All-optical logic based on ultrafast gain and index dynamics in a semiconductor optical amplifier


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Invited Paper

Abstract—We investigate nonlinear carrier dynamics in a multiquantum-well semiconductor optical amplifier (SOA) in the context of ultrafast all-optical logic. A rate-equation model is presented that accounts for two-photon absorption, free-carrier absorption, self- and cross phase modulation, carrier heating, spectral, spatial hole burning, and self- and cross polarization modulation. The nonlinear refractive index dynamics is investigated theoretically and experimentally. We find nonlinear phase changes larger than \( \pi \) radians, which recovers on a timescale in the order of 1 ps. We also investigate a nonlinear AND gate that consists of an SOA that is placed in an asymmetric Mach–Zehnder interferometer. We show that the gate can be operated using 800-fJ optical pulses with duration of 200 fs while having a contrast ratio larger than 11 dB.

Index Terms—Optical logic, optical signal processing, ultrafast carrier dynamics, semiconductor optical amplifier.

I. INTRODUCTION

DIGITAL optical techniques are expected to become increasingly important in futuristic ultrahigh capacity telecommunication networks. Optical communications systems with a capacity of hundreds of gigabits per second are commercially available today, and the capacity has been pushed above 10 Tb/s in research laboratories. The highest bit rate per channel that has been reached is greater than 1 Tb/s [1].

For data rates greater than 40 Gb/s, transmission systems often use optical techniques, since direct electronic processing is limited in speed. In optical time-domain multiplexed systems, the data at a transmission channel are demultiplexed to a lower bit rate using a clocked optical switch. Such an optical switch can be realized by employing photo-generated changes in carrier density of semiconductor optical amplifiers (SOAs). SOAs are attractive as such a nonlinear element, since they provide a high gain and exhibit a strong refractive-index change and allow photonic integration [2].

To obtain optical switching, the SOA is usually placed in an interferometer. Optical switching in the picosecond regime has been shown using a variety of configurations such as the symmetric Mach–Zehnder (SMZ) interferometer, the ultrafast nonlinear interferometer (UNI), and the terahertz optical asymmetric demultiplexer (TOAD) [3]–[8].

In most applications, SOAs are operated by utilizing nonlinearities introduced by resonant optical transitions. The speed of all-optical switches based on SOA nonlinearities is determined by the carrier dynamics of the SOA. In particular, if resonant transitions are employed by using photons with an energy corresponding to the band edge, the switching speed is restricted by the carrier lifetime, which determines the speed that carriers can be injected in the active region. Faster operation can be obtained by artificially reducing the carrier lifetime by using an additional holding beam [9], [10]. Also, it has been shown by using photons with a photon energy below the bandgap that the SOA gain recovery time is determined by the length of the control pulse due to the instantaneous two-photon-absorption (TPA) transient [11], [12]. It should be noted however, the corresponding refractive index recovery is slower, since, due to the Kramers–Kronig relationship, the refractive index also depends on the gain at other wavelengths [12].

The optical switching configurations mentioned above have in common that they allow operation at high repetition rates by using differential interference effects to overcome the speed limitations imposed by the carrier lifetime, while still utilizing resonant nonlinearities. It has been shown by combining switches based on nonlinear interference effects that more sophisticated all-optical logic functionals can be realized. In particular, proof of concept has been given for optical address recognizers [13]–[15], optical bit-level synchronizers [16], [17], optical clock recovery circuits [18], optical shift registers with inverters [19], [20], optical memories with read–write abilities [21]–[24], binary half- and full adders [25], [26], pseudorandom number generators [27], optical parity checkers [28], and optical packet switches [29].
The processing speed of the digital optical logic based on resonant optical transitions as described above is restricted to approximately 200 GHz [2]. The reason for this is that the SOA recovery depends on the carrier lifetime which makes it so that the SOA fully recovers in approximately 1 ns. Differential operation can partly overcome this issue but at switching rates higher than 200 GHz [2], the SOA carrier population cannot establish an equilibrium Fermi–Dirac distribution within one bit-time [30].

Meanwhile, research has been carried out to investigate SOA gain and index dynamics at subpicosecond timescales. Early experiments indicated that strong nonlinearities on sub picosecond timescales in bulk and multiquantum-well (MQW) SOAs can take place [30]–[34]. These nonlinearities were soon identified to be related to nonequilibrium changes in the carrier energy distribution [31], [35]. The main nonlinear processes responsible for these nonequilibrium changes were identified to be spectral hole burning, carrier heating, and TPA [36]–[38].

Early experimental results on nonlinear index changes on subpicosecond timescales were published in [12], [39]–[41]. Rate-equation models that describe nonlinear carrier dynamics on subpicosecond timescales were firstly published in [36], [37], [42], [43]. Later microscopic models that describe the SOA carrier dynamics on subpicosecond timescales have been published [44], [45].

Switching experiments, employing femtosecond pulses in an ultrastable nonlinear interferometer were reported in [46]–[48]. Wavelength switching experiments employing ultrashort pulses were published in [49]–[51]. In this paper, we investigate nonlinear carrier dynamics in an MQW SOA in the context of ultrastable all-optical logic. The nonlinear carrier dynamics of an MQW SOA is investigated using a rate-equation model that accounts for TPA, free-carrier absorption (FCA), self- and cross-phase modulation, carrier heating, spectral, spatial hole burning, and self- and cross-polarization modulation. In particular, attention is paid to the nonlinear refractive index dynamics that is also investigated experimentally. We find using an experimental approach related to spectral interferometry, nonlinear phase changes in an MQW SOA larger than π radians that recover on a timescale in the order of 1 ps. We also investigate a nonlinear AND gate that consists of a single MQW SOA that is placed in an SMZ interferometer. We show that the gate can be operated using 800-nJ optical pulses with duration of 200 fs while having a contrast ratio larger than 11 dB.

II. THEORY

A rate-equation model that describes polarization dependent nonlinear gain and index dynamics in SOAs on subpicosecond timescales is presented in [52]. This model takes into consideration carrier dynamics on femtosecond timescales driven by TPA and FCA, and accounts for self- and cross-phase modulation, carrier heating, and spectral and spatial hole burning as well as self- and cross-polarization modulation. As shown in [24], the polarization dependent gain saturation is taken into account by assuming that the polarized optical field can be decomposed into transverse electric (TE) and transverse magnetic (TM) components that propagate “independently” through the SOA, although they have indirect interaction with each other via the gain saturation. We have accounted for different TE and TM gains by assuming that these polarizations couple to different hole reservoirs. This assumption is justified by the fact that in zinc-blende structures such as GaAs and InP, the optical transitions occur between an $l = 0$ type conduction band state and a (degenerate) $l = 1$ type valence band state. Two out of the three possible transition types are selected by the TE and TM polarizations with the two corresponding inversions. In the isotropic bulk situation, these two transitions will occur in a fully symmetric manner, but we are now interested in the case where tensile strain is built into the bulk medium, and this will cause an asymmetry between the two transition types, such that TM will be favored over TE transitions. The model does not account for the propagation of hybrid modes and for polarization dependence introduced by the device structure.

The incoming arbitrarily polarized electric fields is decomposed in a component parallel to the layers in the waveguide (χ component, TE mode) and a perpendicular component (γ component, TM mode). These two polarization directions are along the principal axes $(\hat{x}, \hat{y})$ that diagonalize the wave propagation in the SOA. In fact, apart from their indirect interaction through the carrier dynamics in the device, these two polarizations propagate independently from each other. The total electric field is given by

$$E^{TE/TM}(z, t) = [A^{TE}(z, t)\hat{x} + A^{TM}(z, t)\hat{y}] e^{i(\omega_0 t - k_0 z)} + c.c.;$$

$$S^{TE/TM}(z, t) = [A^{TE/TM}(z, t)t^2]$$  \hspace{1cm} (1)$$

where $k_0 = (n(\omega_0)/c)\omega_0$, $n(\omega_0)$ is the refractive index taken at the central frequency $\omega_0$ and $c$ the light velocity in vacuum, and $\hat{x}$ and $\hat{y}$ are unit vectors along the $x$ and $y$ directions. The frequency $\omega_0$ has been chosen such that the complex pulse amplitudes $A^{TE/TM}(z, t)$ are slowly varying functions of $z$ and $t$. The propagation equations for the TE and TM modes are

$$\frac{\partial}{\partial z} + \frac{1}{v_g} \frac{\partial}{\partial t} \right) A^{TE}(z, t) = \left\{ \begin{array}{l}
\frac{1}{2} \Gamma^{TE}(1 + i\alpha) g^{TE}(z, t) \\
- \frac{1}{2} \alpha_{int} - \frac{1}{2} \Gamma^{TE}/2(1 + i\alpha) \\
\times [S^{TE}(z, t) + S^{TM}(z, t)] \\
- \frac{1}{2} \Gamma^{TE} \beta_n n_c(z, t) \\
- \frac{1}{2} \Gamma^{TE} \beta_n n_g(z, t) \right\} \times A^{TE}(z, t)$$

$$\frac{\partial}{\partial z} + \frac{1}{v_g} \frac{\partial}{\partial t} \right) A^{TM}(z, t) = \left\{ \begin{array}{l}
\frac{1}{2} \Gamma^{TM}(1 + i\alpha) g^{TM}(z, t) \\
- \frac{1}{2} \alpha_{int} - \frac{1}{2} \Gamma^{TM}/2(1 + i\alpha) \\
\times [S^{TE}(z, t) + S^{TM}(z, t)] \\
- \frac{1}{2} \Gamma^{TM} \beta_n n_c(z, t) \\
- \frac{1}{2} \Gamma^{TM} \beta_n n_g(z, t) \right\} \times A^{TM}(z, t)$$  \hspace{1cm} (2)$$

where $\Gamma^{TE/TM}$ is the total nonlinear gain rates and $\alpha_{int}$ is the total internal loss rate.
where the SOA parameters and their physical definitions are listed in Table I. The first term on the right-hand side of (2) and (3) represents the linear gain. \( \alpha \) is the phase modulation parameter (or linewidth enhancement factor). The second term represents the TPA that is modeled by assuming that both the TE and TM modes are involved in the TPA process, where \( \alpha_2 \) is the corresponding phase modulation parameter, while the last two terms represent the FCA in the conduction and valence bands. The complex field amplitudes can be related to the intensities \( S_{\text{TE/TM}}(z,t) \) and the phases \( \phi_{\text{TE/TM}}(z,t) \) through the well-known relationship

\[
A_{\text{TE/TM}}(z,t) = \sqrt{S_{\text{TE/TM}}(z,t)}e^{i\phi_{\text{TE/TM}}(z,t)}.
\]

The gains for both modes can be expressed as

\[
g_{\text{TE}}(z,t) = \frac{1}{v_g}a_{\text{TE}}(\omega_0)[n_c(z,t) + n_x(z,t) - N_0]
\]

(4)

\[
g_{\text{TM}}(z,t) = \frac{1}{v_g}a_{\text{TM}}(\omega_0)[n_c(z,t) + n_y(z,t) - N_0]
\]

(5)

where \( a_{\text{TE/TM}}(\omega_0) \) are the gain coefficients. Our model takes into account three bands. The numbers of electrons that are involved in the optical transition in the conduction band is \( n_c(z,t) \). We have two reservoirs of holes identified with index \( x \) and \( y \). Holes identified with \( x \) couple with electrons through TE polarized light. The number of holes that can participate in this transition is \( n_x(z,t) \). Similarly, holes identified with \( y \) couple with electrons through TM polarized light. The corresponding reservoir of holes that can participate in the optical transition is \( n_y(z,t) \). \( N_0 \) is the total number of states involved in the stimulated emission. The carrier densities satisfy

\[
\frac{\partial n_c(z,t)}{\partial t} = \frac{n_c(z,t) - \bar{n}_c(z,t)}{\tau_{1c}} - v_g g_{\text{TE}}(z,t)S_{\text{TE}}(z,t) - v_g g_{\text{TM}}(z,t)S_{\text{TM}}(z,t) - n_c(z,t)/\tau_{1c}v_g[\delta S_{\text{TE}}(z,t) + \delta S_{\text{TM}}(z,t)]
\]

(6)

\[
\frac{\partial n_x(z,t)}{\partial t} = \frac{n_x(z,t) - \bar{n}_x(z,t)}{\tau_{1x}} - v_g g_{\text{TE}}(z,t)S_{\text{TE}}(z,t) - n_x(z,t)/\tau_{1x}v_g[\delta S_{\text{TE}}(z,t) + \delta S_{\text{TM}}(z,t)]
\]

(7)

\[
\frac{\partial n_y(z,t)}{\partial t} = \frac{n_y(z,t) - \bar{n}_y(z,t)}{\tau_{1y}} - v_g g_{\text{TM}}(z,t)S_{\text{TM}}(z,t) - n_y(z,t)/\tau_{1y}v_g[\delta S_{\text{TE}}(z,t) + \delta S_{\text{TM}}(z,t)]
\]

(8)

---

**TABLE I**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Value</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Active volume</td>
<td>( V = L \times W \times D )</td>
<td>750 \times 2 \times 0.1</td>
<td>( \mu m^3 )</td>
</tr>
<tr>
<td>Confinement factor</td>
<td>( \Gamma_{\text{TE}}, \Gamma_{\text{TM}}, \Gamma_2 )</td>
<td>0.032, 0.021, 0.09</td>
<td></td>
</tr>
<tr>
<td>Phase modulation coefficients</td>
<td>( \alpha, \alpha_2 )</td>
<td>1.2, -1.5</td>
<td></td>
</tr>
<tr>
<td>FCA coefficients</td>
<td>( \beta_c, \beta_v )</td>
<td>( 1 \times 10^{10}, 0 )</td>
<td>( \mu m^3 )</td>
</tr>
<tr>
<td>Electron-hole pair lifetime</td>
<td>( \tau_\text{s} )</td>
<td>1.3</td>
<td>ns</td>
</tr>
<tr>
<td>Gain coefficient</td>
<td>( a_{\text{TE}}(\omega_0), a_{\text{TM}}(\omega_0) )</td>
<td>( 7.0 \times 10^3, 5.5 \times 10^3 )</td>
<td>( \mu m^3 / ps )</td>
</tr>
<tr>
<td>Group velocity</td>
<td>( v_g )</td>
<td>100</td>
<td>( \mu m / ps )</td>
</tr>
<tr>
<td>Internal loss</td>
<td>( \alpha_{\text{init}} )</td>
<td>0.00175</td>
<td>( \mu m^{-1} )</td>
</tr>
<tr>
<td>Optical transition energies</td>
<td>( E_c, E_{2c} )</td>
<td>0.03, 0.7</td>
<td>eV</td>
</tr>
<tr>
<td>Optical transition energies</td>
<td>( E_c, E_{2c} )</td>
<td>0.003, 0.07</td>
<td>eV</td>
</tr>
<tr>
<td>Carrier-carrier scattering times</td>
<td>( \tau_{1c}, \tau_{1v} )</td>
<td>0.1, 0.05</td>
<td>ps</td>
</tr>
<tr>
<td>Carrier-phonon relaxation times</td>
<td>( \tau_{0c}, \tau_{0v} )</td>
<td>0.7, 0.25</td>
<td>ps</td>
</tr>
<tr>
<td>TPA coefficient</td>
<td>( \beta_2 )</td>
<td>( 2.5 \times 10^9 )</td>
<td>( \mu m^3 )</td>
</tr>
<tr>
<td>Optical transition state density</td>
<td>( N_0 )</td>
<td>( 1.25 \times 10^6 )</td>
<td>( \mu m^{-3} )</td>
</tr>
</tbody>
</table>
The first terms on the right-hand sides of (6)–(8) describe the relaxation of the electrons and holes to their quasi-equilibrium values \( \bar{n}_q(z,t), \bar{n}_h(z,t) \) that are specified later. These relaxation processes are driven by the electron–electron and hole–hole interactions with typical timescales of 50–100 fs. The second terms describe the stimulated emission, and the third term describes FCA. Before the SOA model can be completed, we need to formulate the equation for the electron–hole pair density \( N(z,t) \)

\[
\frac{\partial N(z,t)}{\partial t} = \frac{I}{eV} - \frac{N}{\tau_s} - v_g \left[ g^{\text{TE}}(z,t) S^{\text{TE}}(z,t) + g^{\text{TM}}(z,t) S^{\text{TM}}(z,t) \right] + v_a \beta_2 \left[ S^{\text{TE}}(z,t) + S^{\text{TM}}(z,t) \right]^2 \tag{9}
\]

where it is noted that \( N(z,t) \) counts all the electron-hole pairs, including those that are not directly available for stimulated emission. The energy densities satisfy

\[
\frac{\partial U_c(z,t)}{\partial t} = \beta \bar{n}_o \bar{n}_i v_g \left[ S^{\text{TE}}(z,t) + S^{\text{TM}}(z,t) \right] - E_c v_g g^{\text{TE}}(z,t) S^{\text{TE}}(z,t) + g^{\text{TM}}(z,t) S^{\text{TM}}(z,t) + E_c \beta_2 \left[ S^{\text{TE}}(z,t) + S^{\text{TM}}(z,t) \right]^2 - U_c(z,t) = U_c(z,t) \tag{10}
\]

\[
\frac{\partial U_v(z,t)}{\partial t} = \beta \bar{n}_o \bar{n}_i v_g \left[ S^{\text{TE}}(z,t) + S^{\text{TM}}(z,t) \right] - E_v v_g g^{\text{TE}}(z,t) S^{\text{TE}}(z,t) + g^{\text{TM}}(z,t) S^{\text{TM}}(z,t) + E_v \beta_2 \left[ S^{\text{TE}}(z,t) + S^{\text{TM}}(z,t) \right]^2 - U_v(z,t) = U_v(z,t) \tag{11}
\]

where \( U_c(z,t) \) represents the energy density in the conduction band and \( U_v(z,t) \) the overall energy density in the valence band. In these equations, the first terms describe the change in energy density due to FCA. The second terms describe the contribution of the stimulated emission, and the third terms account for the TPA. The last term represents the relaxation to equilibrium due to carrier–phonon interactions.

The carrier density \( N(z,t) \) and the energy density \( U_c(z,t) \) are needed to self-consistently calculate in each time step the quasi-Fermi level \( E_{f,c}(z,t) \) and temperature \( T_c(z,t) \) of the electrons, using

\[
N(z,t) = \frac{1}{V} \sum_k F \left( E_{f,c}(z,t), T_c(z,t), \frac{\hbar^2 k^2}{2 m_e^*} \right) \tag{12}
\]

\[
U_c(z,t) = \frac{1}{V} \sum_k \frac{\hbar^2 k^2}{2 m_e^*} F \left( E_{f,c}(z,t), T_c(z,t), \frac{\hbar^2 k^2}{2 m_e^*} \right) \tag{13}
\]

where \( F(\mu, T, E) \) is the Fermi–Dirac distribution function defined as

\[
F(\mu, T, E) = \frac{1}{1 + \exp \left( \frac{E - \mu}{kT} \right)} \tag{14}
\]

A similar procedure can be used to compute the Fermi levels and temperatures in the valence band, and this one has to correct with a factor of two, since there are two subbands involved. The quasi-equilibrium values \( \bar{n}_c(z,\tau) \) are given by

\[
\bar{n}_c(z,t) = N_0 F \left( E_{f,c}(z,t), T_c(z,t), \frac{\hbar^2 k^2}{2 m_e^*} \right) \tag{15}
\]

\[
\bar{n}_v(z,t) = f \bar{n}_h(z,t) \tag{16}
\]

and the quasi-equilibrium values \( \bar{U}_{c,v}(z,t) \) are

\[
\bar{U}_{c,v}(z,t) = \frac{1}{V} \sum_k \frac{\hbar^2 k^2}{2 m_{e,v}^*} F \left( E_{f,c,v}(z,t), T_L, \frac{\hbar^2 k^2}{2 m_{e,v}^*} \right) \tag{17}
\]

where \( T_L \) is the lattice temperature and \( f \) is the population imbalance factor describing the gain anisotropy introduced by tensile strain in the SOA. Equation (16) describes how the equilibrium populations \( \bar{n}_c(z,\tau) \) and \( \bar{n}_h(z,\tau) \) are clamped to each other as a consequence of tensile strain [24]. In case of unstrained bulk material, the gain will be isotropic and \( f = 1 \). In case of tensile strain, TM gain will be larger than TE, i.e., \( f < 1 \). For the energy relaxation, the temperature must be taken equal to the lattice temperature \( T_L(300 \text{ K}) \).

We are aware of the fact that neglecting the gain and group velocity dispersion in our model for pulse propagation in an SOA limits the applicability of our model [53], [54]. When the pulse duration is as short as 50–100 fs, we can no longer expect good agreement between our model and measurements. However, in view of the apparently successful application of earlier models for pulses as short as 200 fs, we expect that the present model should be applicable for pulses of the same duration, especially when the central pulse frequency coincides with the gain maximum [36], [37], [42], [55]. Using the gain curves of the SOA that are used in our experiments [56], we have estimated, assuming a pulse with a spectral width of 20 nm, that for a 750-μm-long amplifier, only minor changes occur in the pulse shape. It should be remarked, however, that large distortions on the pulse shape could be expected if the central pulse frequency is close to or at the zero gain region (at transparency). In this case, large changes in the pulse shape take place, which could even lead to pulse breakup [57].

Moreover, we want to remark that we have modeled the phase change by using a constant linewidth enhancement factor that is defined in the usual way [53], [55]. Although this ignores dispersive effects due to strong variations in the carrier density, such a treatment leads to results that are in agreement with experimental results.

Finally, we did not account for different group velocity dispersion coefficients for the TE and TM modes. Numerical simulations show that the pulse broadening due to group velocity dispersion is approximately 5% for a 500-μm-long SOA, which
Fig. 1. Measured and computed polarization dependent amplification for the TE and TM modes as a function of the pump pulse energy. The diamond-shaped points represents the measured amplification for the TE mode and the star-shaped points represent the measured data for the TM mode. The dashed line represents the computed result for the TE mode and the solid line represents the computed result for the TM mode. The SOA injection current was 200 mA and in the computations, we used $f = 0.8$.

is negligible with respect to the pulse broadening due to gain saturation. It is shown in [58] that the difference in the group velocity between the TE and TM modes is in the order of 1%. We estimate that for a 500-μm-long SOA, the pulse distortion effects remain far below 10%. This implies that for a not too long amplifier pulse pattern effects due to birefringence of the SOA are negligible.

III. SIMULATION RESULTS

The set of (2)–(17) is solved numerically. In our simulations, the SOA length is 750 μm, and the active volume of 150 μm$^3$. We will consider optical pulses with Gaussian shape [200 fs, full-width at half-maximum (FWHM)] as input. The SOA pump current is 120 mA. All other SOA parameters are listed in Table I. These parameters characterize the SOA used in the experiments in the sections that follow. The confinement factor $\Gamma_{TM}$ is chosen to be 30% less than $\Gamma_{TE}$ (see Table I) [58], [59].

It should be noted, however, that the SOA parameters $N_0$, $G_{TE/TM}$, $\alpha_{int}^{TE/TM}$, and $\nu_g^{TE/TM}$ cannot be estimated accurately. We have solved this problem by compensating the combined uncertainties in these parameter values by assigning values to $f$ and $\alpha_{TE/TM}^{TM}(\omega_0)$ in such a way that the SOA gain corresponds to typical values. In the simplest approach, one would choose $a_{TE}^{TM}(\omega_0) = a_{TM}^{TM}(\omega_0)$, which is correct in case of isotropic gain, whereas $f$ can be estimated from the measured TE and TM amplification curves by using (4) and (5) and (15) and (16). In this case, the polarization dependent gain could be totally explained by the band filling effects that are represented by the factor $f$. In a somewhat more complicated approach, one can assume different values for $a_{TE}^{TM}(\omega_0)$ and $a_{TM}^{TM}(\omega_0)$ as in [24] for a continuous-wave analysis. The difficulties in estimating $f$ and $\alpha_{TE/TM}^{TM}(\omega_0)$ may be inherent to our modeling the SOA strain in terms of the population imbalance factor $f$. In a more accurate, but also much more complicated, model, one can calculate the band structure and transition matrix elements in the presence of tensile strain and keep track of the different optical transitions involved as well as the relevant populations. This would, however, extend beyond the scope of the present approach [60], [61].

The TPA coefficient has been chosen in such a way that the SOA gain saturation is in agreement with experimental results presented in [57]. In Fig. 1, the SOA gain is presented as a function of the pulse energy. It follows from Fig. 1 that the net amplification becomes negative for pulse energies larger than 3 pJ in the TE mode and 1.8 pJ in the TM mode. The curve presented in Fig. 1 is in quantitative agreement with experimental results presented in [57]. The net attenuation is due to the combined effects of TPA and FCA. It follows from Fig. 1 that for large pulse energies, the difference in TE and TM gain almost vanishes, which can be explained by the fact that both modes equally contribute to the TPA. Thus, for high energetic optical pulses, the TPA terms in (2) and (3) dominate.

In the following numerical experiments, we investigate the feasibility of polarization switching using several pump-probe configurations. We will consider two 200-fs optical pulses that copropagate through the SOA for two different situations. In the first case, the pump pulse is either TE or TM polarized. In the second case the pump pulse is linearly polarized under an angle of $45^\circ$ with the TE and TM polarization axes. While the pulse travels through the SOA, not only the TE and TM field component intensities will be amplified (or attenuated), but also their phase difference will change. Hence, the state of polarization changes dynamically during the propagation of the pulse through the SOA. These processes are fully described in (2) and (3). The pump pulses have variable pulse energy. The probe pulse is linearly polarized (TE or TM) or under an angle of $45^\circ$ with respect to the TE and TM polarization axes. The total probe
pulse energy is fixed to 0.8 fJ. This small energy guarantees that the probe pulse propagate linearly through the SOA. The delay between the pump and probe pulses is optimized to be around 5 fs such that the latter propagates in the gain minimum introduced by the pump pulse.

Fig. 2 shows the gain variations in the middle of the SOA (z = 250 μm) for the different polarization modes. It can be observed that initially the SOA gains $g^{TE/TM}$ are 0.24 and 0.34 μm$^{-1}$ for the TE and TM modes respectively. As an example, in Fig. 2(a), the TE gain is presented for different pump polarizations, where the pump pulse energy is 1.7 pJ. In Fig. 2(b), a similar result is presented for the TM gain. The results show that the largest decrease in the TE gain takes place if the pump pulse is also purely TE polarized and the smallest variation in the TE gain takes place if the pump pulse is purely TM polarized. It can be noted from Fig. 2 that there is a clear gain compression induced by the strong pump pulses. After its compression, an initial gain recovery at a 0.5-ps timescale appears, then followed by a slow recovery time, which is associated with the interband effects determined by the electron and hole recombination times (1.3 ns in our cases, not shown in Fig. 2).

If the probe pulse is linearly polarized under an angle of 45° with respect to the TE and TM polarization axes, we can compare simultaneously the phase change for both of its TE and TM polarization components. The pump-induced phase shifts between the TE and TM components of the probe pulse as a
Fig. 3. Net phase shift difference $\Delta \phi$ between TE and TM modes ($\Delta \phi = \phi_{\text{TE}} - \phi_{\text{TM}}$) as function of the energy of a TE polarized pump pulse.

Fig. 4 is a schematic of the experimental setup. An optical parametric oscillator (OPO) pumped with a mode-locked Ti:Sapphire laser is used to produce optical pulses that were 140 fs (at FWHM) in duration and at a repetition rate of 80 MHz. The central wavelength of the pulses was 1550 nm. The OPO output power is divided by a half mirror into two parts. The first half of the optical power is collimated into a single-mode optical fiber after passing through a polarization controller and an attenuator. A variable attenuator is employed to precisely control the pulse power. A Mach–Zehnder interferometer with unequal arms is utilized as fiber delay system to create the probe and reference pulse. The reference pulse is advancing the probe pulse by 100.4 ps. The second half of the OPO output forms the pump pulse. The pump pulse is subsequently sent through a polarization controller, an attenuator, and a variable delay line, and finally also fed into a single-mode optical fiber. The pump pulse and the probe and reference pulses are cross-linearly polarized to distinguish the pump light from the probe and reference pulse. The pulses are then combined by using an optical coupler and fed into the SOA by using a set of graded-index lenses. In the fiber system, the pulses are broadened to 300 fs due to dispersion. The total coupling losses are estimated to be 10 dB. Measured at the coupler, the optical power of the pump signal was 705 $\mu$W while the optical power of the combined probe and reference pulses was 61 $\mu$W. The SOA output is fed into an inline polarizer after passing through an isolator, an optical bandpass filter (5 nm) and a polarization controller. The inline polarizer is used to separate the pump light from the probe and reference pulse. After passing through the inline polarizer, the power ratio between the pump pulse, and the probe and reference pulse was 1 : 14. Finally, the optical spectrum of the probe and reference pulses are analyzed by using an optical spectrum analyzer with a resolution of 0.01 nm. The relative phase is stable over several minutes without using active control, since the interferometer
is made of fiber couplers and shielded in a box from thermal and mechanical disturbances.

In the first experiment, the SOA is pumped with 120 mA of current. Fig. 5 shows three traces of measured optical spectra of the probe and reference pulse in the presence and absence of pump light. The upper trace in series “A” is the optical spectrum of the probe and reference pulses in absence of pump light. The lower trace in series “A” is the measured optical spectrum if the pump pulse arrives after the probe and reference pulse. Consequently, the pump light does not affect the probe and reference pulses and, thus, no phase changes are visible. The two traces in series “B” are the optical spectra in the case that the pump pulse arrives at the SOA simultaneously with the probe pulse. The upper trace in series “B” is the spectrum of the probe and reference pulses in absence of pump light. Firstly, a decrease of the modulation depth of the spectrum is visible. This is due to the reduced amplification of the probe pulse in the presence of the pump light [62]. It is estimated that the probe pulse has received 2.7 dB less amplification compared to the reference pulse. Secondly, a phase shift of approximately 200° is visible. This is due to the refractive index change introduced by the pump pulse. The two traces in series “C” represent the case that the pump pulse arrives 1.3 ps before the probe pulse at the SOA. Again, the upper trace in series “C” is the spectrum of the probe and reference pulses in absence of pump light. From the reduced modulation depth, it can be concluded that the probe pulse has received less gain, but no phase difference is visible. Fig. 6 shows the phase change as a function of the pump-probe delay. It follows from Fig. 6 that the phase change recovers within a picosecond. In contrast to results for an InGaAsP-InP bulk SOA that are published in [63], we do not observe phase recovery effects on a timescale of a few picoseconds that can be associated with carrier heating. This might be related to the fact that we use an MQW SOA that has a smaller linewidth enhancement factor compared to a bulk SOA, in combination with our experimental approach; we measure the pump induced nonlinear phase with respect to a reference pulse that might create a long-lived tail by itself. In the second experiment, the SOA current was increased to 160 mA while all the other conditions were kept the same. The dashed line in Fig. 6 shows a vanishing phase change as a function of the pump-probe delay for 160 mA. However, the reduced modulation depth of the optical spectrum reveals a maximum difference in amplification between the reference pulse and the probe pulse of 3.2 dB.

Our results concerning the ultrafast phase change in the SOA can be explained by using the formula [55]

$$\frac{\partial \phi}{\partial z} = \frac{1}{2} \alpha g - \frac{1}{2} \alpha \alpha_2 S$$  \hspace{1cm} (18)

where $\alpha$ is the linewidth enhancement factor, $g$ is the SOA gain, $\beta$ the TPA parameter, $\alpha_2$ the linewidth enhancement factor due to TPA, and $S$ the photon number, i.e., proportional to the optical pulse energy. The first term on the right-hand side of (18) describes the phase change due to the SOA gain that depends on the injection current. The second term on the right-hand side describes the phase change due to TPA. In the presence of a pump pulse, the first term will always lead to a negative phase shift contribution with respect to the situation without pump
Fig. 5. Optical spectra of a probe and reference pulse in the case that the pump pulse: (A) arrives after the probe and reference pulse; (B) arrives almost simultaneously with the probe pulse; and (C) arrives 1.3 ps before the probe pulse. The injection current is 120 mA. The upper trace in (A), (B), and (C) represents the interference spectrum in absence of pump light. The 50-GHz modulation that is visible in the spectra is an instrumental artifact related to “aliasing.”

Fig. 6. Phase change as a function of the pump-probe delay for injection currents of 120 mA (solid line) and 160 mA (dashed line). The error margin is $10^\circ$.

pulse. This contribution increases in magnitude with increasing bias current. The second term is only nonzero in the presence of a pump pulse. Clearly, the observed compensating effect for higher current can only be explained when $\alpha_2 < 0$.

V. ULTRAFAST ALL-OPTICAL SWITCH

The results shown in Section IV show that ultrashort optical pulses can introduce nonlinear phase changes larger than 180° in a SOA. In this section, we investigate an optical switch based on ultrafast SOA index nonlinearities.

A schematic of our all-optical logic AND gate is shown in Fig. 7. An OPO pumped with a mode-locked Ti:Sapphire laser is used to produce optical pulses that were 200 fs (FWHM) in duration at a repetition rate of 75 MHz. The central wavelength of the pulses was 1520 nm. The OPO output is firstly attenuated using a half-wave plate and a polarizer. A second half-wave plate is used to set the polarization of the laser beam to linear under 45°. A polarizing beam splitter is used to create a TE polarized laser beam and a TM polarized laser beam. The TM polarized laser beam forms the pump light and is fed into a variable delay line. A beam splitter divides the TE polarized laser beam into a probe beam and a reference beam. The pump and probe beams are coupled into the SOA through microscope objectives. The coupling losses are estimated to be 6 dB. The pump-probe delay is controlled by the variable delay stage. The SOA used in our experiments is an InGaAsP-InGaAs MQW SOA with a central length of 750 μm and a taper zone with a length of 400 μm on each sides of the central part. Neutral density filters are used to control the power of the probe and reference beams. A translatable end mirror controls the delay between the reference beam and the probe beam. When the pump and probe beams have passed through the SOA, the pump light is removed by using another polarizing beam splitter. The probe and reference beams first interfere in the beam splitter. The interfered light is then collimated into an optical fiber that is connected to a detector. The whole setup is placed in a polystyrene
housing box to shield the interferometer from thermal and mechanical disturbances. This makes it so that the relative phase is stable over several minutes without any active control. An automated measurement system is employed to obtain stable measurements without any active control.

In our first experiment, the interferometer output power is measured for zero pump-probe delay. The power of the probe beam was equal to the power of the reference beam, but the pump power was ten times larger. We have observed that our SOA converts about 1% of the TM polarized pump light into TE polarized light, which also interferes with the probe and reference beams. First, we measured the maximum interferometer output (i.e., with zero time delay between probe and reference pulse) as a function of the injection current. The interferometer output power can be related to the nonlinear phase shift through the following relationship:

\[
S_{\text{det}}(\tau) = \frac{1}{T} \int_{-T/2}^{T/2} \left[ P_p(t + \tau) + P_{\text{pr}}(t) + P_r(t) \right. \\
+ 2\sqrt{P_p(t)P_{\text{pr}}(t)} \cos[\phi_{\text{pr}} - aI] \\
+ 2\sqrt{P_p(t + \tau)P_{\text{pr}}(t)} \cos[\phi_{\text{pr}} - \Delta\phi_{\text{NL}}(\tau)] \\
+ 2\sqrt{P_p(t)P_{\text{pr}}(t)} \cos[aI + \Delta\phi_{\text{NL}}(\tau)] \left. \right] dt \tag{19}
\]

where \(S_{\text{det}}(\tau)\) is the detector signal, \(\tau\) the pump-probe delay, \(P_p(t + \tau)\) the power of the polarization converted pump pulse, \(P_{\text{pr}}(t)\) the power of the probe pulse and \(P_r(t)\) the power of the reference pulse. The pump-induced nonlinear phase shift \(\Delta\phi_{\text{NL}}(\tau)\) is the phase difference of the probe pulse between the cases in presence and absence of a pump pulse. \(\phi_{\text{pr}}\) is the phase shift introduced by the optical path length difference between the reference pulse and the polarization converted pump pulse. Similarly, \(\phi_{\text{pr},\text{p}}\) represents the phase shift introduced by the path length difference between the polarization converted pump pulse and the probe. Finally, we have observed that the phase shift induced by the SOA injection current \(I\) equals to \(aI\), where \(a = \pi/100\) rad/mA. The detector response time \(T\) in (19) is much larger than the pulse duration. Fig. 8 shows the measured \(\Delta\phi_{\text{NL}}(\tau)\) as a function of the injection current. It follows that for small injection currents, large positive phase shifts can be obtained. These results are in qualitative agreement with the results published in [64], where it is shown that the phase shift due to TPA opposes the phase shift introduced by the gain.

The nonlinear phase shift per SOA unit length can be expressed as

\[
2(\partial\Delta\phi_{\text{NL}}(\tau)/\partial\sigma) = a[g_p(\tau) - g_0] - a\beta_2 S(\tau) \tag{64}
\]

Here, \(a\) is the linewidth enhancement factor, \(\beta_2\) the TPA coefficient, \(a\beta_2\) the linewidth enhancement factor associated with TPA, \(S(\tau)\) the photon number of the injected light, \(g_p(\tau)\) the gain in presence of a pump pulse, and \(g_0\) the gain in absence of the pump light. The gain difference in the first contribution describes the well-known gain depletion and ultrafast recovery due to carrier cooling versus pump-probe delay time [37]. This term has an overall proportionality to the injection current \(I\). For sufficiently small currents, the first contribution is positive due to dominating absorption. For a certain current, which depends on the pump pulse energy, this term turns negative due to depletions. The second term is proportional to, and has the same shape as, the pump pulse. It was already concluded in the previous section that \(\alpha\beta_2\) has a negative sign. Therefore, the contribution of the second term to the phase shift is always positive. Hence, at zero current we predict the highest phase shifts, while for higher currents the phase shift decreases due to the smaller contribution of the first term.

If an ultrashort optical pump pulse is fed into an SOA that is operated at zero injection current, it will generate carriers, not only directly by absorption but also by TPA. These latter carriers are hot, but will cool down on a subpicosecond timescale and will already lead to an extra increase of the gain within the
carrier–carrier scattering time (50–100 fs), all of which leads to a positive phase shift. On the other hand, if the injection current is increased to a value above transparency, a reservoir of carriers is available in the conduction and valence bands. As soon as the optical pump pulse passes by, these carriers recombine due to stimulated emission followed by a recovery of the carrier number due to TPA and cooling. In this case, the negative gain induced contribution to the phase shift counters the positive instantaneous TPA induced contribution. For a specific injection current, the value of which depends on the pump pulse energy, the net phase shift vanishes. For this injection current, the phase shift due to the stimulated emission is precisely compensated by the phase shift due to TPA [64]. If the injection current is increased further, the net phase shift is dominated by the stimulated emission and saturates for high injection currents.

We have also measured the contrast ratio of the optical gate using pump pulses of 800-fJ energy. The result is shown in Fig. 9, where also the output power of the gate is plotted in the presence and absence of pump light. According to Fig. 9, the best result with 800-fJ pump pulses is expected for $I = 0$. Therefore, the setup was calibrated at $I = 0$ to achieve a minimum output without pump light. We measure for $I = 0$ a contrast ratio of $-11$ dB. This value is limited by the residual noise in the output without pump pulse, as well as by the polarization converted pump pulse residue as discussed below (19). It can be derived from (19) that given the observed noise level, if the pump pulse residue could be suppressed, the ideal contrast ratio can be as small as $-26$ dB, increasing slowly with $I$. This is indicated by the curve labeled “ideal” in Fig. 9. The ideal curve is computed by putting $P_p(I)$ to zero in (19), while keeping all the other values the same. In this latter curve, it is assumed that for each value of $I$, the system is calibrated to the minimum noise floor level in the output without pump pulse (which has not been done in the experiment). The contrast ratio can be further improved by optimizing the delay between the pump and probe pulses, the probe and reference pulse, as well as by lowering the noise floor in the output without pump pulse. In addition, we observed from the optical spectra that the output pulse did not significantly broaden after passing through the gate.

### VI. Discussion

We have presented in this paper an optical logic AND gate which operated by ultrafast carrier dynamics in an SOA. Operation has been demonstrated by using ultrashort pulses at a low repetition rate. We have also presented a rate-equation model that describes carrier dynamics in the SOA at subpicosecond timescales.

The largest technological challenge on the road toward the implementation of ultrafast optical logic based on SOA nonlinearities operated at ultrahigh repetition rates is undoubtedly related to the power consumption of these devices. Fig. 1 shows that an optical pulse with energy of 200 fJ can suppress the SOA amplification with approximately 15 dB. This implies that at a bit rate of 1 Tb/sec an average power of at least 100 mW is required to introduce nonlinearities that are strong enough to allow bit-wise optical switching (here it is assumed that half of the transmitted data are zeros). If switching principles based on nonlinear refractive index dynamics are employed, Fig. 9 shows that pulse energies in the order of 3 pJ are required to introduce a phase shift of $\pi$ radians. As shown in Section V, switching can be realized using pulses with much lower energy, at the expense of a high extinction ratio. In Section V, we obtained an extinction ratio of 11 dB using control pulses with an energy of 800 fJ in an asymmetric Mach–Zehnder interferometer. Commercially available SOAs can handle average input powers with a maximum of 50 mW, which implies that the SOA nonlinearities are too weak to allow bitwise optical switching at ultrahigh repetition rates. We wish to remark that the coupling losses presented in this paper have been estimated conservatively, thus we expect that in reality the switching powers will be lower.

In [57], results are published showing that in a 250-μm-long InGaAsp-InP bulk SOA, negative gain values are reached for pulses with energy of 100 fJ [57]. Pump and probe studies on the same device reveal that pulse energies between 460 fJ and a few picojoules (depending on whether the SOA is in the gain or absorption regime) are required to obtain phase shifts larger than 2 rad [63]. In our device, optical pulses with energy of 800 fJ can introduce a nonlinear phase shift of 2.3 rad.

The observed switching energies in SOAs is relatively low compared to the switching energies in passive intersubband waveguides in which switching energies in the order of 10 pJ per pulse are required to create an extinction ratio of 10 dB [65]. Also, the powers required to obtain switching in an SOA seem to be an order lower compared to electroabsorption modulators [2], [66]. Note that Fig. 9 shows that the largest nonlinear phase shifts in our SOA are obtained at zero injection current. This result also suggests that it is beneficial to carry out optical time domain multiplexing (OTDM) demultiplexing at ultrahigh bit rate by using passive devices.

A second challenge is to employ ultrafast SOA nonlinearities in more sophisticated ultrafast all-optical logic circuits. The main hurdle to be taken here is also related to the power consumption of the circuit. More complex optical logic functionalities such as optical flip–flop memories or optical pseudorandom number generators are often realized by coupling two all-optical logic gates so that the output signal of the first logic gate acts as a control signal for the second logic gate [23], [27].
optical logic gates are usually implemented by employing SOA refractive index nonlinearities in an interferometric environment (usually SOAs in a Sagnac interferometer or a Mach–Zehnder interferometer). It follows from Fig. 1 that if pulses with pulse energies greater than 2 pJ are injected in our SOA, the output pulse energies are smaller than the input pulse energies. Fig. 9 reveals that pulse with energies of 2 pJ can introduce a nonlinear phase shift of approximately 2.7 rad. If nonlinear phase shifts greater than 2.7 rad are required, the output pulse energy of the first gate will be insufficient to control the second gate. Sophisticated integrated optical circuits consist of active elements coupled to each other through passive elements such as splitters and filters which introduce additional losses [67]. It is, therefore, essential to design all-optical logic circuits that can be controlled with pulses with energies far below the critical 2 pJ limit.

It might be possible to design optical logic gates that can be controlled with pulses of much lower energies. Interesting and promising examples include differentially operated Mach–Zehnder interferometers or nonlinear polarization switches [46], [68]. It is also believed that lower power operation can be obtained by employing quantum dot SOA. Recently the first prototype quantum dot SOAs operating at telecommunication wavelengths have been realized [69]. It should be realized however that the nonlinear carrier dynamics of quantum dot SOAs differs fundamentally from the results presented in this paper [70], and it is not yet clear how quantum dot devices can be employed in optical logic.

REFERENCES


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