) as the set of trace translations in \( \Sigma(\tau) \) conforming to fragment \( S \);
- \( ProbConf(\tau, S) = \sum_{\sigma \in \Sigma_S(\tau)} \phi(\sigma) \): as the behavioral space conformance of trace \( \tau \) to fragment \( S \), where \( \phi(\sigma) \) captures the probability of trace translation \( \sigma \).

Because of the probabilistic nature of the ProbConf metric, the metric yields a different kind of result than traditional conformance-checking techniques. In traditional conformance-checking scenarios, i.e., without mapping uncertainty, a trace either conforms or does not conform (or a fragment of) a process model. By contrast, when using our technique, traces are either conforming, non-conforming, or potentially conforming. Potentially conforming traces are those traces for which some trace translations conform to a process model, whereas others do not. The conformance of these traces is associated with a certain probability \( 0 < p < 1 \).

Take, for instance, the process model fragment \( S_3 \) and a trace \( t_1 \) with two trace translations \( \sigma_1(\tau_1) \) and \( \sigma_2(\tau_1) \), as depicted in Fig. 3. Assume that \( \sigma_1(\tau_1) \) is associated with a probability of 0.7 and \( \sigma_2(\tau_1) \) with probability 0.3.

While trace translation \( \sigma_1(\tau_1) \) conforms to \( S_3 \), this does not apply for \( \sigma_2(\tau_1) \). This latter translation executes both of the mutually exclusive activities \( F \) and \( G \). This leads to a conflict between the conformance of the different translations of \( \tau_1 \) with respect to \( S_3 \). Therefore, the trace \( \tau_1 \) is said to be potentially conforming with \( S_3 \) with a probability of 0.7, i.e., ProbConf\(_{\tau_1, S_3} = 0.7 \). This shows that, even though we cannot make certain statements about the conformance of \( \tau_1 \) to \( S_3 \), we do know that \( \tau_1 \) is more likely
... to conform than not. Furthermore, we also know the mapping conditions under which $t_1$ is conforming or non-conforming. Namely, $t_1$ conforms to $S_3$ if the correspondence $e_6 \sim f$ holds, whereas the trace is non-conforming if $e_6 \sim g$ is true. This type of diagnostic information is very useful because it provides insights into which aspects of an uncertain mapping lead to uncertainty in the conformance-checking results for observed behavior.

It is important to note that the $\text{ProbConf}$ metric, despite its probabilistic nature and the presence of mapping uncertainty, can often still produce non-probabilistic (or deterministic) conformance-checking results. To illustrate this, reconsider the process model fragment $S_3$, as well as a trace $t_2$ with the following trace translations:

$$\sigma_1(t_2) = \{a, c, d, e, f, h\}$$
$$\sigma_2(t_2) = \{a, c, d, e, f, g\}$$
$$\sigma_3(t_2) = \{a, c, d, e, f, h\}$$

In this case, mapping uncertainty has resulted in two trace translations that differ with respect to their fifth activity: $F$ for $\sigma_1(t_2)$ and $G$ for $\sigma_2(t_2)$. Despite this uncertainty, we can still with certainty state that $t_2$ conforms to $S_3$. The reason is that both trace translations conform to $S_3$, since $S_3$ allows for the execution of either activity $F$ or $G$. As a result, $\text{ProbConf}(t_2, S_3) = 1.0$, thus yielding a deterministic result. In a similar fashion, we can determine for certain that some traces are non-conforming, despite having multiple translations.

### 4.3 Hierarchical Conformance Insights

Thus far we focused on conformance checking for a single process fragment using the $\text{ProbConf}$ metric. This metric can be applied to obtain conformance information for a process model as a whole, yielding a single $\text{ProbConf}$ value indicating the likelihood that a trace conforms to the entire process. However, an important benefit of decomposed conformance checking is that it can provide conformance results at various levels of detail. In particular, we can exploit the hierarchical relations between the SESE fragments of a decomposition in order to obtain hierarchical conformance-checking results.

Consider, for instance, the SESE fragments depicted in Fig. 4. The fragments $S_8$ and $S_10$ are subsumed by their parent, $S_9$, whereas, in turn, $S_{10}$ subsumes fragments $S_{11}$ and $S_{12}$. By applying $\text{ProbConf}$ on all fragments, we can obtain conformance-checking results at different levels of detail. Using the trace translations of $t_4$ depicted in the same figure, we can observe interesting properties. For instance, even though the conformance of the fragments $S_{11}$ and $S_{12}$ are both equal to 1.0, the conformance of their parent fragment, i.e., $\text{ProbConf}(t_4, S_{10})$, is only 0.1.

These results reveal that the conformance problems for this trace do not relate to either $S_{11}$ or $S_{12}$ individually, but rather to their inter-relation. This example illustrates the usefulness of decomposed conformance checking in combination with behavioral spaces because this diagnosis could only be observed by considering both levels of detail.

We can expand this hierarchical view on conformance checking to consider the entire hierarchical structure of SESE fragments in a decomposition. For this, we can adapt the RPST representation of a decomposition, which we provided in Fig. 2b, to incorporate conformance-checking results obtained by the $\text{ProbConf}$ metric. Fig. 5 illustrates this for the running example with conformance-checking results based on trace $t_4$. This figure clearly shows how the probabilistic conformance of a trace can differ among the various fragments and levels of detail. While the entire process model has a probability of only 0.1 to be conforming (following from the only fully conforming trace translation $\sigma_3(t_4)$), the figure clearly shows that this low probability largely results from problems in the latter part of the process, related to the fragment $S_9$.

Despite these apparent differences between probabilistic conformance values, the relation between the likelihoods of a fragment and its sub-fragments defines a clear bound for conformance values. Namely, the $\text{ProbConf}$ value of a fragment $S_i$ with sub-fragments $S_j = \{S_{j1}, \ldots, S_{jn}\}$ can never be higher than the minimum of its child-fragments, i.e., $\text{ProbConf}(t, S_i) \leq \min\{\text{ProbConf}(t, S_{j1}), \ldots, \text{ProbConf}(t, S_{jn})\}$. Intuitively, this means that a child-fragment can never be less conforming than its parent.

By obtaining conformance insights for all process model fragments at various levels of granularity, our conformance-checking technique provides the foundation for root-cause analysis of conformance problems. The conformance levels of traces to particular fragments reveals which parts of a process can be considered most problematic. As such, these insights can be used in order to take measures to avoid these problems in the future, thereby improving the process. In the next section, we describe how the concepts introduced...
in this section can be used to obtain the conformance-checking results in an efficient manner.

5 Efficient Conformance Checking

In this section, we define an approach that can be used to efficiently compute the conformance-checking results described in the previous section. The ability to obtain these results efficiently is important, because the computational complexity of conformance-checking techniques represents a key issue for their applicability in industrial settings [32]. In the context of this paper, this complexity is particularly problematic, since mapping uncertainty can exponentially increase the number of conformance checks that are required to be performed per trace. For instance, if traces are associated with 10 trace translations, the execution time could be an order of magnitude larger than in a situation without mapping uncertainty. However, because mapping uncertainty may only relate to specific parts of a process, it is not always necessary to recompute the conformance of all process model fragments for every trace translation. By recognizing this, we can define a technique that obtains conformance-checking results in a considerably more efficient manner.

5.1 Approach Overview

Our computation approach builds on the idea that mapping uncertainty often only relates to specific parts of a process. For example, in the running example, mapping uncertainty might affect the parts of the process related to billing (i.e. activities \(E, F,\) and \(G\)), whereas other parts of the process, related to order processing and shipment, are not affected by uncertainty. By utilizing this knowledge, we define an efficient conformance-checking technique that only performs repeated checks (for different trace translations) for those parts of a process affected by mapping uncertainty. For other parts, a single check suffices to determine the conformance of all trace translations in a behavioral space.

We achieve this through the approach visualized in Fig. 6. The approach takes as input an event trace \(t\), a process model \(M\), and an uncertain event-to-activity mapping \(E\)\(A(t, M)\). In our approach we first decompose a process model according to the method from [27], briefly described in Section 3. Furthermore, we compute a behavioral space \(PBS_i\) by generating a single trace translation \(\sigma(t)\) for each mapping in \(E\)\(A(t, M)\), according to the method described in Section 4.1. After these preliminary steps, we conduct three further steps that enable us to conduct conformance checks in a more efficient manner. Based on the established behavioral space, our approach identifies those activities that are associated with mapping uncertainty. Then, we determine which process fragments of the decomposed process model are affected by uncertainty. Finally, we perform an efficient conformance check by only recomputing conformance values for those process model fragments that are actually affected by mapping uncertainty. In the remainder of this section, we describe each of these latter three steps in detail.

5.2 Uncertain Activity Identification

In the first step of our approach, we determine the activities affected by mapping uncertainty. Algorithm 1 describes this step. The method used to identify activities affected by mapping uncertainty depends on whether the event-to-activity mapping was established using a class-level or instance-level mapping technique. Class-level techniques, such as [7], [12], establish a mapping between event \(classes\) and process model activities. As a result, any occurrence of an event of a certain class will be mapped to the same activity or, in case of uncertainty, the same activities. By contrast, instance-level techniques, such as [4], may map events from the same event class to different activities in different traces. In Algorithm 1, we use isClassLevel() on line 4 and isInstanceLevel() on line 11 to distinguish among these two options.

---

**Algorithm 1. Identifying Activities Affected by Mapping Uncertainty**

```
1: function IDENTIFY UNCERTAIN ACTIVITIES
2:   Input: PBS_i = (E(t), \phi) \triangleright Behavioral space of t
3:   Input: E\(A(t, M)\) \triangleright Uncertain mapping
4:   if isClassLevel(E\(A(t, M)\)) then
5:      \(U_M = \emptyset\)
6:      for \(E \in C\) do
7:         \(A_E = \text{getMappedActivities}(E, E\(A(t, M)\))\)
8:      if \(|A_E| > 1\) then
9:         \(U_M = U_M \cup A_E\)
10: \(U_t = U_M \cap A_t\)
11: if isInstanceLevel(E\(A(t, M)\)) then
12:   \(U_t = \emptyset\)
13: for \(\sigma_1(t) \in \Sigma_t\) do
14:   for \(\sigma_2(t) \in \Sigma_t\) do
15:      \(\delta = \text{String.diff}(\sigma_1(t), \sigma_2(t))\)
16:      \(U_t = U_t \cup \delta\)
17: return \(U_t\)
```

A class-level mapping directly provides insights into the activities that differ among the trace translations. In such a scenario, we can, for instance, observe that an event class \(E \in C\) is always mapped to either activity \(B\) or activity \(C\). From this, we know that activities \(B\) and \(C\) are affected by uncertainty. By identifying the activities associated with all event classes subject to mapping uncertainty, see lines 5–9 in Algorithm 1, we then obtain a set \(U_M \subset A_M\) of uncertain activities for the process model \(M\). For a specific behavioral space \(PBS_i\), the set of uncertain activities \(U_t\) is then given as the subset of \(U_t\) that is contained in any of the trace translations in \(BS_i\), i.e. using \(A_t\) to denote the set of activities contained in the behavioral space of trace \(t\), we get \(U_t = U_M \cap A_t\), as described in line 10.

Computing the differences for mappings at the instance-level is more complex. Specifically, this requires a comparison of the trace translations with each other. By abstracting from process model activities to a set of symbols of an
alphabet $A$ (as we have done throughout this work), each trace translation represents a sequence of characters, i.e., a string, from $A$, i.e., $\sigma(t) = \{a, b, c, d\}$ equals the string $abcd$. Given such character sequences, we can employ a string-difference algorithm by Myers [33] to efficiently compute the difference between two character sequences, which find the difference between two strings by identifying the shortest path in an edit graph (line 15).

For instance, sequences $abde$ and $acde$ yield the difference $\delta = \{B, C\}$. The union of all differences that exist among trace translations in $\Sigma_t$ then represents the set of activities affected by mapping uncertainty (lines 15–16).

### 5.3 Affected Fragment Identification

Given a set $U_t$ of activities affected by uncertainty, the next step is to determine to which SESE fragments of a decomposed process model these activities relate. To do this, we check which fragments do not contain any activities from the set $U_t$. Formally, we define the set of certain (i.e., fragments unaffected by uncertainty) fragments as $S_c(t) = \{S \in S \mid T(S) \cap U_t = \emptyset\}$. The set $S_c(t)$ can be efficiently computed in a top-down manner, as illustrated in Algorithm 2. Given a fragment $S$ in the RPST, we first determine if the fragment does not contain any activity in the set of uncertain activities $U_t$ (line 4). If this is the case, then we know that $S$ is not affected by uncertainty and should be included in $S_c(t)$, but we also know that none of the descendants (i.e., elements below $S$ in the RPST) contains any activities from $U_t$. Therefore, also these descendants are included in $S_c(t)$ (line 5). In case $S$ does contain activities from $U_t$, the algorithm recursively moves to the child-nodes of $S$ in lines 8–10.

![Algorithm 2. Identifying Fragments Affected by Mapping Uncertainty](image)

For example, given a set of uncertain activities $U_t = \{E, F\}$, we obtain the set of unaffected fragments $S_c(t) = \{S_1, S_2, S_3, S_4, S_6, S_7, S_8, S_9\}$. This set does not include the fragments $S_5$ and $S_{10}$, which, respectively, encompass activities $E$ and $F$ and it neither includes any of their super-fragments ($S_{10}$, $S_6$, $S_3$, and $S_2$). The complement of the set $S_c(t)$, which we denote as $S_u(t)$, contains all fragments that are affected by uncertainty. We take these two sets as input to the final step of our approach.

### 5.4 Conformance Checking

After determining which fragments of a process model are affected by mapping uncertainty, we can perform the necessary conformance checks. Here, we apply the notion that for fragments not affected by uncertainty, i.e., the set $S_c(t)$, we only have to check the conformance of a single trace translation $\sigma(t) \in \Sigma_t$ in order to determine the conformance of all translations in $\Sigma(t)$. Because these fragments are not affected by uncertainty, all translations are either conforming or all are non-conforming to fragments in $S_c(t)$. As described in Section 4.2, we perform the conformance check between a single trace translation and a fragment by employing the method from [29]. Naturally, when all trace translations have the same conformance, the $ProbConf$ metric will yield a value of either 0.0 or 1.0 for the fragments in $S_c(t)$.

For fragments that are affected by mapping uncertainty, in the set $S_u(t)$, we need to determine the conformance of all trace translations in order to obtain a correct $ProbConf$ value. Therefore, we define the conformance of all trace translations in $\Sigma(t)$ with respect to a fragment $S$ and then compute the probabilistic conformance as $ProbConf_f(t, S) = \sum_{\sigma \in \Sigma(t)} \theta(\sigma)$. After computing $ProbConf_f(t, S)$ for all fragments in $S_c(t)$ and $S_u(t)$, we have obtained the necessary results. These results can, for instance, be visualized in the manner depicted in Fig. 5. These results represent the final output of our conformance-checking technique.

### 6 Evaluation

This section presents a two-stage evaluation in which we assess the usefulness of behavioral space-based conformance checking and the efficiency of our computation approach. In the first part of the evaluation, we assess how the impact of mapping uncertainty on conformance checking can be reduced by using behavioral spaces as a basis. In particular, we observe for how many traces our technique is able to provide non-probabilistic conformance-checking results as compared to traditional conformance-checking techniques. In the second part of the evaluation, we analyze the computational efficiency of our computation approach and compare it to a benchmark.

In the remainder of this section, Section 6.1 first introduces the test collections used for the evaluation experiments. Section 6.2 presents the first part of the evaluation, focusing on the usefulness of our proposed technique. Section 6.3 presents the second part, focusing on the efficiency of our computation approach. Finally, Section 6.4 discusses limitations of the conformance-checking technique and its evaluation.

#### 6.1 Test Collections

To perform the evaluation, we combine a collection of real-world business process models with a collection of synthetic, generated models.

**Real-World Models.** As a real-world collection, we employ the BIP process library, which comprises 886 process models that were created in process automation projects in various industry domains, such as financial services, automotive, telecommunications, construction, supply chain, health care, and customer relationship management [34]. We picked this process model collection because it has already been used in a variety of related evaluations, among others to test several event-to-activity mapping approaches [7], [12]. Hence, we
TABLE 2
Characteristics of the Test Collections

<table>
<thead>
<tr>
<th>Models with</th>
<th>Real-world</th>
<th>Synthetic</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Loops</td>
<td>63</td>
<td>63</td>
<td>126</td>
</tr>
<tr>
<td>Skips</td>
<td>0</td>
<td>139</td>
<td>139</td>
</tr>
<tr>
<td>Non-free choice</td>
<td>0</td>
<td>104</td>
<td>104</td>
</tr>
<tr>
<td>Total</td>
<td>598</td>
<td>650</td>
<td>1248</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Places</td>
<td>8.8</td>
<td>34</td>
<td>17.7</td>
<td>96</td>
<td>13.4</td>
</tr>
<tr>
<td>Transitions</td>
<td>7.4</td>
<td>40</td>
<td>17.7</td>
<td>100</td>
<td>12.8</td>
</tr>
<tr>
<td>And-splits</td>
<td>0.7</td>
<td>5</td>
<td>4.3</td>
<td>62</td>
<td>2.6</td>
</tr>
<tr>
<td>Xor-splits</td>
<td>0.8</td>
<td>12</td>
<td>4.5</td>
<td>33</td>
<td>2.6</td>
</tr>
<tr>
<td>Silent steps</td>
<td>2.2</td>
<td>29</td>
<td>6.1</td>
<td>76</td>
<td>2.7</td>
</tr>
<tr>
<td>Skips</td>
<td>0.0</td>
<td>0</td>
<td>0.2</td>
<td>4</td>
<td>0.1</td>
</tr>
</tbody>
</table>

believe that results obtained by using this collection present a realistic view on the applicability of the event-to-activity mapping approach against which we compare our conformance-checking technique. Following the same filtering steps used in [7], we omitted any process models with soundness issues such as deadlocks or livelocks. Furthermore, we omitted six models for which the employed event-to-activity mapping approach was not able to produce a mapping due to memory shortage. As a result of the filtering, a collection of 598 process models remains available for usage in our evaluation.

Synthetic Models. We have generated a collection of 650 synthetic models that allows us to assess the impact of model characteristics such as loops, arbitrary skips, and non-free choice constructs on the performance of our approach. We employed the state-of-the-art process model generation technique from [35] due to its ability to also generate non-structured models, e.g., models with non-free choice constructs [36]. For the generation, we employed the default parameters used by the developers of the approach in their evaluation.

As shown in Table 2, the test collections contain models that differ considerably in their size, complexity, and characteristics. For this reason, as well as due to the widely-established relevance of the BIT process library, we believe that our test collection is well-suited to achieve a high external validity of the results.

6.2 Deterministic Conformance Evaluation

This section presents our evaluation regarding the utility of behavioral space-based conformance checking. To assess the utility of our approach, we observe for how many traces our approach is able to provide non-probabilistic, i.e. deterministic, conformance-checking results. We compare this to the number of traces for which traditional conformance-checking techniques can provide the same results. We note that these results are independent of the choice for a particular traditional conformance-checking technique, since none of the other techniques are able to provide trustworthy results in the presence of mapping uncertainty.

6.2.1 Setup

Fig. 7 depicts the three main steps of our evaluation setup. To perform these steps, we employ the ProM6 framework, which provides a vast amount of so-called plug-ins that implement process mining techniques. In the first two steps of this evaluation, we build on existing plug-ins for event-to-activity mapping techniques, as described in [7]. For the third step, we implemented the generation of behavioral spaces and our proposed technique for conformance checking as a plug-in, which is available as part of the BehavioralSpaces package in ProM6. In this implementation, we employ the technique for decomposed conformance checking, as described in [29], available in the JorgeMunoz-Gama package.

In step 1 of the evaluation, we first generate an event log for each of the 1248 process models in the test collection. In line with the evaluation in [7], we generate a log containing 1000 traces for each model. For process models that include loops, we generate traces with a maximum length of 1000 events. Since we are interested in conformance checking, we transform these fully conforming logs into logs containing non-conforming behavior. We achieve this by using a noise-insertion plug-in in ProM. This plug-in randomly adds noise to a log (i.e. non-conforming behavior) by shuffling, duplicating, and removing events for a given percentage of traces. In this manner, we generate 11 different event logs, containing 0%, 10%, ..., 90%, 100% noise.

In step 2, we take a process model and an accompanying event log and use the mapping technique from [7] to establish an event-to-activity mapping. We have selected this particular technique for the real-world model collection because it returns all potential mappings in case of uncertainty. Furthermore, the technique is relatively robust in the context of non-conforming behavior. For the synthetic data collection, we use the positional-based matcher from [20], since the technique presented in [7] is not suitable in the presence of non-free choice constructs. In case the approach can compute a single mapping, i.e. there is no mapping uncertainty, we can conclude that for this process model and event log, traditional conformance-checking techniques suffice to determine the conformance of all traces in the log. If the mapping approach returns multiple possible mappings, i.e. there is mapping uncertainty, we continue with the third step of the evaluation.

In step 3, we first construct a behavioral space for a trace based on the uncertain event-to-activity mapping EA established in the previous step. We obtain a behavioral space by creating a trace translation for each of the potential event-to-activity mappings included in EA, as described in Section 4.1. Afterwards, we perform a conformance check between the obtained behavioral space and the process model using the approach described in this paper. If this method returns a ProbConf value of 0.0 or 1.0 for the entire process model, we

3. See www.promtools.org for more information and to download the framework.
4. Provided by the Event2ActivityMatcher package.
can conclude that our technique is able to provide a non-probabilistic conformance-checking result for the trace. This means that we know whether or not \( t \) is conforming with certainty. For other values, also the consideration of behavioral spaces does not suffice to be sure about the conformance of \( t \). Nevertheless, our technique still obtains probabilistic results and diagnostic information, whereas traditional conformance-checking techniques cannot provide any trustworthy results for these cases.

### 6.2.2 Results

In this section, we first consider the overall performance of our technique in practical settings based on the evaluation results obtained for the real-world model collection. Subsequently, we investigate the impact of control-flow constructs on the performance based on the collection of synthetic models.

**Real-World Collection.** Fig. 8 presents the results of our evaluation experiments for the real-world model collection. The figure illustrates for which percentage of traces deterministic conformance-checking results are obtained by our and traditional techniques.

For noise level 0, where all traces in the event logs conform to the process models, we observe that the mapping approach establishes a single event-to-activity mapping for 71 percent of the models in the collection, which means that traditional techniques can provide (deterministic) results 71 percent of the traces. Because these logs do not contain non-conforming behavior, the inability to establish mapping for certain models is caused by activities which are behaviorally identical to each other. Such cases can be seen for activities \( F \) and \( G \) of the running example. Because of these issues, traditional conformance-checking techniques cannot assess the conformance of 29 percent of the traces. However, by using behavioral spaces, we can still determine the conformance of a trace when mapping uncertainty is caused by such behavioral equivalent activities. Hence, by using our proposed conformance-checking technique, we can provide deterministic conformance-checking results for all traces.

For increasing noise levels, the ability of the mapping approach to establish a single event-to-activity mapping diminishes. For logs with 10 and 20 percent noisy traces the approach can still establish a mapping for approximately 66 percent of the process models, as indicated by the 66 percent deterministic conformance results in Fig. 8.

However, this percentage sharply drops to 33 percent certain results for event logs with 40 percent noise, followed by only 21 percent certainty for noise levels above 60 percent. As a result of these steep drops, the ability of traditional conformance-checking techniques to provide trustworthy conformance-checking results also sharply decreases. Although our behavioral space-based technique can also provide less deterministic results when the level of noise increases, this decrease is considerably less severe than for the benchmark. For instance, at 30 percent noise, our technique can still provide deterministic results for 83 percent, whereas the benchmark can only provide such results for 55 percent of the cases. For the highest noise levels, our technique can still provide deterministic results for approximately 30 percent of the traces, which means that the technique outperforms the benchmark by close to 50 percent.

In summary, traditional conformance-checking techniques become less and less useful. For high noise levels, they can provide results for as little as 21 percent of the traces. Although the deterministic results obtainable through conformance checking with behavioral spaces is also affected by the increased levels of noise, the impact is much smaller. Therefore, we can conclude that in practical scenarios our conformance-checking technique is much wider applicable than traditional conformance-checking techniques. Furthermore, a crucial aspect in favor of our conformance-checking technique is that even in cases where also our technique cannot provide deterministic conformance-checking results, our technique still provides trustworthy conformance-checking information in the form of probabilistic results and diagnostic insights.

**Synthetic Collection.** Table 3 provides an overview of the performance of our technique for the collection of synthetic models. Given that these models are all generated based on the same parameters, this collection allows us to accurately assess how the presence of certain control-flow constructs affects our technique’s performance. In particular, the table depicts the performance of the technique on the subset of models that contain loops, skips, and non-free choice constructs. From these results, we can observe that in particular non-free choice constructs affect the performance of our technique. For models with non-free choice constructs, the fraction of traces for which we can compute deterministic conformance-checking results is lower than for the overall collection, e.g. 0.73 versus 0.90 for 0 percent noise and 0.41 versus 0.52 for 40 percent noise. The presence of skips has also been shown to affect the performance of the approach, though the impact is lower in this case. However, the performance on models with loops is slightly higher when compared to the average. This is most likely because the presence of loops results in repeated occurrences of

### Table 3

<table>
<thead>
<tr>
<th>Models with</th>
<th>N</th>
<th>0%</th>
<th>20%</th>
<th>40%</th>
<th>60%</th>
<th>80%</th>
<th>100%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Loops</td>
<td>63</td>
<td>96.5</td>
<td>75.5</td>
<td>57.0</td>
<td>38.4</td>
<td>21.2</td>
<td>3.9</td>
</tr>
<tr>
<td>Skips</td>
<td>130</td>
<td>81.8</td>
<td>60.5</td>
<td>45.9</td>
<td>33.2</td>
<td>19.2</td>
<td>5.5</td>
</tr>
<tr>
<td>N-free choice</td>
<td>104</td>
<td>73.0</td>
<td>53.0</td>
<td>41.2</td>
<td>31.7</td>
<td>18.5</td>
<td>5.9</td>
</tr>
<tr>
<td>All models</td>
<td>650</td>
<td>89.8</td>
<td>68.9</td>
<td>52.1</td>
<td>36.1</td>
<td>19.9</td>
<td>4.0</td>
</tr>
</tbody>
</table>
subtraces, which can be particularly helpful when establishing event-to-activity mappings, resulting in less mapping uncertainty.

6.3 Computational Efficiency

In the second part of our evaluation, we evaluate the computational efficiency of our computation approach. As described in Section 5, our approach analyzes which fragments of a decomposed process model actually need to be recomputed for all trace translations, as a means to reduce the necessary number of conformance checks. To determine the gains obtained in this way, we compare the computation time to a benchmark. This benchmark is obtained by performing the conformance check for all trace translations for every fragment of a decomposition, rather than considering which fragments actually need to be recomputed for all translations. This part of the evaluation is conducted on the collection of real-world models.

6.3.1 Setup

For this evaluation experiment we focused on the time required to perform conformance checks using our technique and the benchmark. We performed this evaluation using the same sets of event logs, with varying noise levels, as used in the first part of the evaluation. Considering the setup depicted in Fig. 7, we start the measurement after we have decomposed a process model in step 3 of the evaluation. This means that we measure the time used for the actual conformance check, not for establishing the event-to-activity mapping and for process model decomposition. We performed the evaluation on an HP desktop with an $8 \times 3.60$ GHz Intel Core i7 processor and 8 GB RAM, running on 64-bit Ubuntu 16.04 and Java Virtual Machine 1.8. As a benchmark, we also measure the computation time that is required when all trace translations are compared against all process model fragments, i.e., the time that would be required without our proposed approach for efficient conformance checking.

6.3.2 Results

Fig. 9 depicts the efficiency gains that can be obtained by using our computation approach when compared to the benchmark. The percentage efficiency gained is here computed as $(1 - \frac{\text{time(approach)}}{\text{time(benchmark)}}) \times 100\%$.

The figure shows that these efficiency gains increase for higher levels of noise. This is the case because for higher levels of noise, the number of possible mappings generated by a mapping approach typically increases. In these cases, more time can be saved when performing conformance checks in a manner that does not require a full enumeration of all possible trace translations for every fragment of a decomposition. In particular, at 0 percent noise, our efficient approach only saves approximately 11 percent of the computation time on average. For this noise level, the mapping approach most often generates only a single mapping and an average of approximately 10 mappings per process. By contrast, for noise levels above 40 percent, our computation approach leads to a reduction of more than half of the throughput time. At higher noise levels, our approach saves approximately 70 percent of the computation time. This reduction can be explained by the large number of mappings generated by the mapping approach: an average of 136 mappings per process for event logs with a 100 percent noise level.

In summary, these results clearly illustrate that the computation approach described in Section 5 can yield significant gains in computational efficiency. In this way, the approach makes conformance checking more applicable in realistic settings.

6.4 Limitations

Our evaluation experiments demonstrate that our technique provides useful and efficient conformance-checking results in realistic settings. However, these results need to be considered against the background of certain limitations. In particular, we identify limitations related to the technique itself, limitations with respect to the expected input, and limitations related to the presented evaluation.

Our proposed technique has to be considered against the limitation that the obtained conformance-checking results are dependent on the quality of the event-to-activity mappings on which our approach builds, i.e. the results depend on the quality of the utilized mapping techniques. Most importantly, its results can be negatively affected if the correct mapping is not included in the set of potential mappings generated by a mapping approach. However, these issues rarely occurred during our evaluation experiments, especially for traces with relatively low levels of noise. This illustrates that the utilized mapping technique is well-suited for our purposes.

As for the expected input of our technique, it is important to note that the level of block-structuredness of the input model affects how detailed the computed conformance insights are. In case the input model consists of a single unstructured fragment, conformance-checking results can be only obtained on that level of granularity. However, since both industrial as well as academic modeling guidelines strongly advocate the use of block-structured models [37], [38], we do not expect this to represent a common issue. What is more, there are automatic techniques available to structure certain types of non-block-structured process models [39].

A limitation related to the evaluation of our technique is that our test collection consisted of partially synthetic data. While the process models used for the evaluation were obtained from a collection of real-world models, the event...
logs were automatically generated. This means that the obtained results may not fully reflect the situation in practice, where event logs related to the process models may have different characteristics. Nevertheless, we generated logs with varying levels of noisy behavior, which means that the utilized test collection contains behavior that can be observed in a variety of situations. Since our evaluation results show that our conformance-checking technique outperforms traditional techniques for all noise levels, we are confident that the improved performance also holds for real-world event logs.

7 RELATED WORK

This section discusses three streams of work related to our conformance-checking technique. Section 7.1 discusses application scenarios and techniques for conformance checking. Section 7.2 considers techniques for the establishment of event-to-activity mappings. Finally, Section 7.3 considers existing works that deal with data uncertainty in other application contexts.

7.1 Conformance Checking

Process conformance checking involves the comparison of observed process behavior to a process specification. These techniques are applied in various application scenarios, including process querying [40], legal compliance [41], and auditing [42]. Most conformance-checking techniques focus on the comparison of observed process behavior, as captured in event traces, to a process specification in the form of a process model, cf. [29], [32], [43], [44], [45], [46]. Recently, however, we also developed a technique for conformance checking for process specifications in the form of natural language texts [47].

The goal of conformance checking is primarily to determine if a trace of observed events conforms to the process specified by a process model. However, most conformance-checking techniques go beyond determining whether or not a trace conforms to a process model. They analyze non-conforming traces in order to determine their degree of non-conformance, as well as to investigate to which parts of a process the trace does and does not conform. Different types of conformance-checking techniques have been developed for this purpose. Examples include the seminal replay-based [2], [45] and alignment-based [32], [43] techniques, as well as the decomposition-based technique [29] utilized in this paper. While these techniques focus on conformance from a control-flow perspective, developments have also been made that check conformance with respect to other process perspectives, such as time-based [48] and database-based conformance [49].

Despite the vast number of existing conformance-checking techniques, all these techniques require the existence of a known event-to-activity mapping, a limitation which we overcome with the conformance-checking technique presented in this paper.

7.2 Mapping Events to Activities

The task of establishing a mapping between events and activities represents a so-called matching problem. Matching problems are addressed by matching techniques that set out to automatically identify relations between two artifacts [50]. A plethora of matching techniques have been developed and applied in various fields, including schema matching (cf. [13], [51], [52]), ontology alignment (cf. [15], [53], [54]), and process model matching (cf. [20], [55], [56]).

A variety of matching techniques [4], [8], [9], [12] have recently been developed that apply concepts from related matching fields to the task of matching events to activities. These techniques aim to identify events and workflow activities with similar characteristics. To achieve this, they consider a variety of information. For instance, techniques presented in [4], [8] compare the labels associated with events and tasks in order to determine their similarity. This supports the identification of events and activities with equal labels, as well pairs with similar labels, e.g. “ship product” and “product sent”. Other information taken into accounts by matchers are structural properties (indicating the relations that exist between different events and activities) [7], [12], work instructions associated with process models [4], and additional data associated with events [9].

A distinction between mapping approaches that is relevant for this paper exists between approaches that map at the event class-level and approaches that map events at an instance-level. Approaches of the former type, such as [7], map all occurrences of a particular event class $E_x$ to the same activity class. By contrast, instance-level techniques might map events of a particular class to different activities for different traces. For instance, an event of type $E_y$ might be mapped to activity $C$ for a trace $\tau$, but to activity $D$ for trace $\tau'$. 

7.3 Representing Data Uncertainty

To be able to reason about process conformance in the context of mapping uncertainty, we introduce the notion of probabilistic behavioral spaces in this paper. This concept is used to capture the implications of uncertainty in a manner that enables probabilistic reasoning about process conformance. In this way, our work relates to streams of research for reasoning in the presence of data uncertainty.

Data uncertainty is inherent to various application contexts, typically caused by data randomness, incompleteness, or limitations of measuring equipment [57]. This has created a need for algorithms and applications for uncertain data managements. As a result, the modeling of uncertain data has been studied extensively [58]. This has, lead to the development of various probabilistic and uncertain databases cf. [59], [60], [61], as well as a variety of querying and analysis algorithms for these data structures [62], [63].

Our notion of probabilistic behavioral spaces shares characteristics with solutions for probabilistic and uncertain databases. Most prominently, our notion of probabilistic behavioral spaces build on a concept of possible worlds used in databases to capture the various possible implications of data uncertainty for database instances [63]. We use a similar notion to capture the impact of mapping uncertainty on the process behavior that may be conveyed by an event trace. Furthermore, the process-orientation of behavioral spaces implicitly capture the dependencies that exist between uncertain events for a single trace. This is similar to the use of conditions to capture dependencies between uncertain database values, such as used by [61]. Despite
these similarities, the application contexts of these uncertain data models, mostly querying and data integration [58], differ considerably from the process-oriented view of probabilistic behavioral spaces used for conformance checking.

8 Conclusion

In this paper, we introduced a conformance-checking technique that can be used in the presence of uncertain event-to-activity mappings. Our technique provides conformance-checking results without the need to select a single, possibly incorrect mapping to base conformance checks on. This is achieved by considering the entire spectrum of possible mappings generated by event-to-activity mapping techniques and capturing this spectrum in a behavioral space. Our probabilistic conformance-checking metric then provides insights into the fraction of compliant mappings, as well as useful diagnostic information. Therefore, our conformance-checking technique avoids the risk of drawing incorrect conclusions about process conformance. A quantitative evaluation based on a large collection of real-world process models demonstrated that our technique can be used to obtain results in a vast number of cases where existing conformance-checking techniques fail to do so. Furthermore, we presented a computation approach that is shown to considerably reduce the time required to obtain conformance-checking results.

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References


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