Performance Evaluation of an Optical Transparent Access Tier Based on PON and Spectral Codes

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Abstract—The increasing amount of bandwidth requirements and quality of service needs for the next-generation access networks has boosted extensive research in the fiber-optics communication field. In this light, passive optical networks (PONs) combined with optical code division multiple access (OCDMA), provide a potentially cost-effective solution to meet such bandwidth demands. This work proposes an optical transparent architecture which enables all-optical communication between the network nodes. The encoded data streams are multiplexed at a merging point which results in multiple user interference (MUI), thus significantly reducing the network throughput. The networking nodes are able to monitor and record user activity in the PON, and further register the (past) state of activity at the merging point. In this work, we study the coherence of state between the networking nodes and the merging point, for different packet size distributions, in order to predict an optimal transmission instant of each node’s data packets. We note that the states are coherent depending on the packet size distribution.

Index Terms—Code division multiaccess; Coherence of state; Network performance; Optical fiber communication; Passive optical networks.

I. INTRODUCTION

A THE TIME of writing, it is estimated that over one billion ($10^9$) people worldwide have access to the Internet [1]. A large-scale measurement experiment recently disclosed important details of commercial access networks in the USA and Europe [2]. Essentially, the traditional digital subscriber line (DSL) and coaxial cable (COAX) networks were evaluated in terms of up/downstream bandwidth (BW), packet latency and packet loss. The measured link BWs were much lower than future residential BW requirements, which have been estimated in the range from 2/20 Mbps [3] to 30/100 Mbps [4]. Additionally, although measured bandwidths have been observed highly asymmetrical, the authors in [5] have shown that traffic patterns are becoming more and more symmetrical. Also the values measured for packet jitter and queueing delay differ significantly from recommended values for interactive services [6]. Therefore, a low quality of service (QoS) is to be expected in DSL and COAX networks for future bandwidth-intensive and time-critical services. Moreover, the network infrastructure has to cope with the increasingly popular peer-to-peer networking which is becoming the dominant application in terms of transmitted traffic volumes. Considering the above, only a fiber-optic network is able to provide a future-proof solution.

This work proposes an optical transparent access tier to meet the requirements for the next-generation access networks. The architecture is based on passive optical networks and optical codes for shared medium access. Recently, promising experimental results have been shown using different optical coding techniques [7], [8]. The encoded data streams of networking nodes are asynchronously combined into a single stream at a merging point and may be passively broadcasted even to nodes located in other PONs connected. This way all-optical node-to-node communication is permitted which is an important added value, especially in access networks.

Inherently, the use of optical codes implies soft capacity degradation, which decreases the effective network throughput if not properly managed. In this work, the optical nodes have the ability to sense the signal level at the merging point, and even infer the user activity. This can be exploited in scheduling network access, as previously reported in [9] employing incoherent time-domain optical codes.

This paper analyzes the coherence of state between the optical node and the merging point where the data streams are multiplexed. That is, it is studied whether or not the level of activity sensed by the optical node remains stable with respect to the activity at the merging point. Unlike the authors in [9], this work proposes the use of orthogonal codes that do not employ time-domain chips and we further analyze the coherence of state from a packet level. The analysis also assumes different packet size distributions, and a bimodal distribution that accurately captures the measured packet size distribution in real networks [10]. Finally, coherence of state has a direct application in the definition of medium access control (MAC) protocols that control the access to the passive optical network. By sensing the activity at the merging point, the end optical nodes have a means to decide the appropriate transmission instant of its packets, on attempts to reduce interference.

The remainder of this work is organized as follows: Section II motivates the use of an optical transparent tier at
the network access, showing its benefits in three emerging network scenarios. Then, the underlying physical architecture is presented in section III and it is shown that its performance is mainly limited by the interference between active users. A key functionality, all-optical traffic monitoring, is introduced at the end of section III which may be used to anticipate on the network activity. The coherence of state between the optical node and the merging point is further analyzed for different packet size distributions and user scenarios in section IV through section VI. Transmission scheduling is presented as a straightforward application of coherence of state in section VII. Finally, a summary of the main contributions of this work is given in section VIII.

In conclusion, this paper provides a novel architecture proposal in the network access, it further shows its limitation in terms of MUI, studies the validity of the monitored interference information via the coherence of state analysis, and proposes how to overcome this limitation via transmission scheduling. To the best of our knowledge, there is no other work that provides such a complete treatment of such optical transparent architecture.

II. Motivation

In this section, the main characteristics of fiber-optics are presented and optical transparency is shown to have added value. Three emerging network scenarios are discussed, namely personal, residential and business, which all benefit from an optical transparent access tier.

Fiber optics provide a strong alternative to alleviate the access bottleneck because of its extremely large bandwidth capacity, low propagation loss and signal transparency. Moreover, optical signal processing and switching speed exceed the capabilities in the electrical domain with less required power consumption per bit [11]. Optical access networks are increasingly being deployed either to replace the existing infrastructure because of lower operational expenses (OPEX), or in green-field situations because of lower capital expenses (CAPEX) [12]. Today’s preferred optical architecture is the PON where multiple optical networking units (ONUs) are connected to a central office (CO) via a single passively split optical fiber. Such a topology becomes cost-efficient when the distance increases between the CO and ONUs and/or when the splitting ratio increases [13].

Downstream traffic is broadcasted from the CO to the ONUs while medium access has to be provided in case of upstream traffic. Conventional systems enable shared access via established time or wavelength division multiple access (TDMA, WDMA). Instead, optical codes are proposed (hence denoted OCDMA) which rely on communication via a unique and orthogonal code. The orthogonality of the code allows the carrier to be asynchronously shared with other users on the network. The primary application domain of OCDMA is the access network because it offers cost-effective network deployment and management combined with physical layer security [14]. Additionally, OCDMA has a natural fit on PON because both are based on broadcast-and-select. Moreover, in a multiple wavelength channel system it allows a code reuse per channel. Thus OCDMA offers cost-effective network access to a large number of subscribers on the reduced infrastructure costs of a PON.

Ubiquitous broadband connectivity and mobility are two network experiences which have become a commodity. Mobile users increasingly interconnect their personal devices to form their own short-range personal area network (PAN) which is enabled by Bluetooth or IEEE 802.15 [15]. The future communication needs of these subscribers is reflected in the recently introduced personal network (PN) concept for global connectivity to personalized networks [16]. If the PAN (a truly mobile network) is taken as an entity, a PN is defined by the PAN and the other remote personal devices the PAN is connected with. An optical transparent access network mitigates many issues currently encountered regarding connectivity and mobility management in PNs [17].

Recently, researchers have analyzed residential networks by studying its parameters, traffic characteristics [18] and implications on the higher network tiers. A conclusion shared by all studies is that peer-to-peer (P2P) communication remains to be a heavy load on the network. Small-world properties are attributed to typical P2P applications such as eMule and BitTorrent [19]. However, in practice, poor locality was shown because more than 70% of existing local content was downloaded from peers outside the domain of the internet service provider (ISP) [5], [20]. Locality-aware protocols have been proposed in order to reduce cross-ISP/cross-tier traffic [21]. Certainly, an increase of local traffic intensity is not supported by the access tier in its current state.

Reliable connections while accessing a shared network such as the Internet is an essential asset in a business environment [22]. Virtual private networks (VPNs) are mostly used because they offer cost savings and communication privacy, and can be implemented in different network layers [23]. Small- to medium-size enterprises may lease a VPN for a cost-efficient business network deployment and operation. Large enterprizes or research institutes with a privately owned infrastructure may run secure connections if different (corporate) parties are using the network. A VPN implemented in Layer 1, or optical VPN (OVPN), is considered to be a key service in the next-generation transport network given its high speed, efficiency and low cost [24]. An optical transparent access layer has an obvious key role in establishing OVPNs.

In summary, the three network scenarios (personal, residential and business) and the particular benefits of transparent optical networks (reliability, reduced complexity, power efficiency and processing speeds) strongly motivate the introduction of optical technologies in the access domain. In the remaining of this work, a solution based on OCDMA and PONs is proposed and analyzed in detail as a potentially cost-effective architecture to be deployed in an optical transparent access tier.

III. Proposed network design

In this section we discuss in detail the optical access network architecture and its parameters, the transmission techniques and traffic handling. Transparent user-to-user communication is proposed by employing optical codes. Out of the many available techniques, incoherent spectral amplitude
coding is depicted as a candidate to implement such transmission scenario because of specific cost-reducing system characteristics. This section concludes with a brief discussion on code-based all-optical contention resolution schemes.

A. Architecture

The optical access network architecture is based on multiple passive optical networks connected to a single central office as depicted in Fig. 1 which is similar to [1]. As shown, the central office has \( M \) PONs connected to it. Each of them has \( N_i \) ONUs which is equal to the splitting ratio \( N_i \) of the passive coupler. Obviously, the value \( M \) is largely determined by the backplane of the CO while \( N_i \) has a physical limitation via the power budget. The power budget determines the allowable losses on the path between a source and destination for a given transmitter power and receiver sensitivity. Current PON deployments use \( N_i = 32 \) or \( N_i = 64 \) as maximum splitting ratio which gives an ideal power loss of \( 10\log(N_i) \) dB plus excess losses. Considering the fiber lengths we assume an urban area scenario meaning a distribution fiber of 1 km and a feeder fiber of 4 km. As shown in Fig. 1, separated fibers are used for up and downstream transmission. The operating bit rate is the synchronous transfer mode (STM)-1 base rate (155.52 Mbps) in order to meet the future BW requirements.

B. Transparent communication via optical codes

The situation may occur when two users located at different ONUs are communicating with each via the CO and, normally, such ONU-to-ONU (O2O) communication requires a conversion to the electronic domain in order to perform the routing of the data. All-optical communication between ONUs results in two additional O2O traffic streams depending on the location of the destination. Both are shown in Fig. 1 next to the regular CO-ONU traffic. All-optical O2O communication has been studied in case of a single PON, i.e. [25], or recently, in case of a sub-net of PONs [26], [27]. The authors in [26] use time slots in a wavelength division multiplexing (WDM) scheme which require a central clock for synchronous access and accurate traffic scheduling to avoid contention. A synchronous time-slotted PON is a complex solution considering the application area. We proposed to use optical codes (OC) instead of time slots on WDM PON and to enable O2O communication in a sub-net of PONs [27].

The O2O data is transmitted on the optical address of the destination. The address is unique and composed by an optical wavelength and a code. Each individual bit is coded with the address instead of only an OC label in front of the data packet such as in optical code generalized multi-protocol label switching (OC-GMPLS) systems. In this work no wavelength conversion nor code conversion is applied in any node between two ONUs in order to have end-to-end truly all-optical communication.

C. Address and traffic handling

If data is ready for transmission, the ONU acquires the optical address of the destination at the CO. We assume that a dedicated collision-free communication channel exists between the CO and ONUs which is used for transmission control and coordination according to a standard common control-channel architecture. The channel is placed out-of-band to not interfere with the data transmission channels. Three forms of address usage are possible namely fixed, semi-dynamic (e.g. the destination either has a fixed code or wavelength and tunes to an available wavelength or code) or dynamic (e.g. the destination may tune to any available address). Thus the transmitter is always tunable but a negligible tuning time is considered. The dynamic entity in the optical address may be assigned via, for example, a list-scheduling algorithm or a hash function.

Users A-D in Fig. 1 may be either fixed and/or mobile network subscribers depending on which network scenario is considered (see Section II). The data for fixed users located at ONU\(_{a,b}\) could be aggregated in a burst. If a mobile user moves from ONU\(_{a,b}\) to ONU\(_{a+1,b}\), the connection should remain with data routed accordingly. The wireless network service can be transparently deployed by using radio-over-fiber techniques as shown in [17]. The CO has a regularly updated list of all active users in the network. As such it keeps track at which ONU a user is located and registers movements from ONU\(_{a,b}\) to ONU\(_{a+1,b}\).

D. Spectral amplitude optical coding

A classification of the available optical coding techniques can be done via the correlation principle (coherent or incoherent), coding domain (time, frequency, or time and frequency), en/decoder implementation (free-space, fiber-based or integrated), and line code (unipolar or polar signaling). We consider the cost-effective spectral amplitude optical coding technique to further reduce the CAPEX and OPEX of the code-based optical access network [28].

Spectral amplitude optical coding employs incoherent correlation, frequency codes, integrated en/decoders (E/Ds) and polar signaling. Here the E/Ds are amplitude filters which imprint their filter pattern, \( A(\omega) \), in the optical field of a broad spectral incoherent source to form a spectral code. This source may be a superluminescent light emitting diode (SLED). The E/D is based on the well-known unbalanced Mach-Zehnder interferometer (MZI) which naturally generates two complementary (or \( \pi \)-shifted) and periodic fringe patterns. The periodicity is defined as the free spectral range (FSR) of the device. Multi-staged configurations with tunable phase shifters are used to generate different, orthogonal filter patterns which represent the spectral codes.

The spectral code and its complementary, \( \overline{A}(\omega) \), are used to transmit the binary data in the optical domain. For example, \( A(\omega) \) is transmitted to represent the logical one and \( \overline{A}(\omega) \) is sent to represent the logical zero. This type of modulation is denoted spectral shift keying (SSK). A similar tunable E/D, \( B(\omega) \), is placed at the receiver side which is combined with a balanced detector. If \( A(\omega) = B(\omega) \) the optical power at the E/D output varies between a maximum and minimum value whereas if \( A(\omega) \neq B(\omega) \) average optical power is received at both outputs. SSK combined with balanced detection leads to polar signaling and has a 3-dB signal to noise (SNR) ratio compared with on-off keying (OOK). Note that coding in
Fig. 1. Passive optical network-based access network and the traffic streams

Fig. 2. Incoherent time vs spectral amplitude optical coding (three bits shown)

an SSK system is done at the bit rate $B$, rather than using chips at the chip rate $C$ of, for example, an incoherent time-domain OCDMA system which typically results in a lower required system bandwidth and optical sources with a lower complexity. The difference between an incoherent time and wavelength-domain OCDMA system is schematically shown in Fig. 2 for the bit sequence 110.

A spectral amplitude encoded optical code multiple access (SAE OCDMA) PON is shown in Fig. 3 for an upstream configuration. As shown, the output of the SLED is filtered by the bandpass filter (BPF) which -3 dB bandwidth equals to one period (or FSR) of the MZ-based cascade E/D. The spectral slice is led into the optical switch to perform the SSK modulation by alternatively launching the optical power at the upper or the lower input of the encoder. The ONU is able to tune to an available wavelength(-band) in a WDM scheme. An optical amplifier finally compensates for the losses experienced by the coding and switch. The encoded optical stream is launched onto the distribution fiber $L_d$ and multiplexed with other streams at the passive coupler. At the CO in Fig. 3, the optical stream is received by a tree E/D which is a parallel code processing element, and balanced detection. The system nodes shown in Fig. 3 are fully integrateable into an optical chip with other optical functions, which enables large-scale system deployment by means of mass production.

E. Contention resolution and activity monitoring

Collisions are at stake when multiple ONUs in Fig. 1 want to send data upstream to the same destination. All-optical code-labeled contention resolution has been proposed and analyzed in [29] for such a network. A combination of optical code-sense medium access /collision detection (OCSMA/CD) and code-labeled packet switching has been proposed. The feasibility of implementing such methods has to be carefully considered therefore a number of issues such as the scalability and complexity is addressed.

OCSMA/CD requires a reflective PON, i.e. the optical power of a transmitting ONU is reflected to all other ONUs except to itself. Let us assume that a given ONU is equipped with code sensing capabilities such that it can detect how many codes or users are active. A proposed design is depicted in Fig. 4 which is able to perform OCSMA/CD combined with code activity monitoring for a specific optical channel. As mentioned before, the ONU receives the transmitted data of the other ONUs which are directed to the tree E/D via the optical circulator after selecting the transmission band with the tunable BPF. The transmission scheduling module also contains a means to store data in an electronic buffer. Recently, a similar tree E/D has been used in field experiments employing coherent wavelength-domain OCs [8] which indicates its potential. The design in Fig. 4 can be fully integrated using hybrid techniques on Silicon.

IV. PERFORMANCE EVALUATION

A well-known limiting factor of OCDMA networks is the multiple user (or access) interference. In this section, we
provide a performance evaluation in terms of the bit error rate (BER) caused by mutual interference.

A. Multiple user interference

As more users simultaneously access the medium, the interference between codes increases at the expense of network throughput. For example, consider an incoherent time-encoded OCDMA system. At the transmitter-side, fiber delay lines apply time-shifts to arrange pulses in order to create an orthogonal sequence. At the receiver, the opposite configuration is used to reconstruct the original high-intensity data signal via incoherent summation of the pulses. Random network access by multiple users may lead to the so-called false positives at receivers (i.e. bit detection where no bit was actually transmitted), which is caused by the summation of time-shifted codes.

A promising method to reduce the MUI in this system was proposed in [30] and experimentally confirmed in [31]. In their approach, interference avoidance (IA) decides the ideal bit release time with respect to the transmitted signals sensed on the line in order to avoid interference, thereby improving throughput. The IA protocol operates at the chip (rate) level. In the case of SAE OCDMA, interference is experienced as long as different codes overlap. Moreover SSK also transmits a code to represent a logical zero while in [30] OOK is used. As such, the interference in the SAE OCDMA system occurs asynchronously during the whole duration of the packet. Under the assumption of Internet protocol (IP) packet transmission, a single bit error directly translates into packet drop at the next IP hop, regardless of the number of bits involved.

A fundamental assessment of the MUI in SSK SAE-OCDMA is shown in [32] where the noise power at the balanced detector is evaluated. The noise can be modeled by the sum of a number of individual noise components, namely thermal, shot and speckle noise. The latter refers to the intensity fluctuations caused by the incoherent summation of signal powers when spectral codes overlap. This noise source is denoted speckle noise by [32] because it is a similar mechanism that gives rise to the spatial intensity variations in coherent images called "speckle". In order to avoid confusion, this work refers to the noise source as incoherent speckle noise. Incoherent speckle noise is a major contributor to MUI and is even present in the absence of interfering users. The components of the total noise power are given as follows (the derivation of the equations can be found in [32]). Note that modulator noise, RF amplifier noise and other noise sources are not included in the analysis.

The thermal noise $\langle I_2^{th} \rangle$ is given by

$$\langle I_2^{th} \rangle = 8\pi kT B_d^2 C$$

with $k$ the Boltzmann constant, $T$ the temperature in Kelvin, $B_d$ the detector bandwidth in Hertz and $C$ the load capacitance in Farad.

The shot noise $\langle I_2^{sh} \rangle$ follows

$$\langle I_2^{sh} \rangle = 2q\Re P_{rec} u B_d$$

with $q$ the charge of an electron in Coulomb, $\Re$ the responsivity of the photodetector, $P_{rec}$ the received power in Watt, and $u$ the number of active users.

Finally the incoherent speckle noise $\langle I_2^{sp} \rangle$ is described by

$$\langle I_2^{sp} \rangle = \Re^2 P_{rec}^2 (u^2 + 1) \frac{2B_d}{mMB_{opt}}$$

with $m = 1$ for polarized light and $m = 2$ for unpolarized light, $M$ the number of modes in the fiber and $B_{opt}$ the spectral width of the code in Hertz.

The total noise contribution $\langle I_2^n \rangle$ at the detector is then

$$\langle I_2^n \rangle = \langle I_2^{th} \rangle + \langle I_2^{sh} \rangle + \langle I_2^{sp} \rangle.$$  

On the other hand, the signal power is given by $I_2^{sig} = \Re^2 P_{rec}^2$. Thus, given a number of users $u$, the bit error rate (BER$_u$)
that they experience is calculated as [32]

\[ BER_{\text{u}} = \frac{1}{2} \left[ 1 - \text{erf} \left( \frac{I_{\text{sig}}}{\sqrt{I_{n}^2}} \right) \right] \]  (5)

The following realistic parameters apply to our system, namely: \( R = 0.71, P_{\text{tot}} = 10^{-6} \) W (per user), \( T = 293 \) K, \( C = 0.02 \cdot 10^{-12} \) C, \( m = M = 1 \), \( B_d = 0.75 \cdot B \) Hz, \( B_{\text{opt}} = 624 \cdot 10^9 \) Hz (=5 nm at 1550 nm). With these values, Fig. 5 shows the calculated BER\(_{\text{u}}\) versus \( u \) (the number of active users) assuming \( B = 155.52 \) Mbps. The detrimental effect of MUI in an SAE OCDMA system becomes clear, since the more users transmitting simultaneously, the higher the bit error rate experienced. In the figure, the error-free (BER=10\(^{-9}\)) limit and a forward error correction (FEC) limit of 10\(^{-5}\) are exceeded when more than twelve and seventeen users are active, respectively. Authors in [33] show that a BER of 3.3·10\(^{-3}\) may be corrected to 10\(^{-9}\) for a 7% FEC overhead. Therefore, the limit of 10\(^{-5}\) introduces a margin in order to alleviate strict requirements to implement FEC in the noisy SAE-OCDMA environment. As indicated by [32], an increase in the received power only improves performance when multimode fiber (MMF, \( M > 1 \)) is used. Other solutions to reduce BER comprise either the increase of \( B_{\text{opt}} \) on attempts to spread the effect of incoherent speckle noise or a reduction of the bit rate. Additionally, Fig. 5 shows that the SAE OCDMA system performance does not depend on which particular codes are being used on the network. This characteristic, combined with the fact that interference is experienced at packet level, deduces the objective to minimize the code activity on the network based on the interference sensed on the line.

**B. Average BER versus network load**

Let \( R_{\text{u}} \) be the average packet or burst arrival rate per user and let \( 1/\tau_{\text{x}} \) be the average transmission time. Then, \( \rho = R_{\text{u}}/\tau_{\text{x}} \) is the utilization factor of the output queue at the ONU, smaller than one for stable queues. Note that, from direct application of the well-known PASTA (Poisson Arrivals See Time Averages) property, the utilization factor is the probability to find the queue is busy, as seen by a random (Poisson) arrival. Furthermore, this result holds regardless of the packet or burst size distribution. Then, it can be assumed that a given user is active (i.e. transmitting a data packet or burst) with probability \( \rho \). The probability \( p(u) \) to find exactly \( u \) active users out of a total population of \( U \) users is then given by the following Binomial distribution

\[ p(u) = \binom{U}{u} \rho^u (1 - \rho)^{U-u}, \quad u = 0, \ldots, U \]  (6)

with \( U = 64 \) ONUs, as noted in section III.

Eq. 6 above can be combined with Eq. 5 to obtain the average BER probability (denoted \( \overline{BER} \)) as a function of the number of users, as given by

\[ \overline{BER} = \sum_{u=0}^{U} BER_{\text{u}} p(u) \]  (7)

Eq. 7 has been plotted in Fig. 6 for several values of \( \rho \).

For example, the chosen FEC limit of 10\(^{-5}\) imposes a load operation below 20% in this architecture, as shown in Fig. 6.

**V. COHERENCE OF STATE ANALYSIS**

Coherence of state is defined as a property by which state at a measurement point and instant is correlated to the state in other measurement point and instant. In [9], the state of the line at the ONU and the merging point is found coherent via the Pearson’s correlation coefficient, under the assumption of exponential packet or burst size distributions.

In the forthcoming, a more rigorous estimation of such coherence of state is derived which takes into account other packet size distributions and also an empirically-observed bimodal distribution. The reader should note that such analysis is performed at the packet level, rather than at the chip level as pointed out in Section IV, given the particular characteristics of the optical codes used. The equations derived shall be evaluated with numerical examples in the next section.

The problem can be stated as follows: Given a set of observations of past “activity” by one of the ONUs, it is
desired to find the probability that such activity will remain at the merging point $d$ seconds into the future ($d > 0$), as shown in Fig. 7. For the sake of simplicity, both ONUs in Fig. 7 are assumed equidistant with respect to the passive coupler i.e. fixed delay $\tau$ is assumed), and only the upstream direction is considered.

The following studies the case for single and multiple active users.

A. Single active user

Let $X$ be the packet duration. Let $\{Y_1, Y_2, \ldots, Y_n, \ldots\}$ be the sampling time instants, with $Y_n = n \cdot \delta$ and $\delta$ is the sampling interval. Let $Y_n = 1$ if activity is sensed and zero otherwise. Our aim is to calculate

$$P(X > n\delta + d|Y_1 = 1, \ldots, Y_n = 1) = P(X > n\delta + d|X > n\delta)$$

for $\delta > 0$ and different packet length distributions, namely an exponential, Gaussian, Pareto and an empirically-observed bimodal distribution.

1) Exponential random variable: If the packet duration $X$ is exponentially distributed, with parameter $\mu$, then, due to its memoryless property it turns out that

$$P(X > n\delta + d|Y_1 = 1, \ldots, Y_n = 1) = P(X > d) = e^{-\mu d}$$

2) Pareto random variable: If $X$ is Pareto of the second kind (Lomax) with tail index $\alpha$, that is

$$P(X \geq x) = (x + 1)^{-\alpha}, x > 0$$

then

$$P(X > n\delta + d|X > n\delta) = \frac{(1 + n\delta + d)^{-\alpha}}{(1 + n\delta d)^{-\alpha}}$$

$$= \left(\frac{1 + n\delta + d}{1 + n\delta d}\right)^{\alpha}$$

It is worth mentioning that for $1 < \alpha \leq 2$ the Pareto distribution has an infinite variance with a finite mean which represents a heavy-tailed packet length distribution.

3) Gaussian random variable: If $X$ is a Gaussian random variable with mean $\mu$ and standard deviation $\sigma$ then

$$P(X > n\delta + d|X > n\delta) = \frac{1 - \Phi\left(\frac{n\delta + d - \mu}{\sigma}\right)}{1 - \Phi\left(\frac{n\delta - \mu}{\sigma}\right)}$$

where $\Phi(\cdot)$ is the distribution function of the standard Gaussian random variable.

4) Bimodal random variable: It has been observed in previous measurement studies that the packet size distribution typically follows a bimodal distribution, that can be accurately characterized by the following combination of two Gaussian distributions (see [10]):

$$P(X = x) = \alpha_1 N(\mu_1, \sigma_1) + \alpha_2 N(\mu_2, \sigma_2), \quad x \geq 0$$

where $N(\mu, \sigma)$ is the probability density function (PDF) of a Gaussian distribution with mean $\mu$ and standard deviation $\sigma$.

The values used in [10] to empirically characterize the packet size distribution are $\alpha_1 = 0.74$, $\mu_1 = 127$ bytes, $\alpha_2 = 0.26$, $\mu_2 = 1366$ bytes, and $\sigma_1 = \sigma_2 = 20$ bytes. In this case:

$$P(X > n\delta + d|X > n\delta) = \frac{1 - \left[\alpha_1 \Phi\left(\frac{n\delta + d - \mu_1}{\sigma_1}\right) + \alpha_2 \Phi\left(\frac{n\delta - \mu_2}{\sigma_2}\right)\right]}{1 - \left[\alpha_1 \Phi\left(\frac{n\delta - \mu_1}{\sigma_1}\right) + \alpha_2 \Phi\left(\frac{n\delta - \mu_2}{\sigma_2}\right)\right]}$$

B. Multiple active users

Consider multiple active users $u = 1, 2, \ldots, U$ in the network, each of them transmitting with its own code $C_1, C_2, \ldots, C_u$, and let $n_1, \ldots, n_u$ be the past activity intervals as sensed by a given ONU. Without loss of generality, let us assume that $n_1 \geq n_2 \geq \ldots \geq n_u$, as illustrated in Fig. 8.

Coherence of state refers to the probability to have all $u$ users active $d$ seconds later, whereby a fixed propagation delay $\tau$ is assumed. Then, in order to have all users active $d$ seconds in the future, it is a necessary and sufficient condition that the minimum of them remain active for $d$ seconds in the future, i.e (15).

Clearly

$$\frac{P(X > n\delta + d)}{P(X > n\delta)} < 1, \quad i = 1, \ldots, u$$

which directly implies that

$$\lim_{n \to \infty} P(\min(X_1, \ldots, X_u) > n_\delta + d) = 0$$

Namely, as the number of active
users increases the coherence of state approaches null. Furthermore, $P(\min(X_1, \ldots, X_u) > n_u \delta + d|X_1 > n_1 \delta, \ldots, X_u > n_u \delta)$ is strictly decreasing with $u$, the number of active users. Also, the more active users sensed, the less coherence of state between the merging point and the optical node. Intuitively, when a large number of codes are present, it is more unlikely to have all of them active for $d$ seconds into the future.

The following solves Eq. 15 for different packet size distributions.

1) **Exponential random variable**: In this case, (16) where $1/\mu_i$ is the mean packet duration for each code. If all packets are assumed to have the same average size, the above simply yields $P(\min(X_1, \ldots, X_u) > n_u \delta + d|X_1 > n_1 \delta, \ldots, X_u > n_u \delta) = e^{-u\delta d}$.

2) **Pareto random variable**: In this case, (17).

3) **Gaussian random variable**: In this case, (18).

4) **Bimodal random variable**: In this case, (19).

**VI. COHERENCE OF STATE EXPERIMENTS**

In this section, a number of numerical examples are proposed to evaluate the coherence of state between a given ONU and the passive coupler when either a single user is transmitting or a number of them.

**A. Simulation parameters**

In all packet size distributions, the mean value has been assumed $EX = 0.74 \times 127 + 0.26 \times 1366 = 449.14$ bytes, since this is the average empirical packet size [10]. This gives an average transmission delay of $23.14 \mu$s at $B = 155.52$ Mbps. For Pareto distributed packet sizes, the simulation value of $\alpha$ was $\alpha = 1.2$, and for Gaussian packet lengths, $\sigma_X = 0.5EX$. Finally, the sampling instant was $5\delta$, where $\delta \in \{0.01EX, 0.1EX, 0.25EX, 0.5EX\}$, and an optical fiber length $L = 1$ km which yields a propagation delay $\tau = 4.8 \mu$s. With these parameters, the following shows the coherence of state assuming a single active user, and multiple active.
users, for all packet size distributions discussed in the previous section.

B. Single user experiments

Fig. 9 shows the complementary cumulative distribution function (CCDF) for the four packet size distributions under study. As shown, exponential (memoryless) behavior shows a straight line CCDF, whereas the Gaussian and Pareto show faster-than and slower-than exponential decay respectively. The bimodal distribution appears as a combination of two exponential distributions (two straight lines).

It is interesting to observe that the higher the values for inter-sampling instants (δ) the more exponential-like behavior observed as indicated by the straight line in the semi-log y-axis. Clearly, the information of previous instants vanishes the more you wait for the next sampling instant, thus approaching memoryless behavior as shown in Fig. 9 bottom-right. Hence, when the sampling ratio is large enough, memorylessness may be assumed.

C. Multi-user experiments

Fig. 10 shows the CCDF of the transmission time duration of all ONUs when a different number of them is sensed. In this case, δ = 0.1EX (2.314 μs). Obviously, the higher amount of codes sensed under transmission, the more time it is necessary to wait until all of them have finished their transmission.

As shown, the CCDF remains the same during some time (d ≤ 20 μs) when more than two users are sensed in the Bimodal packet size distribution (bottom-right).

VII. TOWARDS TRANSMISSION SCHEDULING

As mentioned before, coherence of state can be used to schedule the transmission of the next packet, that is, to determine the most suitable packet release time in terms of bit error rate.

Essentially, when a number of u users have been sensed active, the addition of a new user into the network substantially increases the BER due to interference (Fig. 5). Then, a given ONU might decide to wait for a certain amount of time until one or more active users have finished transmitting their packets.

In this light, let X_1, ..., X_u denote the random variables which represent the transmission duration of ONU number 1, ..., u respectively, and let X_1 < X_2 < ... < X_u without loss of generality. Then, the j-th order statistic:

\[ f_{X_j}(t) = \frac{u!}{(j-1)!(u-j)!} f_X(t) F(t)^{j-1} (1 - F(t))^{u-j} \quad (20) \]

denotes the probability density function of the j-th packet to have finished its transmission. For the particular case of the exponential distribution, Eq. 20 yields:

\[ f_{X_j}(d) = \frac{u!}{(j-1)!(u-j)!} \mu e^{-\mu d} (1 - e^{-\mu d})^{j-1} e^{-\mu(u-j)d} \quad (21) \]

Essentially, Eq. 21 gives the probability to have j ONUs having finished its transmission, thus u - j still under transmission. Hence, if for BER requirements, the system imposes a maximum of 17 ONUs under transmission at the same time (see Fig. 5), then Eq. 21 gives the amount of time required to wait such that u - j ONUs or less are still under transmission.

As a numerical example, let u = 20 denote the actual number of users active, as sensed by the 21-st user. Let user number 21 decide to schedule (delay) its packet to an instant such that the probability to have 11 users or less becomes 95%. The order statistics defined above can be used to answer the following question: How long is it necessary to wait until only 11 users at most are present in the PON with 95% confidence?

Fig. 11 shows the order statistics j ∈ \{1, 5, 9, 13\} assuming that u = 20 are observed active. For brevity, only exponential distributed packet sizes are considered in this example. As shown, at time t = 10 μs, the first five users are very likely to have completed its transmission with probability 1.0000, 0.9978, 0.9883, 0.9568 and 0.8844 respectively. However, the ninth and thirteenth users exhibit a probability of 0.2420 and 0.0063 to have completed the transmission of their packets. Hence, the ONU sensing the channel is 95% confident that,
at time $t = 10 \mu s$ (remember the propagation delay is approximately $5 \mu s$ if the ONUs are 1 km away from the optical merging point), about four ONUs have completed their transmission. As a result, there are no more than $20 - 4 = 16$ ONUs transmitting simultaneously in the PON under the assumption that no other ONU has started its transmission, of course. Thus, the ONU may decide to transmit at that time (16 users is still below the FEC limit see Fig. 5).

It is important to remark that such conclusions are only valid if no other ONU has started any transmission within the period of time of $10 \mu s$. The reader should note that this probability is very small for such a short period of time.

VIII. SUMMARY

Optical technologies overcome the quality of service issues currently encountered in the access network. In this work, the future wired and wireless communication needs are reflected in personal, residential and business networks which all benefit from the deployment of an optical transparent access tier. We have presented, for the first time in full detail, an architecture based on PONs and spectral amplitude encoded optical codes. Additionally, transparent ONU-to-ONU communication is enabled in the sub-net of PONs with a single central office.

As shown throughout the work, the use of spectral codes gives raise to multiple user interference at the passive coupler of the PON. Essentially, the coherence between the observed state at the network node and the real (future) state at the merging point is evaluated at the packet level, thereby simplifying the analysis. A set of experiments are carried out for a number of realistic scenarios in case of four different packet size distributions and a fixed propagation delay between the network node and the merging point.

In all considered cases, the coherence of state is shown to depend on the packet size distribution and on the sampling rate. Regarding a single active user, the observed and future states are found to be coherent with respect to the transmission distance and memorylessness may be assumed for decreasing sampling rates. Concerning multiple active users, the coherence of state is shown to depend on the packet size distribution when the number of transmitting ONUs is small, but to approach exponential behaviour (memorylessness) as the number of simultaneous ONUs increases.

Additionally, it is shown that the a-priori knowledge of user activity can be exploited, for instance by allowing the ONUs to anticipate and decide whether or not to transmit a packet and, if so, when to schedule its transmission. Such scheduling must take into account the network design parameters, such as

Fig. 10. Comparison when multiple ONUs are transmitting: Exponential (top-left), Pareto (top-right), Gaussian (bottom-left) and Bimodal (bottom-right).
propagation delay and the number of ONUs per merging point. Finally, the mathematical framework introduced in this work sets the grounds for further development of medium access protocols in such transparent optical access architectures.

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Fig. 11. Order statistics assuming $u = 20$. $f_{X_1}$ (top-left); $f_{X_5}$ (top-right); $f_{X_9}$ (bottom-left); and $f_{X_{13}}$ (bottom-right).

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