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Anharmonic Magnetic Deformation of Self-Assembled Molecular Nanocapsules

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High magnetic fields were used to deform spherical nanocapsules, self-assembled from bolaamphiphilic sexithiophene molecules. At low fields the deformation—measured through linear birefringence—scales quadratically with the capsule radius and with the magnetic field strength. These data confirm a long standing theoretical prediction [W. Helfrich, *Phys. Lett. A* **43**, 409 (1973)], and permit the determination of the bending rigidity of the capsules as $(2.6 \pm 0.8) \times 10^{-21}$ J. At high fields, an enhanced rigidity is found which cannot be explained within the Helfrich model. We propose a complete form of the free energy functional that accounts for this behavior, and allows discussion of the formation and stability of nanocapsules in solution.

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The spontaneous formation of hollow molecular spheres (vesicles) is a prototype of self-assembly of organic molecules into well-defined architectures. Vesicular self-assembly is a quite general phenomenon [1] observed in lipid molecules (the building blocks of cell membranes [2]), polymers, dendrimers, and π -conjugated oligomers [3]. This large variety makes vesicles interesting for applications like tailor-made nanocapsules for drug delivery [1], optoelectronics [4], and containers for chemical reactions [5]. They also provide ideal systems to develop physical models for self-assembly. Such a model requires a quantitative understanding of the weak noncovalent interactions involved in the self-assembly process on the basis of which vesicle formation and stability can be explained. To this end, we have measured magnetic deformation of novel bolaamphiphilic [6] sexithiophene-based capsules [7,8] and we have developed a theory to describe this effect. Comparison between theory and experiments allows the determination of important quantities like the bending rigidity of the capsules and contributes to an understanding of their stability.

The determination of the elasticity of vesicles through magnetic deformation was proposed three decades ago by Helfrich [9,10], but it was never demonstrated experimentally. A magnetic field is a thermodynamic parameter that exerts well-defined magnetic forces to deform all capsules in solution, in a controlled and contact-free way. Furthermore, the field-induced deformation can be quantified via a linear birefringence measurement. The results are, therefore, easier to compare with theory than those of other deformation methods, such as using capillary forces [11–13], pressure [14,15], electric fields [16,17], mechanical forces by an atomic force microscope tip [18], or optical tweezers [19].

Theoretically we use a fourth order Landau-Ginzburg expression of the capsule free energy that describes quan-

titatively the measured elastic deformation up to high magnetic fields, far beyond the quadratic dependence predicted by Helfrich at low fields [10]. From the data we obtain the free energy as a function of temperature that explains the overall stability of nanocapsules and predicts their dissolution at high temperature. The quantitative determination of the free energy can be used to develop and validate models for the noncovalent interactions responsible for the self-assembly process.

Experimentally we investigate sexithiophene (6T) [2,5''''-(R-2-methyl-3,6,9,12,15-pentaoxahexadecyl ester), Fig. 1(a)] which is a π -conjugated oligomer with a rigid apolar sexithiophene block substituted at both ends by polar ethylene oxide chains. 6T forms hollow spherical self-assemblies in a 2-propanol solution [Fig. 1(b), details can be found in [8]]. Dynamic light scattering reveals a narrow distribution of capsule sizes, with an average radius $R(T)$ ($\pm 10\%$) that increases with temperature T from 56 nm at 20 °C to 126 nm at 60 °C (Table I). At 70 °C the spherical shape is lost, while at 80 °C the scattering intensity is zero because the 6T molecules are molecularly dissolved [8].

6T molecules have a strongly anisotropic diamagnetic susceptibility χ , which means that the sexithiophene core tends to orient along the field [20]. Consequently, capsules are deformed from a sphere to an oblate ellipsoid, where more molecules are parallel (top and bottom of the capsule) than perpendicular to the field [around the equator, Fig. 1(c)], reducing the magnetic energy at the expense of elastic energy. This magnetic deformation is probed by measuring the field-induced optical birefringence Δn in a resistive 20 T magnet using a laser (HeNe, 632.85 nm) modulation technique.

Figure 1(d) shows Δn of a 1 g/l 6T/2-propanol solution at different T . These curves were recorded during slow sweeps of the magnetic field B at constant T (± 0.1 °C) and

FIG. 1 (color online). (a) Chemical structure of a sexithiophene molecule (6T). Schematic representation of a spherical capsule with radius R (b) and magnetically deformed capsule with semiaxes a and c (c). (d) Temperature dependence of the magnetic field (B) induced birefringence of a 1 g/l 6T solution in 2-propanol. Inset: normalized birefringence Eq. (3) divided by R^2 and plotted versus B^2 . The dashed line corresponds to a fit with constant bending rigidity k .

are fully reproducible for up, down, and consecutive sweeps. In our setup a negative Δn corresponds to 6T molecules aligning with their long axis parallel to the magnetic field direction, as expected for an oblate ellipsoid [Fig. 1(c)]. The absolute value of Δn increases with T up to 60 °C. At 70 °C it is considerably reduced with a different field dependence, and Δn is zero at 80 °C, when the capsules are dissolved. At low fields Δn scales with the square of the capsule radius and increases as B^2 with approximately the same slope at all temperatures [inset of Fig. 1(d)]. These experimental facts prove that Δn originates from a reversible effect on stable nanocapsules below their melting temperature (20–60 °C).

For small deformations (low fields) the normalized birefringence $\Delta n/\Delta n_{\max}$ ($\Delta n_{\max} = -6.5 \times 10^{-5}$ [21]) varies linearly with deformation [9,10,22], but a more accurate relation is needed for high deformations (high fields). For small capsule concentrations ρ_c the refractive index n is related to the polarizability of individual capsules α by $n^2 = n_0^2 + 4\pi\rho_c\alpha$, where n_0 is the refractive index of the solvent. The dipole moment of the 6T molecules $\mathbf{p}$ is connected with the effective electric field $\mathbf{E}'$ in the molecular layer by $\mathbf{p} = \alpha_{\perp}[\mathbf{E}' - \mathbf{e}(\mathbf{e}\mathbf{E}')] + \alpha_{\parallel}\mathbf{e}(\mathbf{e}\mathbf{E}')$,

TABLE I. Structural properties of 6T nanocapsules in 2-propanol at different temperatures. Capsule radius R , as determined by dynamic light scattering (exp.) and obtained by fitting the magnetic birefringence (fit). Equilibrium parameters a , c , and l of the deformed capsules at 20 T.

Temperature T (°C)	Radius R (nm) Exp.	Superspheroid (20 T) Fit	a/R	c/R	l
20	56	58	1.19	0.59	0.90
30	68	62	1.20	0.56	0.89
40	75	75	1.23	0.50	0.88
50	88	99	1.26	0.42	0.85
60	126	110	1.28	0.39	0.84

where $\alpha_{\perp}$ and $\alpha_{\parallel}$ are the polarizabilities of 6T molecules with respect to $\mathbf{e}$, the unit vector normal to the capsule at a given point of its surface. Applying standard boundary conditions on the Maxwell equations we find the birefringence of a uniaxially deformed capsule:

$$\Delta n = \pi\rho_c\rho_m\left(\alpha_{\parallel}\frac{\epsilon_0}{\epsilon_n} - \alpha_{\perp}\right)\int dS(1 - 3e_z^2), \quad (1)$$

where ϵ_0 and ϵ_n are the dielectric constants of the solvent and of the 6T in the direction along $\mathbf{e}$, respectively, ρ_m is the surface density of molecules in the layer, the integration is over the surface S of the capsule, and z labels the direction of magnetic field $\mathbf{B}$.

To calculate Δn we assume that the shape of the deformed capsules can be described by superspheroids, parametrized by

$$\begin{aligned} x(u, v) &= a\sin^l u \cos u, & y(u, v) &= a\sin^l u \sin u, \\ z(u, v) &= c\cos^l v, & (a > c), \end{aligned} \quad (2)$$

FIG. 2 (color online). Normalized birefringence of magnetically deformed 6T capsules. Solid lines: experimental data for different temperatures. Dashed lines: calculated birefringence in the Helfrich model, fitting the low-field behavior using a constant k for all T . Inset: calculated relation between birefringence and deformation for superspheroids (solid lines) and spheroids (dashed lines) compared to $\Delta n/\Delta n_{\max} \approx (a - c)/R$ (dash-dotted line).

with a is the radius in the circular xy plane and c the extension in the z direction [Fig. 1(c)]. Superspheroids are more general than the spheroids ($l = 1$) that are commonly used for small deformations [9,10], and allow the capsules to flatten ($l < 1$). The birefringence now reads:

$$\frac{\Delta n}{\Delta n_{\max}} = -\frac{1}{2\pi a^2} \int dS(1 - 3e_z^2). \quad (3)$$

The inset of Fig. 2 shows $\Delta n/\Delta n_{\max}$ as function of deformation $(a - c)/R$ for (super)spheroids. We keep the surface area of the capsule constant, assuming a constant number of 6T molecules that form a permeable membrane. Remarkably, both curves are rather similar, in particular, in the low deformation limit, where we recover the linear relationship between Δn and deformation by expanding Eq. (3) as [9,10,22]

$$\frac{\Delta n}{\Delta n_{\max}} \simeq \frac{a - c}{R}, \quad (4)$$

which holds as long as $(a - c)/R \leq 0.3$ (inset of Fig. 2).

We determine the equilibrium values of a , c , and l at each B by minimizing the total free energy $\mathcal{F}_{\text{tot}}$, which is the sum of the elastic $\mathcal{F}_{\text{el}}$ and magnetic $\mathcal{F}_{\text{mag}}$ free energy. Simultaneously, the parameters in $\mathcal{F}_{\text{el}}$ are determined by a fit to the experimental Δn using relation (3). We first consider the well-known form of the elastic term proposed by Helfrich [10], leading to

$$\begin{aligned} \mathcal{F}_{\text{tot}} &= \mathcal{F}_{\text{el}} + \mathcal{F}_{\text{mag}} + \mathcal{F}_{\text{surf}} \\ &= \frac{k}{2} \int dS H^2 - \frac{\Delta\chi D B^2}{2\mu_0} \int dS \left(e_z^2 - \frac{1}{3} \right) \\ &\quad + \gamma \left(\int dS - 4\pi R^2 \right)^2, \end{aligned} \quad (5)$$

where $H = (\kappa_1 + \kappa_2)/2$ is the mean curvature, κ_1, κ_2 are the principal curvatures, $D = 6.4$ nm (length of long axis of 6T) is the membrane thickness, and $\Delta\chi = \chi_{\perp} - \chi_{\parallel}$, the difference in magnetic susceptibility along the short and long axes of 6T, respectively, [23]. The term $\mathcal{F}_{\text{surf}}$ imposes, for large γ [24], the constraint of constant capsule surface. The bending rigidity k is the only fit parameter to obtain the best description of the experimental birefringence (Fig. 2). This approach can be used because the capsule size is large compared to the intermolecular distances, which means that the capsule shape is characterized by its curvatures.

Considering first the limit of small deformations we can expand Eq. (5) as

$$\frac{a - c}{R} = B^2 \frac{R^2 D \Delta\chi}{3k\mu_0}. \quad (6)$$

Combination of Eqs. (4) and (6) shows that the low-field birefringence is inversely proportional to the bending rigidity k , and scales quadratically with magnetic field and capsule radius (the Helfrich result). Our experimental results (Fig. 2, inset of Fig. 1) indeed exhibit this scaling up to $B \sim 1$ T, allowing one to determine k as $(2.6 \pm 0.8) \times$

10^{-21} J, independent of temperature. Our data, therefore, permit the experimental determination of the bending rigidity of this type of capsules.

The Helfrich free energy thus quantitatively describes the birefringence data in the low deformation regime using a constant bending rigidity. However, this model clearly overestimates the experimental birefringence at high fields (Fig. 2), which indicates an increased bending rigidity at higher deformations. Therefore we extend the expression of the free energy by including all symmetry allowed terms up to fourth order [25]:

$$\mathcal{F}_{\text{el}} = \int dS [A'K + AH^2 + c_1H^4 + c_2H^2K + c_3K^2], \quad (7)$$

where $K = \kappa_1\kappa_2$ is the Gaussian curvature. Note that terms in HK and H^3 are not allowed for symmetric bolaamphiphiles [25]. Since at $B = 0$ the capsules are spherical, with $H^2 - K = 0$, it is convenient to rewrite $\mathcal{F}_{\text{el}}$ as

$$\begin{aligned} \mathcal{F}_{\text{el}} &= \int dS [(A + A')K + A(H^2 - K) + (c_1 + c_2 + c_3)H^4 \\ &\quad - (c_2 + 2c_3)H^2(H^2 - K) + c_3(H^2 - K)^2]. \end{aligned} \quad (8)$$

If we compare the elastic energies Eq. (8) for a flat layer and for a set of spheres with radius R with the same total area, and neglecting the edge energy due to the interaction of the solvent with the hydrophobic cores, we find that $A + A' < 0$ and $c_1 + c_2 + c_3 > 0$ must hold to favor the formation of spheres. In this case, the minimum of Eq. (8) occurs for a sphere of radius

$$R^2 = \frac{1}{H^2} = -2 \frac{c_1 + c_2 + c_3}{A + A'}. \quad (9)$$

Since the term $\int dSA'K$ does not depend on deformation, the magnetic deformation data cannot provide directly information about A' . In fact, according to the Gauss-Bonnet theorem, $\int dSK = 4\pi$ for any surface topologically equivalent to the sphere (like the superspheroid considered here). However, Eq. (9) can be used *a posteriori* to determine A' , once the other parameters are found by a best fit to the experiments. This approach is very powerful, because it experimentally determines the total free energy of nanocapsules, which is very difficult to obtain otherwise, and which can be used to discuss the overall stability of capsules.

Within this description the low-field bending constant k can be calculated analytically for spheroids by expanding Eq. (7) for small deformations:

$$k = 2A + \frac{28c_1 + 22c_2 + 16c_3}{3R^2}, \quad (10)$$

which connects our approach to that of Helfrich. Moreover, since k has to be positive to guarantee stability against deformations, this equation poses an extra constraint on the choice of parameters. In the spirit of Landau theory, we assume that only A depends on T and that the coefficients

FIG. 3 (color online). (a) Fit (dashed lines) of the experimental birefringence (solid lines) at different temperatures, using superspheroidal capsules with deformation energy $\mathcal{F}_{el}$ given by Eq. (8). (b) Equilibrium shapes of the deformed capsules at 20 T.

c_i are temperature independent. In fact, by using the experimental value of k we eliminate the parameter A from the fitting procedure, by which c_i and $R(T)$ are determined via fitting to the experiments at the different temperatures [Fig. 3(a)].

For all temperatures the overall behavior of Δn is nicely reproduced, including the weaker field dependence at higher fields, indicating anharmonic deformation characterized by a field enhanced bending rigidity. The fitted value of $R(T)$ (Table I) is well within the error margins of the experimental dynamic light scattering values. Table I also shows the parameters a , c , and l at 20 T, which correspond to substantially deformed capsules, as illustrated in Fig. 3(b). At the highest fields deformations $(a - c)/R$ as large as 0.9 are found, which agrees very well with the observed deformation of 6T capsules that are fixed in a compatible organogel and imaged by scanning electron microscopy [8]. Not surprisingly, we find that with increasing deformation the capsule shape becomes flatter (decreasing l , see Table I), maximizing the number of molecules aligned along the field.

The best fits in Fig. 3(a) are obtained using $c_1 = 1.148$, $c_2 = -1.336$, $c_3 = 0.358$ (10^{-35} J m^2), and the T -dependent A and $A + A'$ are shown in the inset. Indeed, these values make the capsules stable at $B = 0$ ($A + A' < 0$, $c_1 + c_2 + c_3 > 0$) for $T < 60^\circ \text{C}$. However, $A + A'$ approaches 0 when $T \rightarrow 60^\circ \text{C}$, suggesting an instability of the capsules at higher T , which is indeed compatible with the experiments that show that the capsules melt above 60°C . It is this vicinity of the system to an instability which makes fourth order terms comparable in magnitude to second order ones and make the Helfrich model inadequate for this situation.

The parameters c_1 , c_2 , c_3 , $A(T)$, and $A'(T)$ fully describe the free energy of the nanocapsules. Their actual values are intricately related to the intermolecular interactions within

the capsule-solvent system, such as π - π interactions between neighboring 6T cores and interactions between 6T tails and solvent molecules [25,26]. Determination of these parameters for a physical nanostructure therefore provides a stringent test case, on the basis of which microscopic intermolecular interaction models can be developed. Such a quantitative description of noncovalent interactions within molecular assemblies is an important step toward the detailed understanding of the rules of self-assembly.

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