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Analytical Models for the Wake-up Receiver Power Budget for Wireless Sensor Networks

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Abstract—In this paper analytical models of the energy consumption are presented which uses a real world radio model with two different low power modes. This model is used to compare energy consumption of different MAC protocols. The MAC protocols used for the comparison are chosen with sensor networks in mind. The energy consumption of the nodes in a sensor network needs to be minimized to maximize the lifetime of the network. Emphasis is placed on MAC protocols, since they have a big influence on the energy consumption. One of the MAC protocols uses a low power Wake Up Receiver (WURx) which is used to decrease the total energy dissipation. The WURx MAC protocol is compared with two other low power MAC protocols, namely the asynchronous X-MAC and synchronous TDMA protocol. The obtained model is used to derive the WURx power budget. The response time of the nodes is used as the main design requirement and the important application parameters are given that determine the WURx power budget.

I. INTRODUCTION

Wireless sensor networks have many potential applications, for example medical body area networks (BAN). The vital signs of a patient can be monitored over a long time without the need for the patient to be physically in a hospital. Such a BAN network consists of a limited number of nodes and one of the main design goals is a low power consumption, since the nodes are battery powered making it inconvenient or even impossible to replace the batteries on a regular basis. Decreasing the radio energy consumption has a big impact on the total node energy consumption, since a large part of the energy is consumed by the radio [1].

One of the most important design constraints is the response time of a sensor node. In some applications, for example medical applications, data may have time limited relevance and has to be processed quickly, for example for pacemakers, and in control systems long latencies can lead to system instability [2]. In this paper MAC parameters are chosen in a way to satisfy a given response constraint.

A low power Wake Up Receiver (WURx) is added to a node, and it listens for radio transmissions while the main radio sleeps. This decreases the idle listening and overhearing power consumption, because the WURx has a significant smaller power consumption than the main radio. Overhearing means that a node receives packets that are destined to other nodes, see [3]. Furthermore the WURx MAC protocol is asynchronous and therefore has no synchronization overhead.

This paper presents an analytical model for the WURx power budget taking the application parameters into account and using a real world radio model. The conditions on the application parameters are analyzed that lead to a lower power consumption of a WURx system. The WURx power budget is obtained by comparing a MAC protocol with WURx to other MAC protocols.

MAC protocols can be divided in two groups, the asynchronous and synchronous schemes. B-MAC [4] and X-MAC [5] are two examples of asynchronous low-power, sensor-network, MAC protocols. The X-MAC scheme is shown to be more energy efficient because the transmitter does not have to send a long preamble, but several short preambles. This decreases the energy consumption caused by overhearing, see [5]. The X-MAC protocol can be used with the widely used packet radios in contrast to the B-MAC protocol.

Synchronous MAC protocols, like S-MAC [3], reduce the overhearing and idle listening power consumption by synchronizing the wake up periods. Nodes know when their neighbors are awake and only start the communication during this awake period. Furthermore the collisions can be reduced by appointing transmission slots, like in TDMA. The cost for this is the synchronization overhead and the resynchronization penalty. TDMA is a centrally coordinated synchronization scheme, unlike S-MAC. Static TDMA is beneficial for small networks since it moves the intelligence from the nodes to a central master node, which increases the node lifetime.

In section II a new and improved model is introduced, which is used to derive detailed new models for the energy consumption. These models are applied to various MAC protocols in section III. The application dependent energy consumption benefit of the WURx is analyzed in section V using the proposed models. The packet statistics are given in the appendix.
**II. Radio and Traffic Models**

Both a symmetric and asymmetric system are analyzed. In a symmetric system all the nodes in the network are equal and can both initiate and receive a data link setup. In an asymmetric system there is one master node which can initiate a data link setup, all the nodes are slaves. In this case the energy consumption of the master is less important than the energy consumption of a node since a master node can have a larger battery or can be connected to mains supply.

It is assumed that nodes can receive and transmit data to each other. The node which initiates a communication link is called here a transmitter and a node which receives a communication request is called a receiver. The radio parameters are summarized in table I.

Only the energy needed to set up a data link is taken into account since it is assumed that the data transfer itself is the same for the three MAC schemes used for the comparison: WURx, X-MAC and static TDMA. Furthermore, the application requires that the data link be set up within a given response time $T_{\text{response}}$.

A data link is set up in two steps, at the first step the transmitter transmits a Wake Up Call (WUC). When the WUC is received by the receiver it transmits an acknowledgment (ACK). Both the WUC and ACK are of minimal length $k$ and contain a destination address to decrease the overhearing problem. When the ACK is received by the transmitter the data link is set up and the data can be transferred.

There exist two types of errors, a packet can either be missed or falsely decoded. The packet miss probability is specified by $p_{\text{miss}}$ and a false wake up probability by $p_{\text{false}}$.

When the transmitter does not receive the ACK it retransmits the WUC maximally $N^*$ times. A WUC consists of a preamble, a destination address and a counter which counts the number of setup attempts. The counter is used by the receiver to know how many attempts it has left to transmit the ACK. A receiver starts transmitting acknowledgments when a WUC is received and stops when either the maximal number of attempts is reached or the ACK is received by the transmitter. The packet statistics are analyzed in greater depth in the appendix. In table I the used average values are listed.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\mu_{\text{WUC}}$</td>
<td>WUC</td>
</tr>
<tr>
<td>$\mu_{\text{ACK}}$</td>
<td>Initial ACKs</td>
</tr>
<tr>
<td>$\mu_{\text{ACKx}}$</td>
<td>ACK retransmissions</td>
</tr>
<tr>
<td>$\mu_{\text{set}}$</td>
<td>TDMA slots needed per wake up attempt</td>
</tr>
<tr>
<td>$N^*$</td>
<td>Maximal number of retransmission attempts</td>
</tr>
<tr>
<td>$k$</td>
<td>ACK and WUC packet length</td>
</tr>
</tbody>
</table>

**A. Radio States**

The radio state diagram is shown in figure 1. The radio power consumption in each state is given by the parameters outside the state symbols. The dotted states are transition states, the time period a node stays in these states is given in parenthesis. The sleep mode is the lowest power mode, therefore $P_{\text{sleep}} < P_{\text{standby}}$, and the energy consumed in each state is $E_x = T_x P_x$.

In the equations the difference in power and energy consumption of an active mode and the sleep mode are denoted by adding a leading $\Delta$.

**B. Traffic Scenario**

A network consist of $N_{\text{nodes}}$ nodes. It is assumed that each node receives the same number of packets with packet rate $\lambda$. The node energy consumption is normalized to the packet interval $\frac{1}{\lambda}$.

**III. MAC Energy Consumption Models**

The analytical models of the energy consumptions of three different MAC protocols are presented in the following sections. These models are used to obtain an analytical WURx power budget model.

**A. WURx MAC**

The WURx MAC scheme assumes an extra low power Wake Up Receiver added to the node. The bit rate $R_{bw}$ of the WURx can be different from the bit rate of the main radio, to decrease its power consumption $P_{\text{WURx}}$. The wake up cycle is shown in figure 2 (WURx cycle is not shown). To fulfill the response requirement the transmitter has to be able to transmit $N^*$ WUCs within $T_{\text{response}}$. This gives a WUC cycle period of $T_{\text{cycle}} = \frac{T_{\text{WURx}} - T_{\text{wake}}}{N^*}$. In the shown example the first ACK is missed by the transmitter. From the figure a lower bound on $R_{bw}$ is obtained,

$$R_{bw} \geq \frac{k}{T_{\text{WURx}}} = \frac{k}{T_{\text{cycle}} - 2T_{\text{set}} - T_{\text{wake}} - T_{\text{ACK}}}$$

The maximum wake up duration of one packet is $T_{\text{response}}$ and it is assumed that each node receives the same number of packets. The receiver and transmitter average energy consumption per received packet are given by (2) and (3), respectively. The first term specifies
the energy consumption while sleeping, the second term is the energy spend on the initial ACK transmission and the third term gives the energy consumption for the retransmissions.

\[ E_{RX} = \frac{P_{WURx} + P_{sleep}}{\lambda} + \mu_{ACK1} E_{ACK1} + \mu_{ACKx} E_{ACKx} \]  

\[ E_{TX} = \mu_{WUC} E_{WUC} + \Delta E_{wake} \]  

where,

\[ E_{WUC} = \Delta E_{set} + T_{WUC} \Delta P_T + \Delta E_{Rset} + T_{ACK} \Delta P_R + T_{wake} \Delta P_{standby} \]

\[ E_{ACK1} = \Delta E_{wake} + \Delta E_{set} + T_{ACK} \Delta P_T \]

\[ E_{ACKx} = (T_{wake} + T_{WUC} + T_{set}) \Delta P_{standby} + \Delta E_{Tset} + T_{ACK} \Delta P_T \]

B. X-MAC

The X-MAC [5] is the asynchronous MAC scheme used for comparison. The receiver wakes up periodically to listen for a WUC and the transmitter continuously transmits WUCs and listens for an ACK. The scheme is depicted in figure 3.

Since the receiver and transmitter are not synchronized the receiver has to listen long enough to receive two WUCs: it can happen that the receiver starts listening when the transmitter is already transmitting the wake up call. In that case the receiver will only receive the second one, using this assumption the listening period \( T_{list} \) is given by figure 3, is given below.

\[ T_{list} = 2T_{WUC} + T_{ACK} + 2T_{set} \]  

The receiver has to be able to receive \( N^+ \) WUCs within \( T_{response} \); therefore, the receiver cycle \( T_{cycle} \) is:

\[ T_{cycle} = \frac{T_{response}}{N^+} \]  

The receiver listening duty cycle is given by \( \eta \).

\[ \eta = \frac{T_{wake} + T_{set} + T_{list}}{T_{cycle}} \]  

The average number of WUC transmissions is given by \( \mu_{cycle} \) see (7). In this equation the first term gives the number of package needed to be send before the receiver receives a WUC, where the fact that the transmitter starts to transmit in the middle of the receiver cycle is. And the second term specifies the number of ACK that need to be retransmitted before the transmitter receives them.

\[ \mu_{cycle} = \left( \mu_{WUC} - \frac{1}{2} \right) \frac{T_{cycle}}{T_{response}} + \mu_{ACKx} \]  

The receiver and transmitter energy consumptions are given by (8) and (9), respectively. The first two terms of the receiver specify the sleep mode and idle listening energy consumption, where \( N_{cycle} \) denotes the number of times per received packet the receiver listens. In the receiver equation the third and fourth term specify the energy consumption for transmitting the acknowledgments.

\[ E_{RX} = \frac{P_{sleep}}{\lambda} + N_{cycle} E_{cycle} + \mu_{ACK1} E_{ACK1} + \mu_{ACKx} E_{ACKx} \]  

\[ E_{TX} = \mu_{cycle} E_{cycle} + \Delta E_{wake} \]

where,

\[ N_{cycle} = \frac{1}{\lambda T_{cycle}} \]

\[ E_{cycle} = \Delta E_{wake} + \Delta E_{Rset} + T_{list} \Delta P_R \]

\[ E_{ACK1} = \Delta E_{Tset} + T_{ACK} \Delta P_T \]

\[ E_{ACKx} = (T_{wake} + T_{WUC} + T_{set}) \Delta P_{standby} + \Delta E_{Tset} + T_{ACK} \Delta P_T \]

C. Static TDMA

With static TDMA the network consists of a Master node and one or more slave nodes; note that this is an asymmetric system. The master transmits a synchronization beacon every super frame. Within each super frame there can be a number of TDMA frames. Each TDMA frame has a slot for every node in the network; and the nodes can only communicate in their own slot. Figure 4 illustrates the MAC scheme where the sync period and one slot period are shown.

Each node has its own local clock with inaccuracy \( \Theta [\text{ppm}] \) which leads to clock skew between two nodes. The maximally allowed clock skew is given by \( T_{skew} \) which is depicted as gray areas in figure 4. In this paper it is assumed that \( T_{beacon} \gg \frac{T_{response}}{N^+} \), using this assumption the maximum time between two sync beacons \( T_{beacon} \) to keep the whole network synchronized is given below.

\[ T_{beacon}(\text{ms}) = \frac{T_{skew}(\text{ms})}{\Theta (\text{ppm})} \times 10^{8} \]
The average number of beacons per received packet $\mu_{bcn/pkt}$ is given by (11).

$$\mu_{bcn/pkt} = \frac{1}{\lambda T_{beacon}}$$  \hspace{1cm} (11)

When a node misses the synchronization beacon it stays in receive mode until it receives the next beacon in order to resynchronize. While resynchronizing all the packets are lost and the probability of this event is assumed to be equal to the packet miss probability. If $T_{beacon}$ is large the resynchronization penalty can be quite severe.

The node energy consumption is,

$$E_{Node} = \frac{P_{sleep}}{\lambda} + \mu_{bcn/pkt} E_{sync} + \frac{\Delta P_R}{\lambda} + \mu_{slot} E_{slot}$$  \hspace{1cm} (12)

where,

$$E_{sync} = \Delta E_{wake} + \Delta E_{set} + (2T_{skew} + T_{pkt}) \Delta P_R$$

$$E_{slot} = \Delta E_{wake} + \Delta E_{set} + T_{pkt} \Delta P_R$$

### D. WURx Power Budget Model

The WURx power budget is the difference in power consumption between the X-MAC or TDMA and the WURx MAC scheme. When the actual WURx power consumption is less than the budget the WURx scheme is more energy efficient. The approximated power budget is given below assuming $p_{miss}$ and $p_{false}$ are in the order of a few percent and can be neglected.

1) **WURx vs X-MAC**: The WURx power budgets are given by (13) and (14) for the asymmetric and symmetric systems, respectively. The power budget for the symmetric system consists of two terms, where the first term specifies the average power consumed by the receiver for the periodic listening and the second term gives the average power consumed for transmitting the WUCs by the transmitter.

$$P_{WURx, asym} \leq \frac{N^+}{T_{response}} E_{cycle} - \lambda \Delta E_{wake}$$  \hspace{1cm} (13)

$$P_{WURx, sym} \leq P_{WURx, asym} + \lambda \left( \frac{T_{response}}{N^+} - \frac{1}{2T_{cycle}} - 1 \right) E_{cycle}$$  \hspace{1cm} (14)

2) **WURx vs Static TDMA**: Equation (15) gives the WURx power budget for an asymmetric system. It can be seen that the power budget is highly dependent on the resynchronization penalty, i.e. on $p_{miss}$. The WURx scheme can only be beneficial when the TDMA synchronization overhead is larger than the WURx overhead.

$$P_{WURx, asym} \leq \frac{E_{sync}}{T_{beacon}} + p_{miss} \Delta P_R$$  \hspace{1cm} (15)

3) **X-MAC vs Static TDMA**: The X-MAC scheme is more power efficient than the X-MAC scheme when $p_{miss}$ is lower than the bound given by (16).

$$p_{miss} \leq \frac{T_{response} E_{cycle} - \lambda \Delta E_{wake} - \frac{E_{sync}}{T_{beacon}}}{\Delta P_R}$$  \hspace{1cm} (16)

### IV. Sleep Mode Boundary Conditions

The sleep mode should be used when the penalty for waking up is lower than the energy consumption decrease. This can be written as,

$$E_{wake} \leq E_{standby} - E_{sleep}$$  \hspace{1cm} (17)

The presented energy models assume that the sleep mode is used; when this is not the case then $T_{wake} = 0$ and $E_{sleep} = E_{standby}$.

The boundary conditions for the sleep mode are derived for the different MAC protocols for asymmetric and symmetric systems. The assumption $\Delta P_x \approx P_x$ is used when deriving the boundary conditions.

### A. WURx

The boundary condition on the packet rate is given below; when the inequality holds the sleep mode should be used.

$$\lambda_{asymmetric} \leq \frac{P_{standby} - P_{sleep}}{E_{wake}}$$  \hspace{1cm} (18)

$$\lambda_{symmetric} \leq \frac{P_{standby} - P_{sleep}}{2E_{wake}}$$  \hspace{1cm} (19)

### B. X-MAC

For the asymmetric and symmetric X-MAC systems the boundary conditions for using sleep mode are:

$$N^+ \frac{T_{response}}{T_{resp}} \leq \frac{P_{standby} - P_{sleep}}{E_{wake}}$$  \hspace{1cm} (20)

$$\lambda_{symmetric} \leq \frac{P_{standby} - P_{sleep}}{E_{wake}} - \frac{N^+}{T_{resp}}$$  \hspace{1cm} (21)

The boundary condition on the response requirement holds for both types of systems, whereas the bound on the packet rate exists only for the symmetric system.

### C. Static TDMA

The static TDMA scheme can only be used in an asymmetric system. The sleep mode should be used when the inequality given below holds.

$$\lambda \leq \frac{P_{standby} - P_{sleep}}{E_{wake}} - \frac{1}{T_{beacon}}$$  \hspace{1cm} (22)
V. Application Dependent Energy Consumption

To obtain the numerical results in this section the Nordic nRF24L01 [6] radio is used. The radio parameters are given in table II(a) and the application parameters are given in table II(b). In this section the results are given as a function of the important application parameters: $T_{\text{response}}^{+}$ and $\lambda$.

**TABLE II**

<table>
<thead>
<tr>
<th>Model parameters</th>
<th>(a) nRF24L01</th>
<th>(b) Application</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parameter</td>
<td>Value</td>
<td>Parameter</td>
</tr>
<tr>
<td>$T_{\text{wake}}$</td>
<td>1.5ms</td>
<td>$N_{\text{nodes}}$</td>
</tr>
<tr>
<td>$T_{\text{set}}$</td>
<td>130µs</td>
<td>$N^+$</td>
</tr>
<tr>
<td>$P_{\text{sleep}}$</td>
<td>2.7µW</td>
<td>$p_{\text{miss}}$</td>
</tr>
<tr>
<td>$P_{\text{standby}}$</td>
<td>66µW</td>
<td>$p_{\text{false}}$</td>
</tr>
<tr>
<td>$P_R$</td>
<td>36.9mW</td>
<td>$P_{\text{standby}}$</td>
</tr>
<tr>
<td>$P_T$</td>
<td>33.9mW</td>
<td>$P_{\text{set}}$</td>
</tr>
<tr>
<td>$P_{\text{set}}$</td>
<td>25.2mW</td>
<td>$P_{\text{wake}}$</td>
</tr>
<tr>
<td>$P_{\text{hot}}$</td>
<td>384bits</td>
<td>Packet size $k$</td>
</tr>
<tr>
<td>$\Theta$</td>
<td>50ppm</td>
<td>Bit rate $R_B$</td>
</tr>
</tbody>
</table>

If the packet miss probability is lower than the bound given by (16) and depicted in figure 5 then the TDMA protocol is more power efficient than the X-MAC protocol. The X-MAC system has to wake up less often when the required response time is higher. The TDMA protocol is more energy efficient for high response times when the TDMA resynchronization penalty is low. This can be seen in figure (5), for high response times the boundary condition on $p_{\text{miss}}$ is lower.

The WURx power budget for an asymmetric system as function of the packet rate $\lambda$ and $T_{\text{response}}^{+}$ is shown in figure 6, where the dotted line shows the approximated and the solid line the actual power budget. The approximated power budgets were given by (13) and (15) for the X-MAC and TDMA protocols, respectively. It can be seen that the approximations are good, thus the $p_{\text{miss}}$ and $p_{\text{false}}$ can be neglected when they are smaller than a few percent. For high response times the WURx protocol is compared to the X-MAC protocol since it is more power efficient than the TDMA protocol. Since the X-MAC node can sleep for longer periods for high response times the power budget is lower. The budget decreases for higher packet rate, because the WURx receiver needs to wake up from sleep mode once per packet reception. For $p_{\text{miss}} = 1\%$ the TDMA scheme is more power efficient when $\frac{T_{\text{response}}^{+}}{N^+} \leq 40\text{ms}$, as can be seen in figure 5. This boundary condition is shown by the line labeled with a power budget of 372µW.

The WURx power budget of a symmetric system is shown in figure 7. Again, the approximation is shown by the dotted lines and the real power budget is shown by the solid lines. The TDMA system can not be used as a symmetric system, as there is always a master node, thus the WURx energy consumption can only be compared to the X-MAC protocol. Since the X-MAC transmitter needs to transmit many WUCs before the receiver wakes up the power budget for the symmetric system is much larger than for the asymmetric system. When the packet rate is fixed there are two possible response times for a given power budget. The power consumption is mainly determined by the transmitter.
for the large response time. For the smaller response

time the periodic listening power consumption of
the receiver determines the power budget. At the boundary
between the two regions the transmitter and receiver
contributions are equal.

For large $T_{\text{response}}$ the power budget increases
for higher response times since the X-MAC transmitter needs
to transmit more WUCs which costs a lot of energy. For
lower response times, where the idle listening power
consumption is significant, a decrease in response time
leads to an increase in power budget. The power budget
increases with an increase of the packet rate, because the
X-MAC transmitter transmits more WUCs.

VI. Conclusions

This paper presents analytical models for the energy
consumption of three different MAC protocols as well
as a WURx MAC protocol. Using the analytical models
the application dependent maximum power budget for
the WURx is obtained for asymmetric and symmetric
systems. The used radio model has a deep sleep mode
and a low power standby mode. Whether the deep sleep
mode should be used can be decided when the given
parameters of the actual radio are known.

The TDMA protocol is more power efficient than
the X-MAC protocol when the response requirement and
the packet miss probability are low. For asymmetric systems
the WURx MAC protocol is most efficient when the
response time requirement is low. For the symmetric system
the WURx MAC protocol is most efficient when the
response time and the packet rate is high.

Appendix

Packet statistics

The expected number of WUC and ACK transmissions
are calculated using (23). Where $p_{x,k}$ is the probability
on k number of x transmission attempts.

$$\mu_x = \sum_{k=1}^{N_{\text{WUC}}} k p_{x,k}$$ (23)

A. Wake up calls

The probability of n WUC transmissions $P_{\text{WUC}n}$ is,

$$P_{\text{WUC}n} = n (1 - p_{\text{miss}})^2 p_{\text{mis}}^{n-1}$$ (24)

The receiver starts transmitting ACK after it receives any
of the n WUC packets. The transmitter stops transmitting
after it correctly receives an ACK. For the other $n-1$ wake up
attempts the WUC or ACK packet is missed. An error is
made for $P_{\text{WUC}N_{\text{WUC}}}$ since the transmitter stops after
$N_{\text{WUC}}$ attempts regardless whether it was successful or not.

$$P_{\text{WUC}N_{\text{WUC}}} = 1 - \sum_{k=1}^{N_{\text{WUC}}} P_{\text{WUC}k}$$ (25)

B. Acknowledgments

The probability distribution of n correct ACK transmis-
sions $P_{\text{ACK,Correct},n}$ is given below. The first term specifies
the events where both the WUC and ACK are received correctly. The second term specifies the prob-
ability that all the acknowledgements are missed.

$$P_{\text{ACK,Correct},n} = (1 - p_{\text{miss}}) N_{\text{WUC}}^{n-1} (1 - p_{\text{miss}}) P_{\text{ack},n}^{n-1}$$ (26)

The false wake up probability per other node in the
network is given by (27). The first $N_{\text{WUC}}$ WUC packets
are received correctly. The summation gives the proba-

bility that more than $N_{\text{WUC}}-n$ WUCs are transmitted.

$$P_{\text{ACK,Correct},n} = p_{\text{false}} (1 - p_{\text{false}}) N_{\text{WUC}}^{n} \sum_{k=N_{\text{WUC}}-n+1}^{n} P_{\text{WUC}k}$$ (27)

The ACK transmission probability distribution is
given below. The receiver can falsely wake up when one
of the other nodes transmits WUCs.

$$P_{\text{ACK},n} = P_{\text{ACK,Correct},n} + (N_{\text{nodes}} - 1) P_{\text{ACK,Correct},1}$$ (28)

The expected number of initial ACK transmissions
($\mu_{ACK}$) and retransmissions ($\mu_{ACKx}$) are given by,

$$\mu_{ACK} = P_{\text{ACK,Correct},1} + (N_{\text{nodes}} - 1) P_{\text{ACK,Correct},1}$$ (29)

$$\mu_{ACKx} = \mu_{ACK} - \mu_{ACK1}$$ (30)

C. TDMA slots

The probability that a node needs n TDMA slots to
transmit an ACK $P_{\text{slot},n}$ is,

$$p_{\text{slot},n} = (1 - p_{\text{miss}}) p_{\text{miss}}^{n-1}$$ (31)

The node stops transmitting after the master receives
the ACK. For the other $n-1$ attempts the ACK packet is
missed. An error is made for $p_{\text{slot},N_{\text{WUC}}}$ since the node
stops after $N_{\text{WUC}}$ attempts.

$$p_{\text{slot},N_{\text{WUC}}} = 1 - \sum_{k=1}^{N_{\text{WUC}}} P_{\text{slot},k}$$ (32)

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