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Retrieval of tropospheric NO\textsubscript{2} using the MAX-DOAS method combined with relative intensity measurements for aerosol correction

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Abstract. Multi-Axis Differential Optical Absorption Spectroscopy (MAX-DOAS) is a technique to measure trace gas amounts in the lower troposphere from ground-based scattered sunlight observations. MAX-DOAS observations are especially suitable for validation of tropospheric trace gas observations from satellite, since they have a representative range of several kilometers, both in the horizontal and in the vertical dimension.

A two-step retrieval scheme is presented here, to derive aerosol corrected tropospheric NO\textsubscript{2} columns from MAX-DOAS observations. In a first step, boundary layer aerosols, characterized in terms of aerosol optical thickness (AOT), are estimated from relative intensity observations, which are defined as the ratio of the sky radiance at elevation $\alpha$ and the sky radiance in the zenith. Relative intensity measurements have the advantage of a strong dependence on boundary layer AOT and almost no dependence on boundary layer height. In a second step, tropospheric NO\textsubscript{2} columns are derived from differential slant columns, based on AOT-dependent air mass factors.

This two-step retrieval scheme was applied to cloud free periods in a twelve month data set of observations in De Bilt, The Netherlands. In a comparison with AERONET (Cabauw site) a mean difference in AOT (AERONET minus MAX-DOAS) of $-0.01 \pm 0.08$ was found, and a correlation of 0.85. Tropospheric-NO\textsubscript{2} columns were compared with OMI-satellite tropospheric NO\textsubscript{2}. For ground-based observations restricted to uncertainties below 10%, no significant difference was found, and a correlation of 0.88.

1 Introduction

1.1 Validation of satellite NO\textsubscript{2}

Tropospheric nitrogen dioxide (NO\textsubscript{2}) plays an important role in atmospheric chemistry. It is involved in many chemical cycles such as in the formation of tropospheric ozone, which is toxic to humans. High concentrations of NO\textsubscript{2} often indicate high levels of air pollution in general.

The trace gas NO\textsubscript{2} is monitored in various ways. Primarily by surface in situ monitoring stations all over the world, but since the last decade also from space. Space borne observations of NO\textsubscript{2} form the basis for studies of regional and global trends, global transport and chemical cycles (e.g. Richter et al., 2005; van der A et al., 2006; Blond et al., 2007, and Boersma et al., 2008). In addition, satellite observations of tropospheric NO\textsubscript{2} are essential for validation of atmospheric chemical transport models and top-down construction of emission data bases (e.g. Martin et al., 2003; Mijling et al., 2009).

Despite the many results of observations from space, there is still a great demand for independent, quantitative validation of the NO\textsubscript{2} retrievals (Brinksma et al., 2008; Irie et al., 2008b; Hains et al., 2010). Validation should be performed under various atmospheric conditions and in different parts of the world, since it is known that clouds, aerosols, surface albedo, surface altitude, trace gas profile and other parameters all have significant impact on the satellite retrievals (e.g. Boersma et al., 2004; Zhou et al., 2009).

Whereas satellite validation of ozone retrievals is often done by comparison with ozone-sondes, there is not yet an equivalent in situ profiling measurement for NO\textsubscript{2}. Comparing to in situ surface monitors is problematic due to the large difference in spatial representativeness of the two observation techniques: In situ surface monitors have a local character (e.g. street level), whereas even the smallest pixels of...
current trace gas monitoring satellite instruments have sizes of several hundreds of square kilometers. Although rural stations are representative for larger regions (Blond et al., 2007), comparison with satellite observations requires strong assumptions on the vertical distribution of NO\textsubscript{2}.

1.2 MAX-DOAS method

The Multi-Axis Differential Optical Absorption Spectroscopy (MAX-DOAS) method (e.g. Wagner et al., 2004; Höninger et al., 2004; Wittrock et al., 2004; Sinreich et al., 2005; Friess et al., 2006; Leigh et al., 2007; Irie et al., 2008a) offers an alternative in this respect, since it has a much larger spatial representativeness than in situ surface monitors. MAX-DOAS instruments observe scattered solar radiation from the surface – in the UV and/or Visible – at a spectral resolution of typically 0.5 nm in multiple viewing directions (see Fig. 1). Small elevations have a relatively high sensitivity to the lower troposphere, since detected photons at small elevations have longer paths through these layers than photons observed at larger elevations. Radiative transfer simulations at 428 nm show that the horizontal representative range is about 5 to 10 km, whereas the vertical range is about 1 to 4 km. Both ranges are wavelength dependent. The horizontal and vertical range also have a strong dependence on elevation, see e.g. Wittrock et al. (2004) and Pikelnaya et al. (2007). The increased sensitivity to the lower troposphere also distinguishes the MAX-DOAS technique from other ground-based passive DOAS techniques, such as direct-sun DOAS (total column NO\textsubscript{2}, see e.g. Herman et al., 2009), and zenith sky DOAS (stratospheric NO\textsubscript{2}, see e.g. Melo et al., 2005).

The various DOAS techniques (see Platt and Stutz, 2008, for an extensive overview) have in common that the analysis of spectral measurements of atmospheric radiation is based on the DOAS equation:

\[
\ln \left( \frac{I(\lambda)}{I_{ref}(\lambda)} \right) = - \sum_{i=1}^{n} \Delta \sigma_i(\lambda) \Delta N^i_T + P(\lambda). \quad (1)
\]

In this equation \(n\) differential cross-section spectra \(\Delta \sigma_i(\lambda)\) and a low-order polynomial \(P(\lambda)\) are fitted to the natural logarithm of the ratio of two atmospheric spectra \(I(\lambda)\). A differential cross-section uniquely characterizes a trace gas and is obtained by subtracting a low-order polynomial from the cross-section. The two atmospheric spectra in the DOAS equation correspond to two different viewing directions, or times of observation, or both, depending on the specific DOAS application.

The fitting procedure yields a so-called differential slant column (density) \(\Delta N^S\) in [molecules/cm\textsuperscript{2}] for each trace gas. The differential slant column represents the difference in trace gas absorption along the two light paths corresponding to the atmospheric spectra. In the case of MAX-DOAS, it is custom to combine a zenith spectrum with a spectrum corresponding to another, preferably small, elevation \(\alpha\), since photons detected at small elevation have the largest path length difference with photons detected at the zenith, and this combination thus gives a high sensitivity to the lower troposphere.

In this study, MAX-DOAS observations are used for the retrieval of tropospheric columns of NO\textsubscript{2}. To convert a differential slant column to a corresponding tropospheric vertical column \(N^T\), a so called differential air mass factor \(\Delta M\) is required. This factor is a function of the elevation \(\alpha\) – and to a lesser extent of many other parameters – and is defined here as the ratio of the differential slant column density and the tropospheric column density of NO\textsubscript{2}:

\[
\Delta M_\alpha = \frac{\Delta N^S_\alpha}{N^T}. \quad (2)
\]

The simplest calculation of MAX-DOAS differential air mass factors has become known as the geometrical approximation (Höninger et al., 2004). The geometrical approximation is not based on radiative transfer simulations, but assumes that the last scattering altitude of photons detected at the surface is below the stratosphere and above the tropospheric layer of a trace gas. This assumption leads to the following relation:

\[
\Delta M_\alpha = \frac{1 - \sin(\alpha)}{\sin(\alpha)}. \quad (3)
\]
Although the geometrical approximation is known to be inaccurate for small elevations (see e.g. Wittrock et al., 2004; Pinardi et al., 2008), this approximation is believed to give an acceptable first estimate of the tropospheric column if applied to a relatively large elevation, such as 30°. The geometrical approximation is used in e.g. Brinksma et al. (2008), Hains et al. (2010) and Wagner et al. (2010).

To exploit the high sensitivity of the MAX-DOAS technique at small elevations, it is desirable to have appropriate differential air mass factors for these viewing directions. This requires a more sophisticated description of the radiative transfer than the geometrical approximation. Since photon paths through the atmosphere are affected by aerosols, it is essential to take the effect of aerosols on the differential slant columns into account.

Recently developed algorithms to estimate aerosol extinction profiles from MAX-DOAS observations, often depend on MAX-DOAS measurements of O\textsubscript{4} absorption (see e.g. Wagner et al., 2004; Sinreich et al., 2005; Friess et al., 2006; Irie et al., 2008a; Clémer et al., 2010). Absorption measurements of the collision complex of oxygen molecules, O\textsubscript{4}, can be related via inverse modeling to the aerosol extinction profile, since O\textsubscript{4} absorption depends on the photon path length through the atmosphere on which aerosols have significant impact. The profile shape of O\textsubscript{4} is well-known, it has the shape of the squared pressure profile.

1.3 This paper

In this study, we propose a simple algorithm for a first order aerosol correction on the differential air mass factors as an alternative to the full combined retrieval of NO\textsubscript{2} and aerosol extinction profiles based on both O\textsubscript{4} and NO\textsubscript{2} differential slant column observations. In our algorithm, aerosol characterization, in terms of aerosol optical thickness (AOT), is based on relative intensity measurements. Relative intensity observations are defined as the ratio of the sky radiance at elevation \( \alpha \) and the sky radiance in the zenith, and they have the advantage of a strong dependence on boundary layer AOT and almost no dependence on boundary layer height (Sect. 3.2). This characteristic of relative intensity observations distinguishes it from O\textsubscript{4} differential slant column measurements.

The structure of this paper is as follows: first a short description of the instrument is given, together with a characterization of the field-of-view and slit function (Sect. 2). Also the set-up of the instrument is described, the correction of measured spectra and the settings of the DOAS fit. Radiative transfer modeling of relative intensities and differential air mass factors is described in Sect. 3. A sensitivity study is performed, and error sources are discussed. Results of application of the algorithm to selected days are given in the Sect. 4. Furthermore the applicability of the geometric approximation is discussed, based on both model simulations and observations. Finally a verification of the aerosol optical thickness retrieval with AERONET data is shown, and a comparison with tropospheric NO\textsubscript{2} from the Ozone Monitoring Instrument (OMI).

2 Measurements

2.1 Mini MAX-DOAS instrument

The observations in this study were made with a so-called Mini MAX-DOAS instrument (e.g. Hönninger et al., 2004; Bobrowski, 2005) produced by Hoffmann GmbH, Germany. This relatively small MAX-DOAS instrument consists essentially of a lens, optical fiber and UV/VIS spectrometer, all contained in one metal box that is mounted on a pointing mechanism (stepper motor). The instrument is designed to operate in the open air for long periods in an automated fashion. Stabilizing the temperature by cooling is made possible by a Peltier element, which cools up to 25 °C below ambient. Incoming light is focused by a lens (\( f = 40 \text{ mm} \)) on the entrance of an optical fiber which is connected to the Ocean Optics “USB2000” crossed Czerny-Turner type spectrometer with a Sony “ILX511” CCD detector (2048 pixels). The wavelength range of the instrument is 290 to 433 nm.

Measurements with a monochromatic light source (Mercury lamp) were performed (see Fig. 2). These measurements indicated that the line shape (slit function) is asymmetric, and has a FWHM of 0.6 nm at around 408 nm. The line shape shows some temperature dependence at this wavelength, which is not far from the spectral fitting window for NO\textsubscript{2} (Sect. 2.3.2).

Furthermore, the field-of-view (FOV) of the instrument was characterized (see Figs. 3 and 4). Measurements with a distant light source (ø 2.0 mm at 5 m) and a digital level indicated that the FWHM of the FOV was around 0.45°. The pointing offset was determined from the same experiment. This pointing offset is defined as the angle between the top
plane of the instrument and the horizontal plane, when the instrument is rotated such that it has maximum signal from a distant light source that is at the same height as the lens of the instrument. The pointing offset was measured each time after the instrument box was opened for maintenance and showed substantial variations (e.g. one occasion with a change from $-2.0^\circ$ to $+0.4^\circ$) due to small displacements of the fiber entrance. The experiment was repeated including a black tube in front of the lens (not drawn), which is used normally to block stray light. Adding the tube did not change the results. The pointing offset was taken into account each time the instrument was started. The pointing of the instrument was checked on a weekly basis.

### 2.2 Operations

Observations were performed from the roof of the KNMI building in De Bilt, The Netherlands (52.101° N, 5.178° E), from 14 November 2007 until 29 April 2008 and from 11 September 2008 until 21 April 2009, with some days missing due to technical circumstances, resulting in 362 days of observations in total. The azimuth position of the instrument was fixed towards the North-East (at $46^\circ$ azimuth from North). This direction was chosen for practical purposes due to technical circumstances, resulting in 362 days of observations in total. The azimuth position of the instrument was fixed towards the North-East (at $46^\circ$ azimuth relative to North). This direction was chosen for practical purposes (constraints at small elevations by trees and buildings surrounding the measurement site), and to look away from the sun for most of the day throughout the year, which is advantageous with respect to the sensitivity of the retrievals to estimated fixed parameters. Spectra were recorded at 0°, 2°, 4°, 8°, 16°, 30° and 90° elevation angles. Automated operation of the instrument was done with the DOASIS software developed by IUP Heidelberg in cooperation with Hoffmann GmbH. The integration time for each elevation was set to 30 s divided into multiple shorter scans to prevent the detector from saturation.

### 2.3 DOAS analysis of spectra

#### 2.3.1 Correction of spectra

Spectra were corrected for a CCD read-out offset. This read-out offset (or electronic offset, EO) is temperature-dependent and proportional to the number of sub-spectra that are read-out, added and stored as one spectrum. Since the instrument does not have a shutter, it was not possible to do EO and dark current measurements as a part of regular operations.

EO measurements were performed at different temperatures by reading out many spectra with minimum integration time under complete dark conditions (e.g. 1000 read-outs at 3 ms, which is the minimal read-out time of the spectrometer). These measurements demonstrated that the EO was almost constant over the whole detector range except for the first ten pixels. Since the first hundred pixels of the detector are in the far UV (below 297 nm) they are virtually blind even under atmospheric measuring conditions. A more detailed analysis showed that pixels 60–80 had an EO level that was within one percent of the offset level in the fitting window used in this study. For this reason the EO correction of each spectrum was based on an average of these pixels. An advantage of this approach is that this EO correction is less sensitive to (unknown) instabilities in the actual temperature of the instrument than if the EO correction would be based on the registered operation temperature, and an EO-temperature calibration done at another time.

It was decided not to apply a dark current (DC) correction. The DC correction depends on temperature, integration time (of each individual sub-scan) and typically shows a strong pixel to pixel variation. It requires a thermally very stable instrument to be able to correct measured spectra based on laboratory measured DC. The instrument was not expected to be thermally stable to such a high degree for the whole period of operation. The effect of applying an inappropriate dark current correction is comparable to applying no correction. Not applying the dark current correction in the DOAS NO$_2$ fit will in general lead to somewhat larger fit residuals but not to systematic biases. Tests on temperature-controlled measurements, under representative measurement conditions, have shown that differences between including and not including DC-correction was less than 0.1% in the fitted NO$_2$ differential slant column. A possible explanation for this small effect is that the integration time for individual acquisitions was generally small (of the order of 1 s or less), resulting in a low DC, and that the EO correction described here also includes a correction for the average DC. Only the pixel-to-pixel variations on top of this average DC are not accounted for. For other trace gases with smaller tropospheric column amounts the effect of not correcting for DC will be larger.

#### 2.3.2 DOAS fitting

DOAS-fitting was performed with the “Qdoas” software developed at the Belgian Institute for Space and Aeronomy (IASB/BIRA) (Fayt and Van Roozendael, 2001). For each spectrum at elevation $\alpha$, the nearest (in time) zenith spectrum

---

**Fig. 3.** Set-up of the field-of-view characterization experiment with a light source in the distance. The angle $\alpha$ denotes the rotation in the vertical plane relative to a horizontal starting position of 0°. At this starting position the light source was at the same height above the table as the lens. The experiment was repeated including a black tube in front of the lens (not drawn), which is used normally to block stray light. Adding the tube did not change the results.
2.4 Relative intensity observations

The observation of relative intensity of skylight is another method to derive information on atmospheric constituents from the MAX-DOAS instrument. Intensity of skylight, $I$, is measured here as the MAX-DOAS detector signal, corrected for electronic-offset (see Sect. 2.3), averaged over a certain spectral interval in one viewing direction. Only relative values of intensity can be compared to their simulated counterparts, since the instrument is not radiometrically calibrated. In this work relative intensity, $I^\text{rel}_\alpha$, refers to the ratio of the intensity in direction $\alpha$ to the intensity in the zenith direction, where the nearest (in time) zenith spectrum is used:

$$I^\text{rel}_\alpha = \frac{I_\alpha}{I_{90}}$$

The wavelength interval used for $I^\text{rel}_\alpha$ was 426–429 nm, which is within the NO$_2$ DOAS fitting window, and contains the wavelength chosen for the differential air mass factor calculation (Sect. 3.1.3). In the absence of clouds, relative intensities in the visible are mainly influenced by Rayleigh scattering and aerosol scattering and absorption. Since Rayleigh scattering is accurately known, relative intensity observations contain information on aerosols, as will be shown in Sect. 3.2.

3 Retrieval algorithm

A two step approach is used to derive tropospheric vertical columns of NO$_2$ from MAX-DOAS differential slant column observations, see Fig. 5. The first step is to estimate aerosol optical thickness from relative intensity observations. This is done by interpolation of the observed relative intensity for a particular elevation and solar position (zenith and azimuth) on look-up table values of simulated relative intensity as a function of boundary layer AOT. Here it is assumed that both aerosols and tropospheric NO$_2$ are homogeneously distributed in the boundary layer. The second step is to use this estimated AOT in another look-up table containing the NO$_2$ differential air mass factors for each elevation and solar position as a function of AOT.

By this method, the AOT and the tropospheric vertical column of NO$_2$ ($N^\text{Tr}_\alpha$) are derived for each elevation independent of observations in the other elevations. A final NO$_2$ tropospheric vertical column ($N^\text{Tr}$) is found by averaging over the elevations $4^\circ$, $8^\circ$ and $16^\circ$:

$$N^\text{Tr} = \frac{N^\text{Tr}_4 + N^\text{Tr}_8 + N^\text{Tr}_{16}}{3}.$$

Smaller elevations were not used for several reasons. Firstly, because inhomogeneities in the distribution of aerosols and NO$_2$ in the boundary layer, which are not included in the forward radiative transfer modeling, will have a larger effect at smaller elevations and therefore lead to larger uncertainties in the retrieval. Secondly, because small misalignments
will also have the largest effect for the smallest elevations. Thirdly, because the effect of the curvature of the Earth is not captured by the radiative transfer model, which will only have a noticeable effect in the VIS, for small elevations under very clear conditions (see also Sect. 3.1.1). Larger elevations were not used because the signal-to-noise ratio of the measured differential slant column densities for this elevation was too low, namely often well below 5. This was due to the relative short integration time of 30 s, and the relative low sensitivity of the larger elevations.

As an estimate of the uncertainty on the retrieved average NO$_2$ tropospheric column we use the difference between the maximum and minimum NO$_2$ tropospheric column that is retrieved for 4°, 8° and 16° elevation (see Sect. 3.3).

### 3.1 Radiative transfer modeling

A multiple scattering radiative transfer model was used in this study for two purposes. Firstly to derive the look-up tables that relate relative intensity and differential air mass factors to boundary layer AOT. Those look-up tables are used in the retrieval algorithm. Secondly, to study the sensitivity of relative intensities and differential air mass factors to several parameters that cannot be retrieved and for which fixed (climatological) values are assumed.

The radiative transfer model used in this study is DAK (Doubling-Adding KNMI). The DAK model is based on the doubling-adding algorithm for multiple scattering of sunlight in a vertically inhomogeneous atmosphere with polarization included (De Haan et al., 1987; Stammes et al., 1989). In the doubling-adding method, one starts with an optically thin layer for which the analytical solution for single and double scattering suffices to describe the radiation field. Next, subsequent doubling of this optically thin layer to an optically thick homogeneous layer, and adding different homogeneous layers together leads to a multi-layered atmosphere in which the reflected, transmitted, and internal radiation fields are calculated. In each layer, the extinction optical thickness, single scattering albedo and phase matrix (or phase function for unpolarized light) have to be prescribed. These atmospheric input parameters are calculated from temperature, pressure, trace gas mixing ratio, and aerosol profiles (Stammes, 2001). The inclusion of polarization in computing the radiation fields is especially important in the UV and blue parts of the solar spectrum, where atmospheric Rayleigh scattering is dominating.

#### 3.1.1 Comparison with other radiative transfer models

The DAK model was compared to the results of the model intercomparison of Wagner et al. (2007), where a comparison of nine radiative transfer models was reported with special focus on box-air mass factors for MAX-DOAS viewing geometries. In general a good agreement was found between DAK and the models included in the comparison. A deviation from the spherical models was found only for box air mass factors in the Rayleigh atmosphere (no aerosols) at 577 nm and 2 degrees elevation (Fig. 8 from Wagner et al.,...
This deviation at 577 nm was consistent with the other plane parallel models. The same comparison at 360 nm showed no difference between spherical and plane-parallel models.

Based on this comparison it was concluded that the DAK simulations could be applied to the MAX-DOAS observations at around 425 nm for elevations of 4 degrees and above.

### 3.1.2 Parameter settings

In the algorithm and radiative transfer model, several parameters were assumed fixed. These are also the standard settings in the sensitivity study of Sect. 3.2. These parameters are:

(a) Block functions to describe the aerosol extinction profile and NO\textsubscript{2} profile in the planetary boundary layer (layer height: 1.0 km); (b) US-standard mid-latitude summer profiles for temperature and pressure at all heights and for NO\textsubscript{2} above 5 km; (c) NO\textsubscript{2} tropospheric vertical column is 2x10\textsuperscript{16} molecules/cm\textsuperscript{2}; (d) Aerosol characterization: single scattering albedo is 0.92, asymmetry parameter is 0.70, Henyey-Greenstein phase function; (e) Surface albedo is 0.06; (f) Effect of linear polarization is included. The choice for this single scattering albedo and asymmetry parameter was based on AERONET observations from the Cabauw site (22 km from instrument location), for fourteen blue sky days in the years 2007–2009 throughout the various seasons.

### 3.1.3 Calculation of differential AMF

The differential air mass factor was calculated for one effective wavelength (428.22 nm), and this differential AMF was assumed to be representative for the whole fitting window 415–431 nm. Assumptions with respect to the model atmosphere for which differential AMFs and relative intensities were calculated, are described in the previous section.

The differential air mass factor was calculated in a way that is somewhat different from (A) the traditional method (see Platt and Stutz, 2008), and (B) the box-AMF method (see e.g. Hönninger et al., 2004; Wagner et al., 2007), two methods that can be applied to simulations at a single wavelength. In the case of the traditional method, the AMF is derived from two radiative transfer simulations: one for an atmosphere excluding NO\textsubscript{2}, and another one for an atmosphere including NO\textsubscript{2}, assuming a specific vertical distribution of NO\textsubscript{2}. In the case of the box-AMF method (B), NO\textsubscript{2} is added and removed to the simulated atmosphere, but here only in thin vertical layers, one at a time. For both (A) and (B) the differential AMF (\(\Delta M_\alpha\)) for an elevation is found by subtracting from its AMF (\(M_\alpha\)) the zenith-AMF (\(M_{90}\)).

In our study an approach is followed which is numerically equivalent to the traditional method within one percent. It was chosen because it closely resembles the MAX-DOAS method, where differential slant columns are derived directly from spectra in two viewing directions: one spectrum measured at elevation \(\alpha\) and one zenith reference spectrum. Radiative transfer calculations were performed for just one atmosphere, including an assumed NO\textsubscript{2} vertical profile. Three wavelengths (426.48, 428.22 and 429.86 nm) were used to be able to subtract a background absorption spectrum, which also includes the low-pass filtered (or broad band) absorption by NO\textsubscript{2}. In this way, a simulated differential slant column can be derived from the ratio of the differential absorption slant optical thickness to the differential cross-section of NO\textsubscript{2}. The three wavelengths were chosen such that they were close together, at local maximum and minima of the NO\textsubscript{2} cross-sections, and within the DOAS spectral fitting window in which the measurements are analyzed (see Fig. 6).

The derivation of the differential AMF is as follows. We assume that the light paths in the atmosphere are not changed when adding a relatively weak absorber like NO\textsubscript{2}. The sky radiance for elevation \(\alpha\) and wavelength \(\lambda\) with NO\textsubscript{2} in the atmosphere \(I_\alpha(\lambda)\) is equal to the sky radiance without NO\textsubscript{2} \(I_\alpha^0(\lambda)\) times an attenuation term depending on the NO\textsubscript{2} slant column for this elevation \(N_\alpha^S\), and the NO\textsubscript{2} absorption cross-section \(\sigma(\lambda)\) at this wavelength:

\[
I_\alpha(\lambda) = I_\alpha^0(\lambda) e^{-N_\alpha^S \sigma(\lambda)},
\]

also known as the law of Bouguer-Lambert-Beer. Taking the natural logarithm of the ratio of the radiances at elevation \(\alpha\) and the zenith (\(\alpha = 90^0\)), and writing:

\[
R_\alpha(\lambda) = \ln \left[ \frac{I_\alpha^0(\lambda)}{I_{90^0}^0(\lambda)} \right],
\]

and

\[
\Delta N_\alpha^S = N_\alpha^S - N_{90^0}^S,
\]

leads to:

\[
R_\alpha(\lambda) = R_\alpha^0(\lambda) - \Delta N_\alpha^S \sigma(\lambda).
\]

This equation may be written for the three wavelengths \(\lambda_1 = 426.48\) nm, \(\lambda_2 = 428.22\) nm and \(\lambda_3 = 429.86\) nm. \(R_\alpha^0\) and \(\sigma\) can be interpolated to \(\lambda_2\), using the values at \(\lambda_1\) and \(\lambda_3\), which leads to a second equation defined at \(\lambda_2\). The two equations at \(\lambda_2\) are:

\[
R_\alpha(\lambda_2) = R_\alpha^0(\lambda_2) - \Delta N_\alpha^S \sigma(\lambda_2),
\]

and

\[
R_\alpha^* (\lambda_2) = R_\alpha^{0*} (\lambda_2) - \Delta N_\alpha^S \sigma^* (\lambda_2),
\]

where the * refers to the interpolated values at \(\lambda_2\). Now we assume that in this short interval, \(R_\alpha^0\) can be approximated by a linear function, since it is not affected – in the model atmosphere – by absorbers with a fine-scale structure. Consequently:

\[
R_\alpha^{0*} (\lambda_2) = R_\alpha^0 (\lambda_2).
\]
Table 1. Sensitivity study of eight parameters affecting tropospheric NO\textsubscript{2} retrieval: AOT, boundary layer height for NO\textsubscript{2} and aerosols (BLH), boundary layer column of NO\textsubscript{2} (N), asymmetry parameter of aerosols (ASY), single scattering albedo of aerosols (SSA), surface albedo (ALB), and polarization (POL). Each parameter was changed in the DAK model from case 1 (reference value) to case 2, with all other parameters unchanged. For the elevations 4\degree, 8\degree and 16\degree, the effect of this change is given in percent for the relative intensity ($I_{rel}$), the differential air mass factor ($\Delta M$), and for the tropospheric NO\textsubscript{2} column retrieved by the two-step algorithm ($N_a^{Tr}$). The percentage was calculated as follows: $(P_{(case\ 1)}-P_{(case\ 2)})/P_{(case\ 2)}\times 100\%$, where, for each line, $P_{(case\ 2)}$ is the model simulation where only the quantity indicated by the first column of that line was changed to case 2, and where all other parameters were as in case 1. The values in the table therefore represent the error made when the ‘true’ atmosphere would be in a state with one specific parameter as in case 2, whereas this and all other parameters are assumed to be as in case 1 (which corresponds to the settings of the look-up tables described in Sect. 3.1.2). Values were calculated for a solar zenith angle of 60\degree and a relative azimuth of 180\degree.

<table>
<thead>
<tr>
<th>param.</th>
<th>case 1</th>
<th>case 2</th>
<th>$\alpha=4\degree$ change (%) in:</th>
<th>$\alpha=8\degree$ change (%) in:</th>
<th>$\alpha=16\degree$ change (%) in:</th>
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<td>$\Delta M$</td>
<td>$N_a^{Tr}$</td>
<td>$I_{rel}$</td>
<td>$\Delta M$</td>
</tr>
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<td>55</td>
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</tr>
<tr>
<td>BLH NO\textsubscript{2} [km]</td>
<td>1.0</td>
<td>1.5</td>
<td>-6.5</td>
<td>6.1</td>
<td>-9.7</td>
</tr>
<tr>
<td>BLH aer.&amp;NO\textsubscript{2} [km]</td>
<td>1.0</td>
<td>1.5</td>
<td>-1.3</td>
<td>23</td>
<td>-19</td>
</tr>
<tr>
<td>$N$ [10\textsuperscript{15} molec/cm$^2$]</td>
<td>20</td>
<td>2</td>
<td>-5.7</td>
<td>0.1</td>
<td>-3.8</td>
</tr>
<tr>
<td>ASY</td>
<td>0.70</td>
<td>0.75</td>
<td>-4.8</td>
<td>-3.7</td>
<td>0.15</td>
</tr>
<tr>
<td>SSA</td>
<td>0.92</td>
<td>0.95</td>
<td>-2.1</td>
<td>-0.2</td>
<td>-1.3</td>
</tr>
<tr>
<td>ALB</td>
<td>0.06</td>
<td>0.03</td>
<td>2.7</td>
<td>-0.5</td>
<td>3.2</td>
</tr>
<tr>
<td>POL</td>
<td>on</td>
<td>off</td>
<td>2.4</td>
<td>0.5</td>
<td>1.9</td>
</tr>
</tbody>
</table>

If we define
\[
\Delta R_a (\lambda_2) = R_a (\lambda_2) - R_a^0 (\lambda_2),
\]
and
\[
\Delta \sigma (\lambda_2) = \sigma^0 (\lambda_2) - \sigma (\lambda_2),
\]
(see Fig. 6), take the difference of Eqs. (10) and (11), and make use of Eq. (2), we find the following expression for the differential air mass factor ($\Delta M_a$) at elevation $\alpha$:
\[
\Delta M_a (\lambda_2) = \frac{\Delta R_a (\lambda_2)}{N_a^{Tr} \Delta \sigma (\lambda_2)}.
\]

Note from this equation that the differential AMF is calculated only from radiative transfer simulations including NO\textsubscript{2}, at three wavelengths, in contrast to the other methods mentioned at the beginning of this section, where simulations excluding NO\textsubscript{2} are needed as well, but only at a single wavelength.

3.2 Sensitivity study

A sensitivity study was performed to quantify the effect of variations in several parameters on the differential air mass factors, relative intensities and the combined steps in the algorithm that lead to the retrieved tropospheric NO\textsubscript{2} column. These parameters were: boundary layer height, tropospheric NO\textsubscript{2} vertical column, aerosol optical thickness, asymmetry parameter, single scattering albedo, surface albedo and polarization. In each DAK model run only one parameter was changed with respect to the standard settings described in Sect. 3.1.2. The range of the variation of each parameter is given by columns case 1 and case 2 in Table 1.

The first column of each elevation (4\degree, 8\degree, 16\degree) in this table gives the sensitivity of the relative intensity to a parameter change from case 1 to case 2 (where all other parameters do not change), and each second column gives the sensitivity...
of the differential air mass factor. The third column of each elevation shows the sensitivity of the retrieved tropospheric NO$_2$ column for that elevation.

Table 1 shows that both the relative intensity and the differential AMF are most sensitive to the amount of boundary layer aerosols, as seen by the effect of a change in the aerosol optical thickness. The retrieval of tropospheric NO$_2$ columns however, is insensitive to a change in AOT, since the algorithm is designed to correct for this change. Figure 7 shows the effect of the AOT on relative intensity and differential AMF in more detail.

The sensitivity to a simultaneous change of both the NO$_2$ and aerosol vertical block profiles is given in the second line of Table 1. This shows that relative intensity observations – and thus the AOT retrieval – are quite insensitive to a change in boundary layer height, when compared with the sensitivity to a change in AOT (first line). However, the combined effect of relative intensity and differential AMF leads to a relatively large change in the tropospheric NO$_2$ column, especially for 4° elevation. If only the NO$_2$ vertical block profile is changed with respect to the reference situation (third line), then there is a larger change of the differential AMF and the retrieved tropospheric NO$_2$ column. This underlines that knowledge of the NO$_2$ profile shape is crucial to have an accurate tropospheric NO$_2$ column retrieval.

Measured differential slant columns are influenced not only by the vertical profile shape of NO$_2$, but also by the vertical sensitivity to NO$_2$. A useful quantity to describe the sensitivity to NO$_2$ at various altitudes is the height-dependent air mass factor, a quantity that is also referred to as (differential) box-AMF (see e.g. Höninger et al., 2004; Wagner et al., 2007). The height-dependent differential AMF ($\Delta m_\alpha (z)$) at height $z$ for elevation $\alpha$, was calculated by perturbing the background NO$_2$ profile at height $z$:

$$\Delta m_\alpha (z) = \frac{[\Delta N^\alpha]^z - [N^\alpha]^z - [\Delta N^\alpha]^\text{ref} - [N^\alpha]^\text{ref}}{[N^\alpha]^z - [\Delta N^\alpha]^\text{ref} - [N^\alpha]^\text{ref}},$$

where the superscript “ref” refers to a simulation for a background NO$_2$ profile, and the superscript $z+$ refers to a simulation where NO$_2$ is added to the background profile at height $z$.

Figure 8 shows the differential box-AMF for different elevations and for two values of the AOT (see also Wittrock et al., 2004, and Pikelnaya et al., 2007, for similar results obtained with different radiative transfer models). The low elevations have a sensitivity to NO$_2$ that decreases rapidly with height, whereas the vertical sensitivity of the higher elevations is more constant. Increasing the amount of aerosols in the boundary layer leads, for the low elevations, to a pronounced decrease in sensitivity to NO$_2$ with increasing altitude.

Figure 9 shows the dependence of relative intensity on boundary layer height and aerosol optical thickness, for two elevations (4° and 30°). The relatively weak sensitivity of relative intensity to a change in boundary layer height, is the reason that relative intensity observations are more suitable for boundary layer aerosol optical thickness estimations than measurements of O$_4$, but only in the absence of clouds. A relative intensity observation of only a single elevation is needed to estimate the aerosol optical thickness. O$_4$ observations on the other hand, contain more information on the aerosol profile, which is the reason why they are used in MAX-DOAS aerosol extinction profile retrievals (Friess et al., 2006; Irie et al., 2008a; Clémer et al., 2010).
Fig. 8. Radiative transfer simulations with the DAK model of height-dependent differential AMF (differential box-AMF) for AOT = 0.2 (left) and AOT = 0.6 (right), at 428.22 nm. Settings in the simulations: boundary layer height for aerosols (block profile): 1.0 km, solar zenith angle = 60°, relative azimuth angle = 180°, $\lambda$ = 428 nm.

From the fourth line in Table 1 it appears that there is an unwanted dependence of the algorithm to the tropospheric NO$_2$ column itself. This can be solved by making the algorithm iterative, with the tropospheric NO$_2$ column as an additional dimension of the look-up table, but this step was not applied in this study.

Finally, Table 1 shows that the asymmetry parameter, single scattering albedo, surface albedo and polarization have a relatively small effect on the retrieved tropospheric NO$_2$ column.

Table 1 was calculated for a relative azimuth of 180° and a solar zenith angle of 60°. Additional studies showed that the values in the table are representative for other solar positions except when the instrument is viewing in a direction close to the sun (either in viewing direction $\alpha$, or in the zenith direction) where simulated quantities depend more critically on the aerosol model parameters. Since the Mini MAX-DOAS instrument was pointed towards the North-East, the sun was at relatively large angular distance for most of the time.

### 3.3 Error sources

There are many possible sources of error in the retrieval of NO$_2$ tropospheric columns from MAX-DOAS observations. Two types of error may be distinguished: observational errors and modeling errors. The term observational error is used here for all factors leading to an incorrect value for the differential slant column and/or relative intensity.

Systematic error contributions to the observational error are: (1) errors caused by incorrect knowledge of the actual field-of-view, which may be caused by incorrect aiming of the instrument (e.g. when it is unattended after periods of heavy winds) or by imprecise knowledge of the offset in the field-of-view as described in Sect. 2.1, (2) incorrect electronic offset correction of raw spectra, (3) errors in the differential cross-sections of NO$_2$ (e.g. temperature dependency), (4) errors due to the use of a semi-simultaneous reference spectrum (see Sect. 2.3.2). The DOAS spectral-fitting error represents a mixture of systematic and random errors: incorrect wavelength calibration of spectra, inaccurate knowledge of instrument slit function, incorrect dark current correction, unknown absorbers, and low signal-to-noise.

The DOAS fitting was performed with a cross section at a fixed temperature (see Sect. 2.3.2). This introduces an error in the differential slant column of NO$_2$ that is proportional to the temperature difference between the fixed temperature of the cross section used in the fit and the effective temperature of the tropospheric NO$_2$. Although the NO$_2$ cross section $\sigma_{\text{NO}_2}$ itself is not strongly temperature dependent, the differential cross section $\Delta \sigma_{\text{NO}_2}$ shows a much stronger temperature dependence: a change in temperature of 20 degrees corresponds to a change in $\sigma_{\text{NO}_2}$ of 1.6% and to a change in $\Delta \sigma_{\text{NO}_2}$ of 7.2%. An estimate of the effective NO$_2$ temperature is needed to correct for this effect (see Sect. 4.4).

The modeling errors that affect the differential AMF are introduced in two ways: first by not including parameters in the radiative transfer modeling that do have an effect on the observations, and second by choosing inappropriate values for parameters that are included in the model. Some examples of parameters that were not included in the model are: humidity, clouds, horizontal gradients in all parameters of which a vertical profile is prescribed, and vertical profile shapes other than those described in Sect. 3.1.2.
The effect of inaccurate estimation of the included model parameters was studied in Sect. 3.2. The algorithm described in this study is most sensitive to the boundary layer height, especially to the vertical profile shape of NO$_2$. This is a consequence of the decrease in sensitivity to NO$_2$ with increasing height, especially for low elevations (see e.g. Wittrock et al., 2004, their Fig. 4).

In this study, we estimate the uncertainty $\varepsilon$ on the retrieved average NO$_2$ tropospheric column (Eq. 5) as the difference between the maximum and minimum NO$_2$ tropospheric column that is retrieved for $4^\circ$, $8^\circ$ and $16^\circ$ elevation:

$$
\varepsilon = \max(N^{\text{TR}}_{[4^\circ, 8^\circ, 16^\circ]}) - \min(N^{\text{TR}}_{[4^\circ, 8^\circ, 16^\circ]}),
$$

where the three tropospheric columns are interpolated to the same point in time. Since the tropospheric columns are derived for each elevation independent of the others, this difference, or spread, gives an important indication of the internal consistency of the retrieval. A small spread indicates a consistent retrieval. The spread increases for measurement conditions that differ from the model atmosphere in the look-up table calculations. For instance, an error in the assumed boundary layer height would lead to different systematic errors in the retrieved tropospheric NO$_2$ columns for each elevation angle (see Table 1). This would result in a systematic error in the derived average tropospheric NO$_2$ column and an increase in the spread. The definition of the measurement uncertainty includes effects such as: presence of clouds, pointing elevation offsets, horizontal gradients, vertical profile shape of aerosols and NO$_2$, and uncertainty due to a low signal-to-noise.

Since the boundary layer height may well be the parameter with the largest contribution to the uncertainty $\varepsilon$ in the tropospheric NO$_2$ column retrieval (see Table 1), the two-step algorithm could be modified by including the boundary layer height as a free parameter, changing it iteratively, by minimizing $\varepsilon$. However it was decided in this work not to apply this additional step, as the boundary layer height is not the only parameter affecting $\varepsilon$, as described above.

Typical values of $\varepsilon$ are on average much lower for clear sky than for cloudy conditions (see Sect. 4.1). If data is selected for clear sky conditions, using the criterion that the relative intensity of $4^\circ$, $8^\circ$ and $16^\circ$ is $>1$, then the median of the measurement uncertainty $\varepsilon$ is $2.7 \times 10^{15}$ molecules/cm$^2$ or $17\%$ relative to a mean tropospheric NO$_2$ column of $15.6 \times 10^{15}$ molecules/cm$^2$.

4 Results

In this section various results of our new two-step algorithm will be shown. Firstly, several steps in the tropospheric NO$_2$ retrieval algorithm will be illustrated for three selected days, and AOT and tropospheric NO$_2$ retrievals will be shown for four more days. Secondly, the algorithm is compared to the geometrical approximation, which is the default approach to derive tropospheric columns from MAX-DOAS observations. Finally a comparison with AOT from an AERONET instrument and a comparison with OMI tropospheric NO$_2$ is shown.

4.1 AOT and tropospheric NO$_2$ for selected days

Figure 10 shows the differential slant columns of NO$_2$, relative intensity, aerosol optical thickness and tropospheric NO$_2$ columns for three days, to illustrate the different steps in the retrieval. The first day (12 October 2008) is selected to illustrate the effect of clouds on the retrieval. Until around 13:00 UTC, clouds where present above the measurement location. This can be seen most clearly from the relative intensity observations. Under a homogeneous cloud cover, the intensity of scattered light is higher in the zenith direction than in other directions, and is decreasing with decreasing elevation. This results in relative intensities $<1$. After the clouds disappear (around 13:00 UTC) the situation is...
opposite. Under clear sky conditions the intensity of the scattered sunlight above the horizon is generally higher than the intensity in the zenith; the maximum intensity occurs usually somewhere between $\alpha = 8^\circ$ and $\alpha = 25^\circ$, depending on e.g. solar position and AOT (see Fig. 7). For this reason relative intensity $> 1$ is a good first indication for clear sky conditions, although this is not true in general: for small solar zenith angles the zenith sky may be brighter than the horizon. It is to be expected that relative intensity cannot be used to retrieve AOT under cloudy circumstances since the cloud has a much stronger effect on the relative intensity than the aerosols. As a consequence, AOT values larger than the maximum AOT of the look-up table (0.8) are retrieved before 13:00 UTC on 12 October 2008. At later times the three elevations ($4^\circ$, $8^\circ$, $16^\circ$) give similar AOT values. The effect of too large AOTs can also be seen in the NO$_2$ tropospheric

Fig. 10. Tropospheric NO$_2$ column retrieval for three selected days using the two-step algorithm. All plots have the same time scale on the horizontal axis and in each plot the colors correspond to the elevations indicated by the legend on the upper left. The first row shows the measured NO$_2$ differential slant columns in [10$^{16}$ molecules/cm$^2$]. The second row shows the relative intensities, and the third row the retrieved AOT. The last row shows the retrieved tropospheric column of NO$_2$ in [10$^{15}$ molecules/cm$^2$].
column retrieval for this day. However, a sudden change between 12:00 and 13:00 UTC cannot be seen in the differential slant columns. This illustrates that differential slant column measurements are mostly sensitive to the lowest kilometers of the atmosphere (whether or not below a cloud). The other two days in Fig. 10 (26 December 2008 and 27 January 2009) are included as an example of both a relatively clean and a relatively polluted day. The clean day, 26 December, was a public holiday with temperatures below 0°C. It shows stable conditions in both the tropospheric NO$_2$ column and AOT.

Four more examples of retrievals for cloud free days are shown in Fig. 11. The spread in the tropospheric columns of NO$_2$ between the three different elevations is relatively small, about 10%. Possible causes of the spread are discussed in Sect. 3.3.

### 4.2 Comparison with geometrical air mass factor approximation

The geometrical approximation (GA) of the differential air mass factor for MAX-DOAS observations provides a simple way to determine a first order estimate of the tropospheric column of NO$_2$, or other trace gases that are located primarily in the boundary layer. It is applied to MAX-DOAS observations in e.g. Brinksma et al. (2008) and Hains et al. (2010) in a comparison with other methods to measure tropospheric NO$_2$, such as lidar and satellite.

Using the geometric approximation is simple: it does not require an inversion based on radiative transfer modelling. The accuracy of this approximation has been discussed by e.g. Höninger et al. (2004), Wittrock et al. (2004), and Pinardi et al. (2008), based on radiative transfer modelling results.

Simulations with DAK show that, depending on the boundary layer aerosol load, large differences may occur between the geometrical and modelled differential air mass factors at low elevations $\alpha \leq 16^\circ$ (see Fig. 7, right plot). Therefore the GA should not be used for these elevations. For higher elevations, the difference becomes much smaller. It seems from Fig. 7 that the radiative transfer model and the
GA have almost the same differential air mass factor for 30° elevation. However, it can be seen from Fig. 12 that even for this high elevation, the difference between the GA and the model may become as large as 25%, depending on the relative position of the sun, and to a lesser extent on the AOT. At smaller relative azimuths this relative difference is even higher.

The question remains whether the algorithm proposed here, using a combination of lower elevation angles, an aerosol correction and AMFs derived from radiative transfer model calculations, gives a more accurate value for the tropospheric NO₂ column than the GA used on the 30° elevation measurement.

Figure 13 shows the tropospheric NO₂ column derived from the GA for $\alpha = 30^\circ$ (blue line), and the tropospheric NO₂ column and its estimated uncertainty derived with the two-step algorithm applied to $\alpha = 4^\circ$, 8° and 16° (grey band) for a clear-sky day. The systematic difference between the two methods for most of this day can be fully explained by the known systematic discrepancies of the GA which does not take multiple scattering, the relative azimuth angle, and the solar zenith angle into account.

This can be seen when looking at the difference between the results of the GA (blue line) and the two-step algorithm applied to $\alpha = 30^\circ$ (red line), which directly reflects the difference in AMFs (see also the red line in Fig. 12). The results of the two-step algorithm at $\alpha = 30^\circ$ is close to the results for lower elevation angles (grey band), within twice the estimated uncertainty. The larger uncertainty between 08:30 and 09:30 a.m. indicates an uncertain retrieval, which is probably caused by a relatively large difference between measurement conditions and one or several parameters that are assumed fixed in the model (e.g. the boundary layer height).

The estimated uncertainty in the tropospheric NO₂ column derived with the two-step algorithm is smaller than 15% for most of the day. In Sect. 3.3 it is shown that this uncertainty includes the effect of some major systematic and random error sources, because of the combination of the measurements at three different elevation angles.

It can be concluded that the uncertainty in the results of the two-step algorithm is often smaller than the known systematic discrepancies of the GA. The combination of multiple elevations enables an uncertainty estimate, based on the measurement conditions rather than on simulations, which is not possible with the GA: lower elevations than 30° cannot be used as they have even larger systematic discrepancies, and higher elevations do not add new information since the vertical sensitivity functions (box-AMF) of those higher elevations are almost identical to 30°, i.e. they are parallel to the orange line in Fig. 8.

4.3 Verification of AOT with AERONET data

As a verification of the AOT retrieved by the new two-step algorithm, a comparison is shown in Fig. 14 between the AOT data from the MAX-DOAS observations of relative intensity at De Bilt and the AOT data from the Aerosol Robotic Network (AERONET, see Dubovik and King, 2000) instrument at Cabauw (22 km from De Bilt). For all days in the operational period (see Sect. 2.2) level 1.5 AERONET AOT data at 440 nm was selected (if available) and compared with MAX-DOAS AOT data if the uncertainty in this value – i.e. the spread between AOTs derived from $\alpha=4^\circ$, 8° and 16° – was below 0.1. This selection resulted in 1251 data points (without the constraint on the spread of the AOTs there would have been 1415 data points) with a correlation of 0.85. The mean difference between the AERONET and MAX-DOAS AOT was $-0.01$ with a standard deviation of 0.08. Next, a linear regression was done that minimizes the sum of the squared orthogonal distances. From this regression a slope of 1.01 was found and an offset of $-0.01$. Considering the difference in observation method (direct sunlight versus scattered sunlight), and the distance between the two sites, this agreement is satisfying.

Fig. 13. Retrieved tropospheric NO₂ column in De Bilt for 21 March 2009. The grey band indicates the tropospheric NO₂ column retrieval with the two-step algorithm, based on differential slant column measurements at $\alpha = 4^\circ$, 8° and 16°. The red line represents the two step-algorithm applied to 30°. The blue line is based on the geometrical approximation (GA), also for 30° elevation. A one-hour running average has been applied to the differential slant column data in order to suppress noise.
were applied to all measurements in the observation period (see Sect. 2.2). The red line represents a linear regression, where the squared orthogonal distance of all points to the 1:1 line was minimized.

4.4 Comparison with satellite observations

As a first application of the time series of tropospheric NO\textsubscript{2} columns derived from the Mini MAX-DOAS measurements in De Bilt, an inter-comparison was made with tropospheric NO\textsubscript{2} data (DOMINO-product, see Boersma et al., 2007) from the Ozone Monitoring Instrument (OMI, see Levelt et al., 2006). The DOMINO data selection was based on different criteria described in Sect. 4.3 were applied to all measurements in the observation period (see Sect. 2.2). The selection criteria described in Table 4.3 were applied to all measurements in the observation period (see Sect. 2.2). The red line represents a linear regression, where the squared orthogonal distance of all points to the 1:1 line was minimized.

Figure 14. Comparison between AOT derived from MAX-DOAS relative intensity observations in De Bilt and AERONET AOT (Cabauw). Both sites were 22 km apart. The selection criteria described in Sect. 4.3 were applied to all measurements in the observation period (see Sect. 2.2). The red line represents a linear regression, where the squared orthogonal distance of all points to the 1:1 line was minimized.

where $m(z)$ is the height-dependent differential air mass factor for an AOT of 0.2 (see Fig. 8), $n(z)$ is a block profile for NO\textsubscript{2} from 0–1 km, and $T(z)$ is a standard temperature profile. A difference of about $-2.5^\circ\text{C}$ was found between the surface temperature and the effective NO\textsubscript{2} temperature for all three elevations $4^\circ$, $8^\circ$ and $16^\circ$.

Then surface temperature data were taken from KNMI temperature observations in De Bilt, and from this $2.5^\circ\text{C}$ was subtracted to determine the effective NO\textsubscript{2} temperature. The ratio of $\Delta T$ (see Fig. 6) at the temperature of the NO\textsubscript{2} cross section in the DOAS-fit and $\Delta T$ at the effective NO\textsubscript{2} temperature was applied as a temperature correction factor to the MAX-DOAS tropospheric NO\textsubscript{2} columns.

Figure 15 shows a scatter plot of the comparison. Three different selections of the MAX-DOAS data were made, based on different constraints on the (relative) spread of the ground-based tropospheric column of NO\textsubscript{2} (see Table 2). From 362 days of ground-based observations (see Sect. 2.2) only 123 data points remain after applying the selection criteria on the satellite data (including coincidence with the ground-based observation). Only 17 ground-based observations pass the 10% threshold, as described in Table 2.

The table shows that the correlation between the ground-based and satellite data improves with a more strict selection of the ground-based observations. However, when the estimated uncertainty (spread) of the ground-based observations is less than 10%, the standard deviation of the differences between the two data sets is about 25% ($3.8 \times 10^{15}$ molec/cm\textsuperscript{2} for a mean value of about $15 \times 10^{15}$ molec/cm\textsuperscript{2}).

To test if the spread between the OMI and the MAX-DOAS tropospheric NO\textsubscript{2} columns is dominated by the estimated retrieval errors from both data sets, a $\chi^2$ test was applied:

\begin{equation}
\chi^2 = \frac{1}{N} \sum_{i=1}^{N} \frac{(x_i - y_i)^2}{\epsilon^2_{x_i} + \epsilon^2_{y_i}},
\end{equation}

where $N$ is the number of data points $(x_i, y_i)$, $x_i$ is an OMI tropospheric NO\textsubscript{2} column measurement, with retrieval error $\epsilon_{x_i}$, and $y_i$ is a MAX-DOAS tropospheric NO\textsubscript{2} column measurement with retrieval error $\epsilon_{y_i}$ estimated from the spread as described in Eq. (17). For the three selections of the data, as described in Table 2, $\chi^2$ is between 2.5 and 3. Assuming an average difference of zero between the data sets and normal error distributions, the probability of exceeding these values for $\chi^2$ is less than 0.1%. Hence, the spread is larger than can be expected from the estimated retrieval errors alone.

A possible explanation for the part of the spread that is not explained by the retrieval errors, is the difference in observation techniques. First, the spatial representativity of the two types of observation is quite different. The horizontal footprint of an OMI pixel is different from the horizontal domain of the MAX-DOAS observation. Whereas OMI samples a domain of $>300\text{km}^2$, the MAX-DOAS has a horizontal range – in one direction – of roughly $10\text{km}$ for
Table 2. Comparison between OMI and MAX-DOAS tropospheric NO$_2$. The three rows represent three different sets of selection criteria that are applied to the ground-based retrieved tropospheric NO$_2$ columns. Each set consists of an upper limit of the relative measurement uncertainty ($\epsilon_{\text{rel}}^{\text{MD}}$ in percent) and an upper limit of the absolute measurement uncertainty ($\epsilon_{\text{abs}}^{\text{MD}}$ in 10$^{15}$ molec/cm$^2$). A point is selected if it satisfies one or both of the limits. The other columns are: number of collocations that satisfies these criteria ($n$), correlation ($R$), mean difference ($<d>$ in 10$^{15}$ molec/cm$^2$), standard deviation of differences ($\sigma_{<d>}$) in 10$^{15}$ molec/cm$^2$, slope ($\alpha_{\text{fit}}$) of linear fit that minimizes the sum of the squared orthogonal distances, y-axis offset of this linear fit ($\beta_{\text{fit}}$), mean relative and absolute measurement uncertainty of the ground based observations ($<\epsilon_{\text{rel}}^{\text{OMI}}>$ in percent and $<\epsilon_{\text{abs}}^{\text{OMI}}>$ in 10$^{15}$ molec/cm$^2$), and the same quantities for the satellite observation: ($<\epsilon_{\text{rel}}^{\text{MD}}>$ and $<\epsilon_{\text{abs}}^{\text{MD}}>$).

<table>
<thead>
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<th>Selection criteria</th>
<th>Comparison OMI – MAX-DOAS</th>
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<tbody>
<tr>
<td>set</td>
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</tr>
<tr>
<td>1</td>
<td>$\leq$ 30%</td>
</tr>
<tr>
<td>2</td>
<td>$\leq$ 20%</td>
</tr>
<tr>
<td>3</td>
<td>$\leq$ 10%</td>
</tr>
</tbody>
</table>


tables the lowest elevation of 4$^\circ$. Also the vertical range that contributes to the tropospheric NO$_2$ signal is different for the satellite and the MAX-DOAS observations. The sensitivity of MAX-DOAS to NO$_2$ decreases quickly with increasing height of NO$_2$, especially for high aerosol loads (see Fig. 8), whereas the satellite has increasing sensitivity with increasing NO$_2$ height (Eskes and Boersma, 2003). Consequently, the relative contribution of the free-tropospheric NO$_2$ to the total tropospheric NO$_2$ differs between the satellite and the MAX-DOAS.

Separation of the free tropospheric and boundary layer contribution to the tropospheric NO$_2$ column requires accurate knowledge of the NO$_2$ profile shape, both for the satellite and the MAX-DOAS retrieval. Lack of knowledge of the vertical distribution of NO$_2$ thus complicates the comparison of satellite and MAX-DOAS NO$_2$-data as well as the interpretation of satellite retrievals in terms of surface concentrations.

More observations and understanding of vertical profiles of NO$_2$ are needed to study the variety of circumstances under which differences between satellite and ground-based observations occur.

5 Conclusions

We described a new two-step algorithm to retrieve aerosol corrected tropospheric NO$_2$ columns from MAX-DOAS observations.

We used relative intensity observations performed with a mini MAX-DOAS instrument to estimate the aerosol optical thickness of the boundary layer. Based on this AOT-estimation, aerosol corrected differential air mass factors for NO$_2$ were determined to convert differential slant columns of NO$_2$ to tropospheric columns.

Relative intensity measurements have a strong dependence on boundary layer AOT and almost no dependence on boundary layer height although this dependence increases slightly with decreasing elevation.

Since relative intensity observations are very sensitive to clouds, the retrieval method can only be applied to cloud-free conditions. Under cloud-free conditions, the main source of error is the assumption of a fixed boundary layer height for
NO$_2$ in the algorithm. An uncertainty estimate in the results is derived from the spread in the tropospheric NO$_2$ columns that are derived independently for each elevation (4°, 8° and 16°). A low spread indicates a consistent retrieval of the tropospheric NO$_2$ column for the three elevations.

The use of the relatively low elevations makes the retrieval method more sensitive to trace gases in the boundary layer than the often used geometrical approximation that can only be applied at higher elevations (30°). The geometrical air mass factor approximation for 30° elevation gives a good first estimate of the tropospheric column. However, even for this high elevation, the differential air mass factor of the geometrical approach may differ up to 25% from the differential air mass factors using radiative transfer modeling. For relative azimuths smaller than 40°, this difference may even be larger.

The relatively low-cost (Mini) MAX-DOAS instruments are capable of generating long-time series of tropospheric composition data in an automated fashion. MAX-DOAS observations are particularly valuable for the purpose of satellite validation of tropospheric trace gases due to the horizontal and vertical range where trace gases can be detected, which is on the order of 1 to 4 km in the vertical and 5 to 10 km in the horizontal, depending on the AOT. Accurate comparison of satellite and ground-based observations requires knowledge of the NO$_2$ profile shape, in order to account for differences in the sensitivity to NO$_2$ at different heights.

The two-step retrieval scheme presented here was applied to cloud-free periods in a twelve month data set of MAX-DOAS observations in De Bilt, The Netherlands, between Autumn 2007 and Spring 2009 (summer of 2008 not included). For cloud free periods, the average tropospheric NO$_2$ column was $15.6 \times 10^{15}$ molecules/cm$^2$. The median of the estimated relative uncertainty was 17%.

In a comparison with AERONET (Cabauw site, 22 km from De Bilt) a mean difference in AOT (AERONET minus MAX-DOAS) of $-0.01 \pm 0.08$ was found, and a correlation of 0.85.

Tropospheric NO$_2$ columns were compared with OMI satellite tropospheric NO$_2$. Only satellite pixels over De Bilt were selected. The spread in the tropospheric NO$_2$ columns retrieved (semi)-simultaneously from the different MAX-DOAS elevations was used as a selection criterion. For ground-based observations restricted to a spread below 10%, a correlation of 0.88 was found, and no significant difference. The spread between OMI and MAX-DOAS tropospheric NO$_2$ column measurements is larger than can be expected from the estimated retrieval errors alone. This may be due to differences in the spatial representativity of the two observation techniques.

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