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by

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Specification of tools for Message Sequence Charts

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Abstract. The recent formalization of the semantics of Message Sequence
Charts enables the derivation of tools for MSCs directly from this formal def­
inition. We use the ASF+SDF Meta-environment to make a straightforward
implementation of tools for transformation, simulation and requirements test­
ing. In this paper we present the complete specification of the tools.

1 Introduction

Message Sequence Charts (MSCs) are a graphical method for the description of the interac­
tion between system components [IT94]. Due to the recent formalization [MR94a, MR94b,
IT95] of the semantics of Message Sequence Charts, we can consider MSC as a formal de­
scription technique.

Currently, this formalization has already influenced the development of the language (in
particular with respect to composition of MSCs, for which algebraic operators are considered)
and it is expected to also influence the use of MSCs.

Formalization will also have impact on the work of tool builders. The behavior of tools
can be validated against the formal semantics, but even more valuable is the possibility
to generate tools, or prototypes, directly from the formal definitions. This paper is to
be considered a case study in the formal development of computer tools for programming
languages.

In practice, tools for an informally defined language are developed mainly based on
the intuition of the program designer. Unless all people have a common understanding
of the language, this leads to inconsistent tools. If a formal definition of the language is
available, tools can also be based on the understanding of these formal semantics. This
may lead to more consistent tools, but in practice this only works if the semantics is well
accessible. A better approach would be to automatically implement the formal semantics
of the language. This leads to correct and consistent tools. A possible problem with this
approach is that necessarily a formal semantics has a high level of abstraction and is not
directed towards possible tools. Thus, automatic implementation of the formal semantics is
not always feasible. An operational semantics and decisions on implementation details may
be needed.

Our aim is to demonstrate how the abstract definitions of the formal semantics of Basic
Message Sequence Charts (BMSCs) can be implemented. BMSCs are Message Sequence
Charts with only the main features: communication and local actions. The techniques
described in this paper transfer straightforward to the complete MSC language. As described
in [MR94a] the semantics of BMSCs is defined by a translation into process algebra. This
translation is defined by means of equations and the axioms defining process algebra are

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also equations. Therefore, the obvious way of implementing the semantics of MSCs is by using algebraic specifications [EM85].

We used the ASF+SDF Meta-environment [Kli93] for the implementation. With this system algebraic specifications can be implemented by means of term rewriting systems. Furthermore, a complete programming environment for BMSCs can be generated, including a syntax directed editor, a parser and a pretty printer.

The implementation consists of three parts. The first part consists of an implementation of the static requirements for BMSCs expressed informally in [IT94] and formalized in [Ren94]. The second part is the translation of BMSCs into process algebra expressions. This is based on the definition of the semantic functions in [MR94a]. The third part is the definition of a simulator for BMSCs. Although a simulator is not part of the formal semantics, it can easily be derived from the operational semantics given in [MR94a]. In fact the description of the simulator can be regarded as a formal specification of a simulation tool.

Figure 1 describes the structure of the generated tool set. Boxes denote expressions in the given language and arrows represent transformations from one language to the other. Apart from the INPUT language which is plain ASCII, we consider the following languages. MESSAGES is the language of output messages generated by the requirements checker and the simulator, BMSC is the language of (parsed) Basic Message Sequence Charts, \( PA_{BMSC} \) is the process algebra theory used for describing the semantics of BMSCs (see [MR94a]) and BPA is the sub-language of \( PA_{BMSC} \) that only contains the normalized \( PA_{BMSC} \) expressions. The generated tools are considered as transformation tools, described by algebraic specifications. We specified the following tools.

**Syntax directed editor and parser** The parser converts plain ASCII text into BMSC.

**Checker** The additional syntax requirements (static semantics) for BMSCs can be checked with this tool.

**Semantics Calculator** The semantics of a BMSC is described by a translation into the process algebra \( PA_{BMSC} \). The Semantics Calculator (or semantics function) computes the semantics of a BMSC.

**Normalizer** The normalizer reduces the expression resulting from the previous step to normal form. This tool makes it possible to inspect the complete behavior of the given BMSC.
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Simulator Test runs of the BMSC can be generated interactively with the simulator. It offers the user a choice between all possible continuations. After selecting one event, it calculates the \( \text{PABMSC} \) expression that results after execution of the event.

This paper is structured in the following way. Section 2 contains a description of the ASF+SDF Meta-environment. In Section 3 we give a short overview of the BMSC language. Section 4 contains the specification of the static requirements. In Section 5 we define the process algebra and its specification in ASF+SDF. The Semantics Calculator and Normalizer are defined in Section 6 and the simulator in Section 7.

Although this paper covers the complete semantics of BMSCs, it is not intended as a self-contained explanation of these semantics. Refer to [MR94a] for a comprehensive treatment.

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2 The ASF+SDF Meta-environment

The ASF+SDF Meta-environment [Kli93] is a programming environment generator based on algebraic specifications. From a specification of the syntax and semantics of a language an environment is generated, in its simplest form consisting of a syntax directed editor and a term rewrite system. The generated environment can be customized further by means of the language SEAL [Ko092, Ko094].

2.1 Algebraic Specifications

An algebraic specification consists of a signature, a set of variables and a set of equations. The signature describes a number of sorts and functions over these sorts. Using these functions and the variables one can construct terms. The equations define equalities between these terms.

Consider, e.g., an algebraic specification of the data-structure Booleans. The signature defines one sort BOOL, two constants of sort BOOL, namely true \( \rightarrow \) BOOL and false \( \rightarrow \) BOOL, one unary function not: BOOL \( \rightarrow \) BOOL, and two binary functions and: BOOL \# BOOL \( \rightarrow \) BOOL and or: BOOL \# BOOL \( \rightarrow \) BOOL. Let's assume that a variable Bool over sort BOOL is declared. From the signature and the variables terms like true, false, Bool, not(true), not(Bool), and(true,false), and(Bool,true), etc. can be derived. The semantics of the functions "not", "and" and "or" are defined by equations. We have, for instance, \( \text{not(true)} = \text{false} \). A complete specification of this data-structure in ASF+SDF notation will be given in section 2.2.

The most common strategy for implementing algebraic specifications is via term rewrite systems (TRSs). An algebraic specification can be transformed into a TRS by interpreting the equations as rewrite rules from left to right. An algebraic specification of the Booleans can thus be used to compute the value of a function by rewriting a term to its normal form, true or false.

The transformation into a TRS sometimes implies that decisions on implementation details are made, which were not expressed in the algebraic specification. For example, if we aim at complete TRSs (i.e. TRSs which are confluent and terminating, see [Kli92]), we need to decide on the implementation of commutative operators and the implementation of
sets by ordered lists. Therefore, a completely automatic implementation of an algebraically specified semantics by means of a TRS is not always feasible.

2.2 The formalism ASF+SDF

When specifying programming languages in an algebraic manner the syntax for function definitions is found to be too restrictive. The formalism ASF+SDF therefore combines the algebraic specification formalism ASF with a formalism for defining syntax: SDF. SDF allows for the combined specification of concrete syntax (like in BNF) and abstract syntax. Hence, ASF+SDF is a formalism for writing algebraic specifications with user defined syntax.

An ASF+SDF specification consists of a sequence of modules. Each module may contain

**Imports** of other modules.

**Sort declarations** defining the sorts of a signature.

**Lexical syntax** defining layout conventions and lexical tokens.

**Context-free syntax** defining the concrete syntactic forms of the functions in the signature.

**Variables** to be used in equations. In general, each variable declaration has the form of a regular expression and defines the class of all variables whose name is described by the regular expression.

**Equations** Conditional equations define the meaning of the functions defined in the context-free syntax.

Sort declarations, lexical functions, context-free syntax and variables are either part of an **export section** in a module or can be declared as **hidden**. When a module imports another module the export sections in the syntax definition as well as the equations of the imported module are visible in the importing module. Hidden sorts, functions or variables cannot be referred to by the importing module.

**Example** A simple example specification is given below consisting of the modules Layout and Booleans. Module Booleans defines the Boolean values and operators. In order to avoid ambiguities in parsing terms attributes \{left\} or \{right\} can be added to function declarations, defining a function to be left associative or right associative. For instance, the attribute \{left\} in BOOL \& BOOL \rightarrow BOOL indicates that the term true \& false \& true should be parsed as (true \& false) \& true rather than true \& (false \& true). Moreover, the specifier can indicate by means of priorities rules how terms should be parsed. For instance, the priority rule in module Booleans states that the operator \texttt{not} binds stronger than the operator \texttt{\&} which in turn binds stronger than the operator \texttt{\textasciitilde}. Hence, the term \texttt{not true \& false} will be parsed as (not true) \& false rather than not (true \& false). Likewise, the term true \& false \texttt{\textasciitilde} true should be parsed as (true \& false) \texttt{\textasciitilde} true. The function with the attribute \{bracket\} is added only for grouping and disambiguation, it is not included in the abstract syntax.

The variable declaration \texttt{Bool[1-9]* \rightarrow BOOL} declares an infinite number of variables of sort BOOL. All variables start with the letters \texttt{Bool} followed by zero or more (*) occurrences of numbers and quotes \texttt{[1-9\']}. In the equations we use only one variable.

Module Booleans imports module Layout which consists of two lexical functions for the predefined sort LAYOUT. The upper one defining that spaces (\texttt{\textasciitilde}), tabs (\texttt{\textasciitilde\textasciitilde}) and
newlines (\n) are layout, and thus separate tokens. The lower function defines a comment
convention by stating that any string starting with two percentage signs ("%%") followed
by any number of characters other than a newline (\n), and concluded by a newline (\n)
is to be considered layout as well.

2.2.1 Booleans

imports Layout^{2.2.2}
exports
  sorts BOOL
  context-free syntax
    true ➔ BOOL
    false ➔ BOOL
    BOOL "\p" BOOL ➔ BOOL \{left\}
    BOOL "\&" BOOL ➔ BOOL \{left\}
    "not" BOOL ➔ BOOL
    "(" BOOL ")" ➔ BOOL \{bracket\}

hiddens
  variables
    Bool [1-9]^* ➔ BOOL

priorities
  BOOL "\p" BOOL ➔ BOOL < BOOL "\&" BOOL ➔ BOOL <
  "not" BOOL ➔ BOOL

equations

[1] true | Bool = true
[2] false | Bool = Bool
[3] true & Bool = Bool
[4] false & Bool = false
[5] not true = false
[6] not false = true

2.2.2 Layout

exports
  lexical syntax
    \[\{\{\{\{\\}\}\}\}\]} ➔ LAYOUT
    "%%"\~\{\{\{\{\\}|\{\{\{\{\\}\}\}\}\}\}\}\]} ➔ LAYOUT

Other features Other features of ASF+SDF will be explained when necessary. In partic­
ular, the use of default equations and the description of list sorts is explained in section 4.1. More advanced priority rules are referred to in section 5.2.

3 Message Sequence Charts

Message Sequence Charts provide a graphical method for the description of the communica­
tion behavior of system components. The ITU-TS (the Telecommunication Standardization
Section of the International Telecommunication Union, the former CCITT) maintains rec­
ommendation Z.120 [IT94] which contains the syntax and an informal explanation of the
semantics of Message Sequence Charts. A formal semantics based on process algebra has been proposed in [MR94b]. This proposal has been accepted for standardization by the ITU [IT95].

3.1 Basic Message Sequence Charts

In this paper we restrict ourselves to the core language of Message Sequence Charts, which we call Basic Message Sequence Charts (BMSCs). A Basic Message Sequence Chart concentrates on communications and local actions only. These are the features encountered in most languages comparable to Message Sequence Charts. Their semantics is described in [MR94a].

A Basic Message Sequence Chart contains a (partial) description of the communication behavior of a number of instances. An instance is an abstract entity of which one can observe (part of) the interaction with other instances or with the environment. The Basic Message Sequence Chart in Figure 2 defines the communication behavior between instances a and b. This will be the running example in the remainder of this paper. An instance is denoted by a vertical axis. The time along each axis runs from top to bottom.

A communication between two instances is represented by an arrow which starts at the sending instance and ends at the receiving instance. In Figure 2 we consider message m from instance a to instance b and message k which is sent from a to the environment. The behavior of the environment is not specified. For instance b we also define a local action p.

![Figure 2: Example Basic Message Sequence Chart](image)

Although the activities along one single instance axis are completely ordered, we will not assume a notion of global time. The only dependencies between the timing of the instances come from the restriction that a message must have been sent before it is received. In Figure 2 this implies for example that message m is received by b only after it has been sent by a. Furthermore, it is required that action p is executed before message m is received, and that message m is sent before message k. For the sending of k and the reception of m no ordering is specified.

3.2 BMSC syntax

The grammar defining the syntax of textual Basic Message Sequence Charts as presented in [MR94a] is given in Table 1. The nonterminals <mscid>, <iid>, <mid> and <aid> represent identifiers. The symbol <> denotes the empty string. The following identifiers are reserved
keywords: action, endinstance, endmsc, env, from, in, instance, msc, out and to. The language generated by a non-terminal $<x>$ is denoted by $\mathcal{L}(<x>)$.

Table 1: The BNF grammar of Basic Message Sequence Charts

| $<\text{msc}>$ | ::= | msc $<\text{mscid}>$; |
| $<\text{msc body}>$ | ::= | $<>$ | $|$ |
| $<\text{instancedef}>$ | ::= | instance $<\text{iid}>$; |
| $<\text{instancebody}>$ | ::= | $<>$ | $|$ |
| $<\text{event}>$ | ::= | in $<\text{mid}>$ from $<\text{iid}>$; | $|$ |
| | | in $<\text{mid}>$ from env; | $|$ |
| | | out $<\text{mid}>$ to $<\text{iid}>$; | $|$ |
| | | out $<\text{mid}>$ to env; | $|$ |
| | | action $<\text{aid}>$; |

The Basic Message Sequence Chart of Figure 2 has the following textual representation.

```plaintext
msc example1;
  instance a;
  out m to b;
  out k to env;
  endinstance;
  instance b;
  action p;
  in m from a;
  endinstance;
endmsc;
```

The context free syntax for BMSCs is expressed in ASF+SDF in the following specification. It is easily derived from the BNF grammar.

The first module below defines the Identifiers, which consist of a character followed by characters and digits. It states that there is an (invisible) mapping from elements of the sort ID to the sorts MSCID, IID, MID and AID. The second module defines the syntax of BMSCs.

3.2.1 Identifiers

```plaintext
imports Layout2-2-2
exports sorts ID MSCID IID MID AID
lexical syntax
  \([a-z][a-z0-9]* \rightarrow \text{ID}\)
context-free syntax
  ID \rightarrow MSCID
  ID \rightarrow IID
  ID \rightarrow MID
  ID \rightarrow AID
```
3.2.2 BMSC-Syntax

import Identifiers

exports

sorts
MSC MSC-BODY INST-DEF INST-BODY EVENT

context-free syntax

 massacre MSCID \"\" MSC-BODY endmsc \"\" → MSC

INST-DEF \"\" MSC-BODY → MSC-BODY

instance IID \"\" INST-BODY endinstance → INST-DEF

EVENT \"\" INST-BODY → INST-BODY

in MID from IID → EVENT

in MID from env → EVENT

out MID to IID → EVENT

out MID to env → EVENT

action AID → EVENT

3.3 Example

A syntax directed editor for BMSC is generated by the ASF+SDF Meta-environment. From the definition of the (context-free) syntax of BMSC, a scanner and a parser for BMSC is created. If the text in the editor is conform the BMSC syntax the parser generates the corresponding BMSC term. Figure 3 shows a snapshot of the syntax directed editor, containing the running example of figure 2. Note, that buttons are connected to the editor for the four other tools. These buttons are created by means of the user interface language SEAL [Koo92, Koo94]. When a button is selected the corresponding tool is applied to the BMSC in the editor.

4 Requirements

Two static requirements for Basic Message Sequence Charts are formulated in [MR94a]. The first is that an instance may be declared only once. The second is that every message identifier occurs exactly once in an output action and once in a matching input action, or in case of a communication with the environment a message identifier occurs only once. In addition we will check whether all instances that are referred to in messages have been declared. Module Requirements imports two auxiliary modules: Xevents and Messages.
4.1 Xevents

The specification of the requirements is facilitated when an MSC is represented by a list of its events. We therefore introduce the sort XEVENT. This is an event extended with the name of the instance it belongs to. E.g., when instance \texttt{a} sends a message \texttt{m} to instance \texttt{b}, \texttt{out m to b}, the corresponding extended event is \texttt{out m from a to b}.

The declaration \texttt{[\{XEVENT \n;\}* \} \to XEVENTLIST} declares a list of zero or more (*\ XEVENTs separated by semicolons (\n;\n) and surrounded by square brackets ([\ [ \]).\ The variables declaration \texttt{<"xevent">"\n*[0-9]* \to XEVENT \n;\ )*} declares variables over such lists of XEVENTs. Any list of XEVENTs matches variables like \texttt{<xevent>*}, \texttt{<xevent>*1}, \texttt{<xevent>*13} etc.. Equation 6 defines the union of two lists of XEVENTs as a list containing the events of the first list followed by those of the second list.

The functions \texttt{xevent}, \texttt{xevent\_body}, \texttt{xevent\_list} and \texttt{extend} are introduced to derive a list of extended events from an MSC. Equations 1 through 11 specify the behavior of these functions.

The function \texttt{message\_name} returns an MIDLIST, a list containing the message identifier of an XEVENT. Equations 12 through 15 specify the application of this function to all xevents describing input or output actions. Equation 16 is a so called default equation, marked with the keyword otherwise. Such an equation is only used for rewriting a given term if no other equation applies. Hence, equation 16 states that the \texttt{message\_name} of any xevent not describing an input or output action equals the empty list [\].

Equations 17 and 18 specify that two xevents match, if one of them represents the sending of a message to an instance and the other one is the xevent for the reception of that message. The default equation 19 states that applying the predicate \texttt{matching\_xevents} to any other pair of xevents equals false.

4.1.1 Xevents

imports BMSC-Syntax3.2.2 Booleans5.2.1
exports
sorts XEVENTLIST XEVENT MIDLIST
context-free syntax
\texttt{"[" \{(XEVENT \n;\]*) \n;\]* \} \to XEVENTLIST}
\texttt{xevents(MSC)} \to XEVENTLIST
\texttt{xevents \n;\ n body \"(" MSC-BODY \n;\")\"} \to XEVENTLIST
\texttt{xevents \n;\ n inst \"(" IID \n;\ INST-BODY \n;\")\"} \to XEVENTLIST
\texttt{XEVENTLIST \n;\ n \"U\" XEVENTLIST} \to XEVENTLIST \{left\}
\texttt{in MID from IID to IID} \to XEVENT
\texttt{in MID from env to IID} \to XEVENT
\texttt{out MID from IID to IID} \to XEVENT
\texttt{out MID from IID to env} \to XEVENT
\texttt{action AID by IID} \to XEVENT
\texttt{extend(IID, EVENT)} \to XEVENT
\texttt{message\_name(XEVENT)} \to MIDLIST
\texttt{"[" \{(MID \n;\]*) \n;\]*) \to MIDLIST}
\texttt{matching\_xevents(XEVENT, XEVENT)} \to BOOL

hiddens
variables
\texttt{"<" \"msg\_body"\">"} \to MSC-BODY
\texttt{"<" \"inst\_def"\">"\n*[0-9]* \to \{INST\_DEF \n;\]*)\*}
equations

[1] \text{xevents}(\text{msc} <\text{mscid}>; <\text{msc-body}> \text{ endmsc}) = \text{xevents}_{\text{body}} (<\text{msc-body}>)

[2] \text{xevents}_{\text{body}} () = \emptyset

[3] \text{xevents}_{\text{body}} (\text{instance} <\text{iid}>; <\text{inst-body}> \text{ endinstance}; <\text{msc-body}>) =
\text{xevents}_{\text{inst}} (<\text{iid}>, <\text{inst-body}>) \cup \text{xevents}_{\text{body}} (<\text{msc-body}>)

[4] \text{xevents}_{\text{inst}} (<\text{iid}>,) = \emptyset

[5] \text{xevents}_{\text{inst}} (<\text{iid}>, <\text{event}>; <\text{inst-body}>) =
[\text{extend}(<\text{iid}>, <\text{event}>)] \cup \text{xevents}_{\text{inst}} (<\text{iid}>, <\text{inst-body}>)

[6] [<xevent_1>] \cup [<xevent_2>] = [<xevent_1>; <xevent_2>]

[7] \text{extend}(<\text{iid}_1>, \text{in} <\text{mid}> \text{ from} <\text{iid}_2>) = \text{in} <\text{mid}> \text{ from} <\text{iid}_2> \text{ to} <\text{iid}_1>

[8] \text{extend}(<\text{iid}_1>, \text{in} <\text{mid}> \text{ from env}) = \text{in} <\text{mid}> \text{ from env to} <\text{iid}_1>

[9] \text{extend}(<\text{iid}_1>, \text{out} <\text{mid}> \text{ to} <\text{iid}_2>) = \text{out} <\text{mid}> \text{ from} <\text{iid}_1> \text{ to} <\text{iid}_2>

[10] \text{extend}(<\text{iid}_1>, \text{out} <\text{mid}> \text{ to env}) = \text{out} <\text{mid}> \text{ from} <\text{iid}_1> \text{ to env}

[11] \text{extend}(<\text{iid}_1>, \text{action} <\text{aid}>) = \text{action} <\text{aid}> \text{ by} <\text{iid}_1>

[12] \text{message-name}(\text{in} <\text{mid}> \text{ from} <\text{iid}_1> \text{ to} <\text{iid}_2>) = [<\text{mid}>]

[13] \text{message-name}(\text{in} <\text{mid}> \text{ from env to} <\text{iid}_2>) = [<\text{mid}>]

[14] \text{message-name}(\text{out} <\text{mid}> \text{ from} <\text{iid}_1> \text{ to} <\text{iid}_2>) = [<\text{mid}>]

[15] \text{message-name}(\text{out} <\text{mid}> \text{ from} <\text{iid}_1> \text{ to env}) = [<\text{mid}>]

[16] \text{message-name}(<\text{xevent}>) = [] \text{ otherwise}

\text{matching-xevents}(\text{out} <\text{mid}> \text{ from} <\text{iid}_1> \text{ to} <\text{iid}_2>) = \text{true}

\text{matching-xevents}(\text{in} <\text{mid}> \text{ from} <\text{iid}_1> \text{ to} <\text{aid}_2>) = \text{true}

\text{matching-xevents}(\text{in} <\text{mid}> \text{ from} <\text{iid}_1> \text{ to} <\text{iid}_2>) = \text{false} \text{ otherwise}
4.2 Messages
Module Messages defines the general syntax of the error messages used in module Requirements. Note, that these are not messages in the sense of MSC, but messages to inform the user of the system. Four kinds of messages are distinguished in the lexical syntax. (1) Opening brackets « followed by a string without the symbol > and concluded by », (2) Opening brackets « followed by a string without quotes or >, and concluded by quotes. (3) Quotes followed by a string without > and concluded by ». (4) Quotes followed by a string without quotes or > and concluded by quotes.

This syntax allows for composed messages of sort MESSAGELIST like [« in instance "a" an error has been found »].

The operator $\cup$ specifies the union of lists of messages.

4.2.1 Messages
imports Layout\textsuperscript{2.2.2}
exports
sorts MESSAGE MESSAGELIST
lexical syntax
$\langle \rangle $ $\rightarrow$ MESSAGE
$\langle \rangle $ $\rightarrow$ MESSAGE
$\langle \rangle $ $\rightarrow$ MESSAGE
$\langle \rangle $ $\rightarrow$ MESSAGE
context-free syntax
$\langle \rangle $ MESSAGE $\rightarrow$ MESSAGELIST
MESSAGELIST $\cup$ MESSAGELIST $\rightarrow$ MESSAGELIST \text{(left)}
hiddens
variables
$\psi$ $\rightarrow$ MESSAGE$	extsuperscript{+}$
equations

\[1\] $[m_1] \cup [m_2] = [m_1 \cap m_2]$

4.3 Requirements specification
The main function in module Requirements is the function check for MSCs. The result of checking an MSC is CHECKINFO, composed of a boolean value and a possible empty list of error messages. Two CHECKINFOs can be added by means of the function CHECKINFO and CHECKINFO. Equation 1 specifies how this is done. The sort MESSAGE is extended so that identifiers and xevents can be referred to in error messages.

As mentioned before, three requirements will be checked. Equation 2 states that the function check invokes the functions unique-instance-names, inst-declared and check-message-names. Equations 3 to 5 specify the semantics of the functions unique-instances and $\text{uinbody}$. According to equation 4 an empty MSC-BODY is correct, i.e. all instance names are unique. If the MSC-BODY consists of an instance definition followed by an MSC-BODY, we check that the name of the first instance does not occur in the set of declared instance names of the remaining MSC-BODY. By a recursive call of the function $\text{uinbody}$ the rest of the BMSC is checked (equation 5). The error messages are generated by the auxiliary function notin. Equation 6 states that if a given instance name occurs at any position in a list of instance names, the Boolean value false and an error message are returned. Otherwise, the Boolean
value true and an empty list of error messages are returned (equation 7). Equations 8, 9 and 10 inductively define the auxiliary function declared-instnames, which computes the set of instance names in an MSC-BODY.

The function inst-declared checks whether instances referred to by input and output actions have been declared (equation 11). The auxiliary functions refinsts select the names of all instances referred to by input or output actions of an MSC (equations 12 unto 17). The function included-in checks if all IIDs in a list do occur in another list of IIDs. If not, an error-message is generated (equations 18 – 20).

Application of the function check-message-names to an MSC invokes the application of the functions unique-message-names and check-nonmatching-messages to the corresponding list of xevents. Equation 23 specifies that unique-message-names selects all pairs of xevents that mistakenly have the same message name. If such a pair is present, an error message is generated and the function is recursively applied to the rest of the list. Lists without such pairs are correct according to equation 24.

Equation 25 specifies that check-nonmatching-messages removes all matching pairs of input output actions from a list of xevents. If no such pairs are left in the list the function aux-nonmatching-messages is invoked (equation 26). Applying aux-nonmatching-messages to an empty list yields the boolean value true and an empty list of error messages. If the first xevent in the list represents receiving a message from an instance or sending a message to an instance, no matching action will be present in the rest of the list. Therefore, an error message is generated and the rest of the list is checked. If the first xevent is any other action, it is correct and the rest of the list is checked (equations 27 – 30).

4.3.1 Requirements

imports Xevents\^{4.1.1}\hspace{1em} Messages\^{4.2.1}
exports
sorts CHECKINFO IIDLIST
context-free syntax
  check(MSC) → CHECKINFO
  "Check: BOOL "Errors:” MESSAGE LIST → CHECKINFO
  CHECKINFO and CHECKINFO → CHECKINFO \{left\}
  MESSAGE IID MESSAGE → MESSAGE
  MESSAGE MID MESSAGE → MESSAGE
  MESSAGE XEVENT MESSAGE → MESSAGE
  unique-instance-names "(” MSC "")" → CHECKINFO
  un in "-" body "(” MSC-BODY "")" → CHECKINFO
  IID not in IIDLIST → CHECKINFO
  declared-instnames "(” MSC "")" → IIDLIST
  declared-instnames "(" MSC "")" → IIDLIST
  inst-declared(MSC) → CHECKINFO
  refinsts(MSC) → IIDLIST
  refinsts(XEVENTLIST) → IIDLIST
  refinsts(XEVENT) → IIDLIST
  IIDLIST includedin IIDLIST → CHECKINFO
  "[ [IID "";] * [""
  IIDLIST ""] IIDLIST → IIDLIST \{left\}
  check-message-names(MSC) → CHECKINFO
  unique-message-names(XEVENTLIST) → CHECKINFO
check-nonmatching-messages(XEVENTLIST) -> CHECKINFO
aux-nonmatching-messages(XEVENTLIST) -> CHECKINFO

hiddens variables
b[0-9]* -> BOOL
m[0-9]* -> MESSAGELIST
"<" msc">" -> MSC
"<" msc-body">" -> MSC-BODY
"<" inst-def">" -> INST-DEF
"<" inst-body">" -> INST-BODY
"<" event">" "[0-9]* -> {EVENT "", "}*
"<" event">" -> EVENT
xel -> XEVENTLIST
"<" xevent">" "[0-9]* -> {XEVENT "", "}*
"<" xevent">" -> EVENT
mscid -> MSCID
"<" uid">" "[0-9]* -> {IID ", "}*
i -> IID
"<" iid">" "[0-9]* -> IID
"<" mid">" -> MID
"<" aid">" -> AID

equations

[1] Check: b1 Errors: ml1 and Check: b2 Errors: ml2 = Check: b1 & b2 Errors: ml1 ∪ ml2

[2] check(<msc>) = unique-instance-names(<msc>)
and inst-declared(<msc>)
and check-message-names(<msc>)

[3] unique-instance-names(msc <mscid>; <msc-body> endmsc;) = uin_body (msc-body)

[5] uin_body (instance <uid>; <inst-body> endinstance; <msc-body>) =
<uid> notin declared-instnames(<msc-body>) and uin_body (msc-body)

[6] <uid> notin [<uid>; <uid>; <uid>;] =
Check: false Errors: [<"<"duplicateuinstanceuname" <uid> "u">]

[7] <uid> notin [<uid>"] = Check: true Errors: [] otherwise
[8] declared-instnames() = []

[9] declared-instnames(instance <uid>; <inst-body> endinstance; <msc-body>) =
[<uid>] ∪ declared-instnames(<msc-body>)

[10] declared-instnames(msc <mscid>; <msc-body> endmsc;) =
declared-instnames(<msc-body>)}
\[\text{inst-declared}(\text{<msc>}) = \]
\[\text{refinsts}(\text{<msc>}) \text{ includedin} \text{ declared-instnames}(\text{<msc>})\]

\[\text{refinsts}(\text{<msc>}) = \text{refinsts}(\text{xevents}(\text{<msc>}))\]

\[\text{refinsts}([]) = []\]

\[\text{refinsts}(\text{[<xevent>; <xevent>']}) = \]
\[\text{refinsts}(\text{xevents}(\text{<xevent>})) \cup \text{refinsts}(\text{[<xevent>']})\]

\[\text{refinsts}(\text{in <mid> from <iid> to <iid>2}) = [\text{<iid>1}]\]

\[\text{refinsts}(\text{out <mid> from <iid> to <iid>2}) = [\text{<iid>2}]\]

\[\text{refinsts}(\text{<xevent>}) = []\]

\[\text{[] includedin} [\text{<iid>}] = \text{Check: true Errors: []}\]

\[\text{[<iid>1]; <iid>2; <iid>3] includedin} [\text{<iid>1}; <iid>2; <iid>3] = \]
\[\text{[<iid>1]; <iid>2] includedin} [\text{<iid>1}; <iid>2; <iid>3]\]

\[\text{[<iid>1; <iid>2]} includedin} [\text{<iid>2}] = \]
\[\text{Check: false Errors: ["instance not declared"] otherwise}\]

\[\text{and} [\text{<iid>1}; <iid>2] includedin} [\text{<iid>2}]\]

\[\text{[<iid>1}; <iid>2] \cup [\text{<iid>1}; <iid>2] = [\text{<iid>1}; <iid>2]\]

\[\text{check-message-names}(\text{<msc>}) = \text{unique-message-names}(\text{<xel>})\]

\[\text{and} \text{check-nonmatching-messages}(\text{<xel>})\]

\[\text{when}\]
\[\text{<xel> = xevents}(\text{<msc>})\]

\[\text{unique-message-names}(\text{[<xevent>1}; <xevent>2; <xevent>3; <xevent>4]) = \]
\[\text{Check: false Errors: ["duplicate message name" <mid> "but not declared"] otherwise}\]

\[\text{and} \text{unique-message-names}(\text{[<xevent>1}; <xevent>2; <xevent>3; <xevent>4])\]

\[\text{when}\]
\[\text{[<mid>] = message-name}<xevent>2, <xevent>4, <xevent>4), <xevent>4\]
\[\text{false = matching-xevents}(<xevent>2, <xevent>4)\]

\[\text{unique-message-names}(\text{[<xevent>']}) = \text{Check: true Errors: [] otherwise}\]

\[\text{check-nonmatching-messages}(\text{[<xevent>1}; <xevent>2; <xevent>3; <xevent>4}) = \]
\[\text{check-nonmatching-messages}(\text{[<xevent>1}; <xevent>2; <xevent>3; <xevent>4})\]

\[\text{when}\]
\[\text{matching-xevents}(<xevent>2, <xevent>4) = \text{true}\]
check-nonmatching-messages([<xevent>]*)) =
aux-nonmatching-messages([<xevent>]*)) otherwise

aux-nonmatching-messages([]) = Check: true Errors: []

aux-nonmatching-messages([in <mid> from <iid>1 to <iid>2; <xevent>]) =
Check: false
Errors: [<<no_matching_event_for in <mid> from <iid>1 to <iid>2 " Event >>] and check-nonmatching-messages([<xevent>*])

aux-nonmatching-messages([out <mid> from <iid>1 to <iid>2; <xevent>]) =
Check: false
Errors: [<<no_matching_event_for out <mid> from <iid>1 to <iid>2 " Event >>] and check-nonmatching-messages([<xevent>*])

aux-nonmatching-messages([<xevent>; <xevent>]) =
Check: true Errors: [] otherwise
and check-nonmatching-messages([<xevent>*])

4.4 Example

When the Check button in Figure 3 is selected the relevant functions are applied to the term in the editor and the generated term rewrite system is used to compute the result. A window will pop up containing this result. Figure 4 shows the result of checking the BMSC in our running example. Since this term is correct the list of error messages is empty. Next, suppose that we change the message name k in out k to env of Figure 3 into m. Selecting the check button then results in the window of Figure 5.
5 Process algebra

This section contains the definition of the process algebra \( PABMSC \). First we define the atomic actions. After that we give the definition of the process algebra \( PA_c \) and extend it with the state operator.

5.1 Atomic actions

The process algebra \( PABMSC \) is an algebraic theory for the description of process behavior based on ACP [BW90, BK84]. First we will define the set of atomic actions of \( PABMSC \).

Every (extended) event occurring in a BMSC will be translated into an atomic action from \( PABMSC \). Thus we have the atomic actions as displayed in Table 2.

Table 2: The atomic actions of \( PABMSC \)

| \( A_1 \) | \( \{\text{in}(s,r,m) \mid s, r \in IID, m \in MID\} \) |
| \( A_o \) | \( \{\text{out}(s,r,m) \mid s, r \in IID, m \in MID\} \) |
| \( A_e \) | \( \{\text{out}(s,\text{env},m) \mid s \in IID, m \in MID\} \) |
| \( A_a \) | \( \{\text{action}(i,\text{aid}) \mid i \in IID, \text{aid} \in AID\} \) |
| \( A \) | \( A_1 \cup A_o \cup A_e \cup A_a \) |

The description in ASF+SDF of the atomic actions is given in module Atoms. Instead of defining the sets from Table 2, we define four predicates. The equations defining these predicates are straightforward.

5.1.1 Atoms

imports PA-Kerne\[5.2.2\] Identifiers\[3.2.1\] Booleans\[2.2.1\]
exports
context-free syntax
\( \text{in}(IID, IID, MID) \rightarrow \text{ATOM} \)
\( \text{in}(\text{env}, IID, MID) \rightarrow \text{ATOM} \)
\( \text{out}(IID, IID, MID) \rightarrow \text{ATOM} \)
\( \text{out}(IID, \text{env}, MID) \rightarrow \text{ATOM} \)
\( \text{action}(IID, AID) \rightarrow \text{ATOM} \)
\( \text{is-in-atom}(\text{ATOM}) \rightarrow \text{BOOL} \)
\( \text{is-out-atom}(\text{ATOM}) \rightarrow \text{BOOL} \)
\( \text{is-env}(\text{ATOM}) \rightarrow \text{BOOL} \)
\( \text{is-action}(\text{ATOM}) \rightarrow \text{BOOL} \)

variables
\( \text{atom}[0-9]* \rightarrow \text{ATOM} \)
\( "<\text{id}>"[0-9]* \rightarrow \text{IID} \)
\( "<\text{id}>"[0-9]* \rightarrow \text{IID} \)
\( "<\text{aid}>"[0-9]* \rightarrow \text{AID} \)

equations

\[1\] is-in-atom(in(<\text{id}>1_1, <\text{id}>2_2, <\text{mid}>) \) = true
5.2 $PA_e$

The theory $PA_{BMS}$ is an extension of the theory $PA_e$. The signature, $\Sigma_{PA_e}$, of $PA_e$ consists of the following functions.

1. the special constants $\delta$ and $\epsilon$
2. the set of atomic actions $A$
3. the unary operator $\mathord{\mathcal{J}}$
4. the binary operators $+$, $\cdot$, $\|$, and $\|$

The special constant $\delta$ denotes the process that has stopped executing actions and cannot proceed. This constant is called deadlock. The special constant $\epsilon$ denotes the process that is only capable of terminating successfully. It is called the empty process.

The atomic actions from $A$ are the smallest processes in the description. The actual set $A$ is defined in Table 2.

The binary operators $+$ and $\cdot$ are called the alternative and sequential composition. The alternative composition of the processes $x$ and $y$ is the process that either executes process $x$ or $y$ but not both. The sequential composition of the processes $x$ and $y$ is the process that first executes process $x$, and upon completion thereof starts with the execution of process $y$.

The binary operator $\|$ is called the free merge. The free merge of the processes $x$ and $y$ is the process that executes the processes $x$ and $y$ in parallel. For a finite set $D = \{d_1, \ldots, d_n\}$, the notation $\|_{d \in D} P(d)$ is an abbreviation for $P(d_1) \| \cdots \| P(d_n)$. If $D = \emptyset$ then $\|_{d \in D} P(d) = \epsilon$. For the definition of the merge we use two auxiliary operators. The termination operator $\mathord{\mathcal{J}}$ applied to a process $x$ signals whether or not the process $x$ has an option to terminate immediately. The binary operator $\|$ is called the left merge. The left merge of the processes $x$ and $y$ is the process that first has to execute an atomic action from process $x$, and upon completion thereof executes the remainder of process $x$ and process $y$ in parallel.

In the priorities section of module $PA$-Syntax one finds the line \{left: PROCESS $\|$ PROCESS $\rightarrow$ PROCESS ; PROCESS $\|$ PROCESS $\rightarrow$ PROCESS \}. This means that the operators merge $\|"$ and left merge $\|"$ associate from left to right. Moreover, the operator $\cdot$ for sequential composition binds stronger than either of the merge operators, whereas the merge operators bind stronger than the operator for alternative composition.
5.2.1 PA-Syntax

imports Layout 2.2.2
exports
sorts ATOM PROCESS
context-free syntax

ATOM \rightarrow PROCESS
PROCESS "+" PROCESS \rightarrow PROCESS \{right\}
PROCESS "." PROCESS \rightarrow PROCESS \{right\}
"\delta" \rightarrow PROCESS
"\varepsilon" \rightarrow PROCESS
PROCESS "||" PROCESS \rightarrow PROCESS \{left\}
PROCESS "||" PROCESS \rightarrow PROCESS \{left\}
"\sqrt{\varepsilon} \{" PROCESS ")\} \rightarrow PROCESS
"\sqrt{\varepsilon} \{" PROCESS ")\} \rightarrow PROCESS \{bracket\}

priorities
PROCESS "." PROCESS \rightarrow PROCESS \{left:
PROCESS "||" PROCESS \rightarrow PROCESS
PROCESS "||" PROCESS \rightarrow PROCESS \}
PROCESS "+" PROCESS \rightarrow PROCESS

For \(a \in A \cup \{\delta\}\) and processes \(x, y, z\), the axioms of \(PA_e\) are given in the Table 3.

<table>
<thead>
<tr>
<th>Axiom</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>(x + y = y + x)</td>
<td>A1</td>
</tr>
<tr>
<td>((x + y) + z = x + (y + z))</td>
<td>A2</td>
</tr>
<tr>
<td>(x + x = x)</td>
<td>A3</td>
</tr>
<tr>
<td>((x + y) \cdot z = x \cdot z + y \cdot z)</td>
<td>A4</td>
</tr>
<tr>
<td>((x \cdot y) \cdot z = x \cdot (y \cdot z))</td>
<td>A5</td>
</tr>
<tr>
<td>(x + \delta = x)</td>
<td>A6</td>
</tr>
<tr>
<td>(\delta \cdot x = \delta)</td>
<td>A7</td>
</tr>
<tr>
<td>(x \cdot \varepsilon = x)</td>
<td>A8</td>
</tr>
<tr>
<td>(\varepsilon \cdot x = x)</td>
<td>A9</td>
</tr>
<tr>
<td>(x \parallel y = x \parallel y + y \parallel x + \sqrt{(x)} \cdot \sqrt{(y)})</td>
<td>TM1</td>
</tr>
<tr>
<td>(\varepsilon \parallel x = \delta)</td>
<td>TM2</td>
</tr>
<tr>
<td>(a \cdot x \parallel y = a \cdot (x \parallel y))</td>
<td>TM3</td>
</tr>
<tr>
<td>((x + y) \parallel z = x \parallel z + y \parallel z)</td>
<td>TM4</td>
</tr>
<tr>
<td>(\sqrt{(\varepsilon)} = \varepsilon)</td>
<td>TE1</td>
</tr>
<tr>
<td>(\sqrt{(a \cdot x)} = \delta)</td>
<td>TE2</td>
</tr>
<tr>
<td>(\sqrt{(x + y)} = \sqrt{(x)} + \sqrt{(y)})</td>
<td>TE3</td>
</tr>
</tbody>
</table>

Axioms A1–A9 are well known. The axioms TE1–TE3 express that a process \(x\) has an option to terminate immediately if \(\sqrt{(x)} = \varepsilon\), and that \(\sqrt{(x)} = \delta\) otherwise. In itself the termination operator is not very interesting, but in defining the free merge we need this operator to express the case in which both processes \(x\) and \(y\) are incapable of executing an atomic action. Axiom TM1 expresses that the free merge of the two processes \(x\) and \(y\) is their interleaving. This is expressed in the three summands. The first two state that \(x\) and
y may start executing. The third summand expresses that if both $x$ and $y$ have an option to terminate, their merge has this option too.

Some problems arise when interpreting the axioms of Table 3 as term rewrite rules. It is clear that axiom A1 hinders termination. If we would simply delete this axiom, we would not be able to rewrite $\delta + a$ into $a$, so we add axiom A6a from Table 4. A second problem is that axiom A8 \((x \cdot \varepsilon = x)\) is often used from right to left in calculations (e.g. \(a \| b = a \cdot \varepsilon \| b = a \cdot (\varepsilon \| b) = \ldots = a \cdot b\)). Therefore, if we give A8 an orientation from left to right, we must add the axioms TM3a and TE2a.

Finally, in order to simplify expressions we add axioms TM1a and TM1b. Note that all these axioms are provable for closed process expressions.

<table>
<thead>
<tr>
<th>Table 4: Additional axioms</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\delta + x = x$</td>
</tr>
<tr>
<td>$\varepsilon | x = x$</td>
</tr>
<tr>
<td>$x | \varepsilon = x$</td>
</tr>
<tr>
<td>$a | x = a \cdot x$</td>
</tr>
<tr>
<td>$\sqrt{a} = \delta$</td>
</tr>
</tbody>
</table>

We decided to split up the axioms of $PA_n$ over two separate $ASF+SDF$ modules. The first module $PA$-Kernel only contains rules which deal with simplification of expressions containing the special constants. The second module $PA$ contains the rules concerning the actual rewriting into normal form. The reason is that after translating a BMSC into a process algebra expression, one is not always interested in a complete reduction into normal form. The simulator, for example, does not need the normal forms.

It is well known that the complete state space of a parallel process may become very large. This is the so-called state explosion problem. The normal form of a process corresponds to its state space, so we will only calculate it when necessary.

### 5.2.2 PA-Kernel

imports $PA_{\text{Syntax}}^{5.2.1}$

hiddens

variables

$\rightarrow$ PROCESS

equations

\[\begin{align*}
[1] & \quad x + \delta = x \\
[2] & \quad \delta + x = x \\
[3] & \quad \delta \cdot x = \delta \\
[4] & \quad x \cdot \varepsilon = x \\
[5] & \quad \varepsilon \cdot x = x \\
[6] & \quad x \| \varepsilon = x \\
[7] & \quad \varepsilon \| x = x
\end{align*}\]
5.2.3 PA
imports PA-Kernel^{5.2.2}
hiddens
variables
\[
a \to \text{ATOM}
\]
\[
[xyz] \to \text{PROCESS}
equations
\[
\begin{align*}
(\res x + y) + z &= x + y + z \\
x + x &= x \\
(x + y) \cdot z &= x \cdot z + y \cdot z \\
(x \cdot y) \cdot z &= x \cdot y \cdot z \\
x \res y &= x \res y + x \res y + \sqrt{x} \cdot \sqrt{y} \\
\varepsilon \res x &= \delta \\
\varepsilon \res x &= a \cdot (x \res y) \\
a \res x &= a \cdot x \\
\delta \res x &= \delta \\
(x + y) \res z &= x \res z + y \res z \\
\sqrt{\varepsilon} &= \varepsilon \\
\sqrt{a \cdot x} &= \delta \\
\sqrt{a} &= \delta \\
\sqrt{\delta} &= \delta \\
\sqrt{x + y} &= \sqrt{x} + \sqrt{y}
\end{align*}
\]

5.3 The state operator $\lambda_M$
A Basic Message Sequence Chart specifies a (finite) number of instances that communicate by sending and receiving messages. A message is divided into two parts: a message output and a message input. The correspondence between message outputs and message inputs has to be defined uniquely by message name identification.

A message input may not be executed before the corresponding message output has been executed. We introduce an operator $\lambda_M$ that enables only those execution paths that respect the above constraint. The operator $\lambda_M$ is an instance of the state operator as can be found in [BW90]. This operator remembers all message outputs that have been executed in a set $M$ and only allows a message input if its corresponding message output is in that set.

Before specifying the signature of the state operator, we need a specification of sets of atomic actions with operators for testing, difference and union.

5.3.1 Atom-Set
imports Atoms^{5.1.1}
exports
sorts ATOM-SET
context-free syntax
\[
\begin{align*}
\{^* \{\text{ATOM} \ "\},^* \}^* \to \text{ATOM-SET} \\
\text{elem}(\text{ATOM}, \text{ATOM-SET}) \to \text{BOOL}
\end{align*}
\]
Atomic Set Specifications

\[
\text{ATOM-SET "\" \" ATOM-SET} \rightarrow \text{ATOM-SET \{left\}}
\]

\[
\text{ATOM-SET "\" \" ATOM-SET} \rightarrow \text{ATOM-SET \{left\}}
\]

\[
\text{\"\" ATOM-SET \")\"} \rightarrow \text{ATOM-SET \{bracket\}}
\]

Priorities

\[
\text{ATOM-SET \"\" ATOM-SET} \rightarrow \text{ATOM-SET \rightarrow \text{ATOM-SET \{left\}}}
\]

Hiddens

Variables

\[
M [0-9]* \rightarrow \text{ATOM-SET}
\]

\[
b"*"[0-9] \rightarrow \{\text{ATOM \"\"} \}
\]

\[
b"+"[0-9] \rightarrow \{\text{ATOM \"\"}\}+
\]

\[
[ab] \rightarrow \text{ATOM}
\]

Equations

\[
\begin{align*}
\{b_1, a, b_2, a, b_3\} &= \{b_1, a, b_2, b_3\} \\
\text{elem}(a, \{b_1, a, b_2\}) &= \text{true} \\
\text{false} &= \text{otherwise} \\
\{b_1, a, b_2\} \setminus \{b_1, a, b_3\} &= \{b_1, b_2\} \setminus \{b_3, b_2\} \\
M_1 \setminus M_2 &= M_1 \text{ otherwise} \\
\{b_1\} \cup \{b_2\} &= \{b_1, b_2\}
\end{align*}
\]

5.3.2 State-Operator-Syntax

Imports Atom-Set^{2.2.1}

Exports

Context-Free Syntax

\[
\text{"\" ATOM-SET \"\") \rightarrow \text{PROCESS}
\]

The axioms for the state operator are given in Table 5.

<table>
<thead>
<tr>
<th>Axiom</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\lambda_M(\varepsilon) = \varepsilon)</td>
<td>if (M = \emptyset)</td>
</tr>
<tr>
<td>(\lambda_M(\varepsilon) = \delta)</td>
<td>if (M \neq \emptyset)</td>
</tr>
<tr>
<td>(\lambda_M(\delta) = \delta)</td>
<td></td>
</tr>
<tr>
<td>(\lambda_M(a \cdot x) = a \cdot \lambda_M(x))</td>
<td>if (a \not\in A_o \cup A_i)</td>
</tr>
<tr>
<td>(\lambda_M(\text{out}(i, j, m) \cdot x) = \text{out}(i, j, m) \cdot \lambda_M(\text{out}(i, j, m))(x))</td>
<td>if (\text{out}(i, j, m) \in M)</td>
</tr>
<tr>
<td>(\lambda_M(\text{in}(i, j, m) \cdot x) = \text{in}(i, j, m) \cdot \lambda_M(\text{in}(i, j, m))(x))</td>
<td>if (\text{out}(i, j, m) \in M)</td>
</tr>
<tr>
<td>(\lambda_M(\text{in}(i, j, m) \cdot x) = \delta)</td>
<td>if (\text{out}(i, j, m) \not\in M)</td>
</tr>
<tr>
<td>(\lambda_M(x + y) = \lambda_M(x) + \lambda_M(y))</td>
<td></td>
</tr>
</tbody>
</table>

Table 5: Axioms for the state operator \(\lambda_M\)

Again, some additional axioms are needed in order to get a complete term rewriting system. These are displayed in Table 6.

The axioms are again partitioned in axioms for simplification (module State-Operator-Kernel) and axioms for reduction to normal form (module State-Operator). The equations can be derived easily from Tables 5 and 6.
Table 6: Auxiliary axioms for the state operator

<table>
<thead>
<tr>
<th>Equation</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\lambda_M(a) = a$</td>
<td>if $a \notin A_o \cup A_i, M = \emptyset$ (LM4a)</td>
</tr>
<tr>
<td>$\lambda_M(a) = \delta$</td>
<td>if $a \notin A_o \cup A_i, M \neq \emptyset$ (LM4b)</td>
</tr>
<tr>
<td>$\lambda_M(out(i, j, m)) = out(i, j, m) \cdot \delta$</td>
<td>(LM5a)</td>
</tr>
<tr>
<td>$\lambda_M(in(i, j, m)) = in(i, j, m)$</td>
<td>if $out(i, j, m) \in M, M \setminus {out(i, j, m)} = \emptyset$ (LM6a)</td>
</tr>
<tr>
<td>$\lambda_M(in(i, j, m)) = in(i, j, m) \cdot \delta$</td>
<td>if $out(i, j, m) \in M, M \setminus {out(i, j, m)} \neq \emptyset$ (LM6b)</td>
</tr>
<tr>
<td>$\lambda_M(in(i, j, m)) = \delta$</td>
<td>if $out(i, j, m) \notin M$ (LM7a)</td>
</tr>
</tbody>
</table>

5.3.3 State-Operator-Kernel

**imports** State-Operator-Syntax^{5.3.2}

**hiddens**

**variables**

- $M [0-9]*$ $\rightarrow$ ATOM-SET
- $a$ $\rightarrow$ ATOM
- $x$ $\rightarrow$ PROCESS
- "$<"$tid"$>$" [0-9]* $\rightarrow$ IID
- "$<"$mid"$>$" $\rightarrow$ MID

**equations**

- [1] $\lambda_M(\varepsilon) = \varepsilon$ \textit{when} $M = \{\}$
- [2] $\lambda_M(\varepsilon) = \delta$ \textit{when} $M \neq \{\}$
- [3] $\lambda_M(\delta) = \delta$

5.3.4 State-Operator

**imports** State-Operator-Kernel^{5.3.3}

**hiddens**

**variables**

- $M [0-9]*$ $\rightarrow$ ATOM-SET
- $a$ $\rightarrow$ ATOM
- $xyz$ $\rightarrow$ PROCESS
- "$<"$tid"$>$" [0-9]* $\rightarrow$ IID
- "$<"$mid"$>$" $\rightarrow$ MID

**equations**

- [1] $\lambda_M(a \cdot x) = a \cdot \lambda_M(x)$ \textit{when}
  
  $\text{is-out-atom}(a) = \text{false},$
  
  $\text{is-in-atom}(a) = \text{false}$

- [2] $\lambda_M(a) = a$ \textit{when}
  
  $M = \{\}$,
  
  $\text{is-out-atom}(a) = \text{false},$
  
  $\text{is-in-atom}(a) = \text{false}$
Specification of tools for Message Sequence Charts

\[ \lambda_M (a) = a \cdot \delta \]
when
\[ M \neq \{ \}, \]
is-out-atom(a) = false,
is-in-atom(a) = false

\[ \lambda_M (\text{out}(\langle iid_1, iid_2, mid \rangle) \cdot x) = \text{out}(\langle iid_1, iid_2, mid \rangle) \cdot \lambda_M \cup \{\text{out}(\langle iid_1, iid_2, mid \rangle)\} (x) \]

\[ \lambda_M (\text{out}(\langle iid_1, iid_2, mid \rangle)) = \text{out}(\langle iid_1, iid_2, mid \rangle) \cdot \delta \]

\[ \lambda_M (\text{in}(\langle iid_1, iid_2, mid \rangle) \cdot x) = \text{in}(\langle iid_1, iid_2, mid \rangle) \cdot \lambda_M \cup \{\text{out}(\langle iid_1, iid_2, mid \rangle)\} (x) \]
when
\[ \text{elem}(\text{out}(\langle iid_1, iid_2, mid \rangle), M) = \text{true} \]

\[ \lambda_M (\text{in}(\langle iid_1, iid_2, mid \rangle)) = \text{in}(\langle iid_1, iid_2, mid \rangle) \]
when
\[ \text{elem}(\text{out}(\langle iid_1, iid_2, mid \rangle), M) = \text{true}, \]
\[ M \setminus \{\text{out}(\langle iid_1, iid_2, mid \rangle)\} = \{\} \]

\[ \lambda_M (\text{in}(\langle iid_1, iid_2, mid \rangle)) = \text{in}(\langle iid_1, iid_2, mid \rangle) \cdot \delta \]
when
\[ \text{elem}(\text{out}(\langle iid_1, iid_2, mid \rangle), M) = \text{true}, \]
\[ M \setminus \{\text{out}(\langle iid_1, iid_2, mid \rangle)\} \neq \{\} \]

\[ \lambda_M (\text{in}(\langle iid_1, iid_2, mid \rangle) \cdot x) = \delta \]
when
\[ \text{elem}(\text{out}(\langle iid_1, iid_2, mid \rangle), M) = \text{false} \]

\[ \lambda_M (\text{in}(\langle iid_1, iid_2, mid \rangle)) = \delta \]
when
\[ \text{elem}(\text{out}(\langle iid_1, iid_2, mid \rangle), M) = \text{false} \]

\[ \lambda_M (x + y) = \lambda_M (x) + \lambda_M (y) \]

6 Translation into process algebra

In this section, we will define a semantic function \( S \) that associates to every Basic Message Sequence Chart in textual format a closed \( \mathcal{PA_{BMSC}} \) term. Before we give the definition of this semantic function we need to explain some auxiliary functions. The powerset of a set \( S \) is denoted by \( \mathcal{P}(S) \).

The function
\[ \text{Instances} : \mathcal{L}(\text{msc}) \rightarrow \mathcal{P}(\mathcal{L}(\text{inst def})) \]

that associates to a Basic Message Sequence Chart the set containing all instance definitions of the instances defined in the chart, is defined by

$$\text{Instances}(\text{msc }<\text{mscid}>; <\text{msc body}> \text{ endmsc;} ) = \text{Instancesbody}(<\text{msc body}>)$$

where the function

$$\text{Instancesbody}: \mathcal{L}(<\text{msc body}>) \rightarrow \mathcal{P}(\mathcal{L}(<\text{inst def}>))$$

is defined by

$$\text{Instancesbody}(\epsilon) = \emptyset$$
$$\text{Instancesbody}(<\text{inst def}> <\text{msc body}> ) = \{ <\text{inst def}> \} \cup \text{Instancesbody}(<\text{msc body}>)$$

Next we define the following two functions

$$\text{Name}: \mathcal{L}(<\text{inst def}> ) \rightarrow \mathcal{L}(<\text{iid}>)$$
$$\text{Body}: \mathcal{L}(<\text{inst def}> ) \rightarrow \mathcal{L}(<\text{inst body}> )$$

These functions associate to an instance definition its name and body.

$$\text{Name}(\text{instance }<\text{iid}>;<\text{inst body}> \text{ endinstance;} ) = <\text{iid}>$$
$$\text{Body}(\text{instance }<\text{iid}>;<\text{inst body}> \text{ endinstance;} ) = <\text{inst body}>$$

### 6.1 The semantic function

The general idea is that the semantics of a Basic Message Sequence Chart is the free merge of the semantics of its instances. By this construction we enable all interleavings of the message outputs and message inputs. However, a message input can only be performed after its corresponding message output. In order to rule out all interleavings where a message output is preceded by the corresponding message input we use the state operator $\lambda_M$. We define the function $S$ from the language generated by $<m>$ to the set of $\mathcal{PA}_{BMSG}$ terms, $S: \mathcal{L}(<\text{msc}> ) \rightarrow T(\Sigma_{\mathcal{PA}_{BMSG}})$, by

$$S[<\text{msc}> ] = \lambda_0 (\| i\text{ def} \in \text{Instances}(<\text{msc}> ) \ S[<\text{i def}> ] )$$

The semantic function $S_{\text{inst}} : \mathcal{L}(<\text{inst def}> ) \rightarrow T(\Sigma_{\mathcal{PA}_{BMSG}})$ is defined to express the semantics of one instance in separation. In the textual representation of an instance the atomic actions are specified in the order they are to be executed, thus the semantics of an instance definition is the sequential composition of its actions.

$$S_{\text{inst}}[<\text{i def}> ] = S_{\text{body}}^{\text{Name}(<\text{i def}> )}[\text{Body}(<\text{i def}> )]$$

where for $i \in \mathcal{L}(<\text{iid}>)$ the function

$$S_i^{\text{body}}: \mathcal{L}(<\text{inst body}> ) \rightarrow T(\Sigma_{\mathcal{PA}_{BMSG}})$$

is defined by

$$S_i^{\text{body}}[\epsilon] = \epsilon$$
$$S_i^{\text{body}}[<\text{event}> <\text{inst body}> ] = S_i^{\text{event}}[<\text{event}> ] . S_i^{\text{body}}[<\text{inst body}> ]$$
and for every \( i \in \mathcal{L}(\\langle \text{iid} \rangle) \) the function

\[
S^i_{\text{event}} : \mathcal{L}(\\langle \text{event} \rangle) \rightarrow T(\Sigma_{PA\text{BMSC}})
\]

is defined by

\[
\begin{align*}
S^i_{\text{event}}(\text{in } \langle \text{mid} \rangle \text{ from } \langle \text{iid} \rangle) & = \text{in}(\langle \text{iid} \rangle, i, \langle \text{mid} \rangle) \\
S^i_{\text{event}}(\text{in } \langle \text{mid} \rangle \text{ from env}) & = \text{in}(\text{env}, i, \langle \text{mid} \rangle) \\
S^i_{\text{event}}(\text{out } \langle \text{mid} \rangle \text{ to } \langle \text{iid} \rangle) & = \text{out}(i, \langle \text{iid} \rangle, \langle \text{mid} \rangle) \\
S^i_{\text{event}}(\text{out } \langle \text{mid} \rangle \text{ to env}) & = \text{out}(i, \text{env}, \langle \text{mid} \rangle) \\
S^i_{\text{event}}(\text{action } \langle \text{aid} \rangle) & = \text{action}(i, \langle \text{aid} \rangle)
\end{align*}
\]

The translation of the semantic function into ASF+SDF is rather straightforward. The only problem is that the generalized merge construct \( \text{def Instances}_{(\text{mid})} \) occurring in the definition of \( S[\text{msc}] \) requires higher order functions. Therefore, we combined the generalized merge and the application of the function \( S_{\text{inst}} \) into one single function \( \text{def } S_{\text{inst}} \). This function requires the collection of all instance definitions as input and calculates the parallel composition of the semantics of these instances. The set of instances is calculated by the auxiliary function \( \text{Instances} \).

Furthermore, notice that we only import the kernel of the process algebra. This means that we only have the signature and some rules for simplification, but not the defining equations.

### 6.1.1 BMSC-Semantics

**imports** State-Operator-Kernel^{3.3} BMSC-Syntax^{3.2.2}

**exports**

- **sorts** INST-DEF-LIST
- **context-free syntax**
  
  \[
  \begin{align*}
  "S" & \quad \text{"(" MSC "\)}} \quad \rightarrow \text{PROCESS} \\
  "S" & \quad \text{" inst" \quad "(" INST-DEF "\)}} \quad \rightarrow \text{PROCESS} \\
  "S" & \quad \text{" body" \quad \text{IID } "(" INST-BODY "\)}} \quad \rightarrow \text{PROCESS} \\
  "S" & \quad \text{" event" \quad \text{IID } "(" EVENT "\)}} \quad \rightarrow \text{PROCESS}
  \end{align*}
  \]

- **hiddens**

  \[
  \begin{align*}
  \text{\"(\" Instances\" & \quad \text{\"(" INST-DEF-LIST } \quad \rightarrow \text{PROCESS} \\
  \text{\"(\" } & \quad \text{\" (INST-DEF \"; \",\") \" )\" } \quad \rightarrow \text{INST-DEF-LIST} \\
  \text{\"(\" Instances\" & \quad \text{\"(" INST-DEF-LIST } \quad \rightarrow \text{INST-DEF-LIST} \{\text{left}\} \\
  \text{\"(\" Name\" & \quad \text{\"(" INST-DEF } \quad \rightarrow \text{IID} \\
  \text{\"Body\" & \quad \text{\"(" INST-DEF } \quad \rightarrow \text{INST-BODY}
  \end{align*}
  \]

**variables**

\[
\begin{align*}
"<" \text{\" inst-def\"\";\",\") \rightarrow & \text{\"(\" INST-DEF \"; \",\") } \\
i & \rightarrow \text{IID} \\
"<" \text{\" mid\"\";\",\") } & \rightarrow \text{MSC} \\
"<" \text{\" mid\"\";\",\") } & \rightarrow \text{MSC-BODY} \\
"<" \text{\" mid\"\";\",\") } & \rightarrow \text{INST-DEF} \\
"<" \text{\" mid\"\";\",\") } & \rightarrow \text{INST-BODY} \\
"<" \text{\" mid\"\";\",\") } & \rightarrow \text{EVENT} \\
"<" \text{\" mid\"\";\",\") } & \rightarrow \text{MSCID} \\
"<" \text{\" mid\"\";\",\") } & \rightarrow \text{IID} \\
"<" \text{\" mid\"\";\",\") } & \rightarrow \text{MID} \\
"<" \text{\" mid\"\";\",\") } & \rightarrow \text{AID}
\end{align*}
\]
equations

1. \[ S(<\text{msc}>) = \lambda_i \left( ||S\_{\text{inst}} \ 	ext{Instances}(<\text{msc}>) \right) \]

2. \[ ||S\_{\text{inst}} () = e \]

3. \[ ||S\_{\text{inst}} (<\text{inst-def}) = S\_{\text{inst}} (<\text{inst-def}) \]

4. \[ ||S\_{\text{inst}} (<\text{inst-def}), <\text{inst-def}^\ast> = S\_{\text{inst}} (<\text{inst-def}) \parallel ||S\_{\text{inst}} (<\text{inst-def}^\ast> \]

5. \[ S\_{\text{inst}} (<\text{inst-def}) = S\_{\text{body}}^{\text{Name}}(\text{Body}(<\text{inst-def}))) \]

6. \[ S\_{\text{body}} () = e \]

7. \[ S\_{\text{body}} (<\text{event}>; <\text{inst-body}>) = S\_{\text{event}} (<\text{event}>). S\_{\text{body}} (<\text{inst-body}>) \]

8. \[ S\_{\text{event}} (\text{in} <\text{mid}> \text{ from} <\text{iid}>) = \text{in}(<\text{iid}>, i, <\text{mid}>) \]

9. \[ S\_{\text{event}} (\text{in} <\text{mid}> \text{ from} \text{env}) = \text{in}(<\text{env}>, i, <\text{mid}>) \]

10. \[ S\_{\text{event}} (\text{out} <\text{mid}> \text{ to} <\text{iid}>) = \text{out}(i, <\text{iid}>, <\text{mid}>) \]

11. \[ S\_{\text{event}} (\text{out} <\text{mid}> \text{ to} \text{env}) = \text{out}(i, <\text{env}>, <\text{mid}>) \]

12. \[ S\_{\text{event}} (\text{action} <\text{aid}>) = \text{action}(i, <\text{aid}>) \]

13. \[ \text{Instances}(\text{msc} <\text{mscid}>, <\text{msc-body}> \text{ endmsc}; ) = \text{Instances}_{\text{body}} (<\text{msc-body}>) \]

14. \[ \text{Instances}_{\text{body}} () = () \]

15. \[ \text{Instances}_{\text{body}} (<\text{inst-def}>; <\text{msc-body}>) = ( <\text{inst-def}>) \cup \text{Instances}_{\text{body}} (<\text{msc-body}>) \]

16. \[ \text{Name}(\text{instance} <\text{iid}>; <\text{inst-body}> \text{ endinstance}) = <\text{iid}> \]

17. \[ \text{Body}(\text{instance} <\text{iid}>; <\text{inst-body}> \text{ endinstance}) = <\text{inst-body}> \]

18. \[ (<\text{inst-def}>^\ast) \cup (<\text{inst-def}>^\ast) = (<\text{inst-def}>^\ast, <\text{inst-def}>^\ast) \]
6.2 Example

The result of applying this translation to the BMSC in the editor of Figure 3 is the process algebra term $\lambda_e(out(a, b, m) \cdot out(a, env, k) \| action(b, p) \cdot in(a, b, m))$. The application of the merge operator (\(\|\)) shows that the semantics of the given BMSC is the interleaved execution of the processes $out(a, b, m) \cdot out(a, env, k)$ and $action(b, p) \cdot in(a, b, m)$. The state operator ($\lambda_e$) in front of the expression enforces that input of message $m$ only occurs after the corresponding output.

Figure 6 shows the window that appears after having selected the Semantics button.

![Figure 6: Result of computing the semantics of a BMSC](image)

6.3 Normalization

The state operator and the merge operator in the expression of Figure 6 can be eliminated. This is called normalization. The resulting term contains the operators for sequential composition (\(\cdot\)) and alternative composition (\(+\)) only. It expresses all possible behaviors of the BMSC. The normalizer is simply defined by combining the definitions of the semantic functions and the complete specification of the process algebra.

6.3.1 Normalize

```plaintext
imports BMSC-Semantics\^6.1.1 PA\^5.2.3 State-Operator\^5.3.4
```  

6.4 Example

Figure 7 shows the effect of pressing the normalize button in the editor of Figure 3. It expresses the branching structure of the process. First one can make a choice between executing $out(a, b, m)$ and $action(b, p)$. If one chooses the first option, another choice has to be made between $out(a, env, k)$ and $action(b, p)$. The rest of the process can be understood in a similar way.

![Figure 7: Result of normalizing the semantics of a BMSC](image)
7 A simulator

For large BMSCs, the expressions describing the normalized semantics as in Figure 7 become quite large and complex. This is the so-called state explosion problem. Therefore, the tools offer the possibility to walk through the events of a BMSC in any of the admitted orders. Thus, the user can interactively simulate the behavior of a BMSC. For this purpose we used the operational semantics for BMSCs from [MR94a]. This operational semantics defines for a given BMSC a labeled transition system. The transitions correspond with the events of the BMSC.

First, we will interpret the definition of the transition rules in an algebraic specification. After that, we define the additional functions needed to obtain a simulator.

7.1 Transitions

In this section we define a structural operational semantics of Basic Message Sequence Charts in the style of Plotkin [Pl83]. For this purpose we define action relations on closed PABMSC terms.

On the set of PABMSC terms we define a predicate $\downarrow \subseteq T(\Sigma_{PABMSC})$ and binary relations $\Rightarrow \subseteq T(\Sigma_{PABMSC}) \times T(\Sigma_{PABMSC})$ for every $a \in A$. These predicates are defined by means of inference rules, which have the following form.

$$\frac{p_1, \ldots, p_n}{q}$$

This expression means that for every instantiation of variables in $p_1, \ldots, p_n$, $q$ we can conclude $q$ from $p_1, \ldots, p_n$. If $q$ is a tautology, we omit $p_1, \ldots, p_n$ and the horizontal bar.

The intuitive idea of the predicate $\downarrow$ is as follows: $t \downarrow$ denotes that $t$ has an option to terminate immediately, i.e. $\varepsilon$ is a summand of $t$. For $x, y \in T(\Sigma_{PABMSC})$, and $M \subseteq A_o$, the predicate $\downarrow$ is defined in Table 7.

<table>
<thead>
<tr>
<th>Table 7: The predicate $\downarrow$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\varepsilon \downarrow$</td>
</tr>
<tr>
<td>$x \downarrow$</td>
</tr>
<tr>
<td>$(\sqrt{x}) \downarrow$</td>
</tr>
</tbody>
</table>

The intuitive idea of the binary operator $\Rightarrow$ is as follows: $t \Rightarrow s$ denotes that the process $t$ can execute the atomic action $a$ and after this execution step the resulting process is $s$. For $x, x', y, y' \in T(\Sigma_{PABMSC})$, $a \in A$, $M \subseteq A_o$, $i, j \in L(\langle iid \rangle)$, and $m \in L(\langle mid \rangle)$, the binary relations $\Rightarrow$ are defined in Table 8.

We will illustrate the use of these action relations with an example. Consider the following expression.

$$\lambda_b(out(a, b, k) \parallel in(a, b, k))$$

We have $out(a, b, k) \Rightarrow \varepsilon$, so we can derive $out(a, b, k) \parallel in(a, b, k) \Rightarrow \varepsilon \parallel in(a, b, k)$. From this we can conclude
Table 8: The action relations $\overset{\alpha}{\rightarrow}$

\[
\begin{array}{cccc}
\alpha & \overset{\alpha}{\rightarrow} & \varepsilon \\
\frac{x \overset{\alpha}{\rightarrow} x'}{x + y \overset{\alpha}{\rightarrow} x'} & \frac{y \overset{\alpha}{\rightarrow} y'}{x + y \overset{\alpha}{\rightarrow} y'} & \frac{x \overset{\alpha}{\rightarrow} x'}{x \cdot y \overset{\alpha}{\rightarrow} x' \cdot y} & \frac{x \downarrow, y \overset{\alpha}{\rightarrow} y'}{x \cdot y \overset{\alpha}{\rightarrow} y'} \\
\frac{x \overset{\alpha}{\rightarrow} x'}{x \parallel y \overset{\alpha}{\rightarrow} x' \parallel y} & \frac{y \overset{\alpha}{\rightarrow} y'}{x \parallel y \overset{\alpha}{\rightarrow} x \parallel y'} & \frac{x \overset{\alpha}{\rightarrow} x'}{x \parallel y \overset{\alpha}{\rightarrow} x' \parallel y}
\end{array}
\]

$A \subseteq A \cup A_i \cup x \overset{\alpha}{\rightarrow} x'$ \\
$\lambda_M(x) \overset{\alpha}{\rightarrow} \lambda_M(x') \\
\lambda_M(x) \overset{\text{out}(i,j,m)}{\rightarrow} \lambda_M(x') \\
\lambda_M(x) \overset{\text{in}(i,j,m)}{\rightarrow} \lambda_M(x')$

$\lambda_{\emptyset}(\text{out}(a,b,k) \parallel \text{in}(a,b,k)) \overset{\text{out}(a,b,k)}{\rightarrow} \lambda_{\emptyset}(\text{out}(a,b,k))(\varepsilon \parallel \text{in}(a,b,k))$

Next we have $\text{in}(a,b,k) \overset{\text{in}(a,b,k)}{\rightarrow} \varepsilon$, and we can derive $\varepsilon \parallel \text{in}(a,b,k) \overset{\text{in}(a,b,k)}{\rightarrow} \varepsilon \parallel \varepsilon$. Thus we have

$\lambda_{\emptyset}(\text{out}(a,b,k))(\varepsilon \parallel \text{in}(a,b,k)) \overset{\text{in}(a,b,k)}{\rightarrow} \lambda_{\emptyset}(\varepsilon \parallel \varepsilon)$

In order to see that this expression has the possibility to terminate, we derive $\varepsilon \downarrow$ and thus $(\varepsilon \parallel \varepsilon) \downarrow$, so

$\lambda_{\emptyset}(\varepsilon \parallel \varepsilon) \downarrow$

Finally, we conclude that the given process $\lambda_{\emptyset}(\text{out}(a,b,k) \parallel \text{in}(a,b,k))$ can first execute $\text{out}(a,b,k)$, then execute $\text{in}(a,b,k)$ and finally terminate. Note that this is the only execution sequence that can be derived from the inference rules.

### 7.2 Algebraic specification of the transition rules

The translation of the transition rules into an algebraic specification needs some explanation. In the transition rules we defined the transition predicate and the termination predicate. However, for a simulator we need to know for a given process algebra expression all possible transitions coming from this expression. Thus we are not interested in the transition relation itself, but in the function transitions which calculates for a given PROCESS a TRANSITIONLIST. A TRANSITION consists of an ATOM which is the label of the transition and a PROCESS which is the resulting process after executing the atomic action. Some additional functions are needed for calculating the list of transitions of a given process.

For example, Table 8 shows that if one wants to calculate the transitions for $x + y$, one simply has to calculate the transitions of both $x$ and $y$ (equation 4). The case of $x \cdot y$ is a bit more involved. By combining the two derivation rules for sequential composition from Table 8, we obtain equations 5 and 6. If we consider the case that $x$ does not terminate, the subtle point is that the transitions of $x \cdot y$ are not completely equal to the transitions of $x$. The residue after executing an action has to be extended with $y$. For this purpose we use the overloaded "·" function. The same procedure is carried out for the remaining operators.

The algebraic specification of the predicate terminates is straightforward.
7.2.1 Transitions

imports BMSC-Semantics

context-free syntax

"" ATOM """" PROCESS \rightarrow TRANSITION
""\{TRANSITION ""\}""\} "" TRANSITIONLIST
TRANSITIONLIST ""\u2227"" TRANSITIONLIST \rightarrow TRANSITIONLIST \{left\}
TRANSITIONLIST ""\u2225"" PROCESS \rightarrow TRANSITIONLIST
TRANSITIONLIST ""\u2227"" TRANSITIONLIST \rightarrow TRANSITIONLIST
""filter\,*\,*"" ATOM-SET ""\u2227"" TRANSITIONLIST \)\)\) \rightarrow TRANSITIONLIST

terminates(PROCESS) \rightarrow BOOL
transitions(PROCESS) \rightarrow TRANSITIONLIST

hiddens
variables

M \rightarrow ATOM-SET
x \rightarrow PROCESS
y \rightarrow PROCESS
a \rightarrow ATOM
t\{0-9\}* \rightarrow \{TRANSITION ""\}\*
""<"" id""\>""\{0-9\}* \rightarrow IID
""<"" mid""\>""\{0-9\}* \rightarrow MID
""<"" aid""\>""\{0-9\}* \rightarrow AID
equations

[1] transitions(\delta) = []
[2] transitions(e) = []
[3] transitions(a) = [\langle - a \rightarrow e \rangle]
[4] transitions(x \oplus y) = transitions(x) \cup transitions(y)
[5] transitions(x . y) = transitions(x) . y \cup transitions(y)

\textbf{when}
\quad \text{terminates}(x) = \text{true}

[6] transitions(x . y) = transitions(x) . y

\textbf{when}
\quad \text{terminates}(x) = \text{false}

[7] transitions(x \parallel y) = transitions(x) \parallel y \cup transitions(y)
[8] transitions(x \parallel y) = transitions(x) \parallel y
[9] transitions(\lambda_M (x)) = \text{filter}_M (transitions(x))

[10] terminates(e) = true
[11] terminates(a) = false
[12] terminates(\delta) = false
7.3 Simulation

A simulator displays the current state of the BMSC and offers the user a choice between all possible continuations. Such a STATE consists of three parts. The first component is the PROCESS under consideration. The second component, NUMBERED-TRLIST, is the list of transitions associated to this process. The transitions are numbered in order to offer the user the possibility of choosing such a transition. The third component of the state is an ATOMLIST which contains the history of the simulation session. It consists of all atomic actions chosen so far.
The function execute accepts a number and a state and calculates the resulting state after execution of the transition labeled with the given number.

Note that the imported module Naturals is not included in this paper. It defines the sort NAT with obvious properties.

### 7.3.1 Simulator

**Imports**: Naturals Transitions

**Exports**

- **Sorts**: NUMBERED-TRLIST, STATE, NUMBERED-TRANSITION, ATOMLIST, NUMBERED-ATOM, NUMBERED-ATOMLIST

**Context-free syntax**

- `initial-state(PROCESS)` → STATE
- `"<" PROCESS "" NUMBERED-TRLIST "" ATOMLIST "">"` → STATE
- `"{" [ATOM ".,"]* "}"` → ATOMLIST
- `"{" NAT ".," ATOM` → NUMBERED-ATOM
- `"{" [NUMBERED-ATOM ".,"]* "}"` → NUMBERED-ATOMLIST
- `ATOMLIST ".," ATOMLIST` → ATOMLIST
- `execute(NAT, STATE)` → ATOMLIST
- `number(TRANSITIONLIST)` → NUMBERED-TRLIST
- `number-from(NAT, TRANSITIONLIST)` → NUMBERED-TRLIST
- `NUMBERED-TRLIST ".," NUMBERED-TRLIST` → NUMBERED-TRLIST

**Hiddens**

- `tl` → TRANSITIONLIST
- `n` → NAT
- `a` → ATOM
- `al` → ATOMLIST
- `a[0-9]*".,"` → [ATOM ".,"]*
- `tr[0-9]*".,"` → [TRANSITION ".,"]*
- `ntr[0-9]*".,"` → [NUMBERED-TRANSITION ".,"]*
- `x[0-9]*".,"` → PROCESS
- `ntl` → NUMBERED-TRLIST

**Equations**

1. `number(tl) = number-from(1, tl)`
2. `number-from(n, []) = []`
3. `number-from(n, [(n) → a]) = [(n) → a] ∪ number-from(n + 1, [tr])`
4. `[ntr1] ∪ [ntr2] = [ntr1, ntr2]`
5. `execute(n, < x1, [ntr1], (n) → a → x2, [ntr2], al >) = < x2, number(transitions(x1)), al ∪ [a] >`
6. `[a1] ∪ [a2] = [a1, a2]`
7.4 Example

For the running example, represented by the term $\lambda_0(out(a, b, m) \cdot out(a, env, k) \parallel action(b, p) \cdot in(a, b, m))$ the set of transitions is $\{out(a, b, m) \rightarrow \lambda_0(out(a, env, k) \parallel action(b, p) \cdot in(a, b, m))$, $\lambda_0(out(a, b, m) \cdot out(a, env, k) \parallel in(a, b, m))\}$. This means that executing event $out(a, b, m)$ results in the BMSC represented by $\lambda_0(out(a, env, k) \parallel action(b, p) \cdot in(a, b, m))$ and that execution of the alternative action $action(b, p)$ results in $\lambda_0(out(a, b, m) \cdot out(a, env, k) \parallel in(a, b, m))$. Likewise, the transition sets of the resulting processes can be determined. If the BMSC is finished, the resulting process is $\varepsilon$.

If we select the simulate button in Figure 3, we obtain three windows from Figure 8. The upper window is the selection window, in which all possible continuations of the BMSC are displayed. Either event may occur. The middle window displays the list of all events executed until now. This list is empty. The lower window shows the process algebra representation of the BMSC under consideration.

![Figure 8: Starting the simulator](image)

If the user selects the first event, all windows will be updated (see Figure 9). The selection window now contains a new choice. The trace window contains the chosen event and the current window contains the process algebra representation of the BMSC resulting after having executed the event.

![Figure 9: Result after selecting event number (1) in the previous figure](image)

If we subsequently select the second event, we obtain the situation from Figure 10.
Next, we select the first event and obtain the situation from Figure 11.

Finally, there's only one remaining event. The result of selecting this event is in Figure 12. It shows that execution of the BMSC is finished.

8 Conclusions

The main objective of this case study was to provide evidence that the formal semantics definition of Basic Message Sequence Charts can be used to derive tools in a straightforward way. The translation of the process algebra and the definitions of the semantics functions into algebraic specifications is easy, but care has to be taken when implementing them as rewrite rules. In order to obtain a nice term rewriting system, some rules have to be deleted, added or modified.

We also specified a simulator tool based on the operational semantics for Message Sequence Charts. The definition of this simulator could serve as a formal specification of such a tool. Finally, we formalized the static requirements.

By using the ASF+SDF Meta-environment we derived (prototypes of) tools for BMSCs. It proved to be a flexible programming environment whose capabilities of incremental development helped in easy prototyping. The possibilities of defining a user interface on top of the term rewrite engine enables the generation of demonstrable and usable tools.
Specification of tools for Message Sequence Charts

The possibility of prototyping makes it easy to explore new versions of MSC in standardization work and to make dialects of MSC for internal use. Changes to the syntax only require minor modifications to the specification. Changes with respect to the semantics and new language features require modification of the formal semantics and a corresponding modification of the specification.

A disadvantage of the term rewriting paradigm in ASF+SDF is that, sometimes, easy to understand algebraic rules have to be transformed into a more implementation directed form. The transformation into a TRS sometimes implies that decisions on implementation details are made, which were not expressed in the algebraic specification. For example, if we aim at complete TRSs (i.e. TRSs which are confluent and terminating, see [Klo92]), we need to decide on the implementation of commutative operators and the implementation of sets by ordered lists. Therefore, a completely automatic implementation of an algebraically specified semantics by means of a TRS is not always feasible.

The techniques described in this paper can be easily extended to the general setting of Message Sequence Charts. Due to the modular description, the framework for Basic Message Sequence Charts can be reused almost completely.

Starting from the algebraic specifications, there are two ways to proceed with the development of real tools. The obvious way is to manually translate the functionality expressed in the equations into efficient code. The specification can then be used for validation purposes. The second way is to (semi-) automatically generate efficient programs. This is topic of ongoing research ([RW93]).

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