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Citation for published version (APA):

Document status and date:
Published: 01/01/2010

Document Version:
Publisher’s PDF, also known as Version of Record (includes final page, issue and volume numbers)

Please check the document version of this publication:
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Download date: 03. Apr. 2019
Velocity Trajectory Optimization in Hybrid Electric Trucks

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Abstract—Hybrid Electric Vehicles (HEVs) enable fuel savings by re-using kinetic and potential energy that was recovered and stored in a battery during braking or driving down hill. Besides, the vehicle itself can be seen as a storage device, where kinetic energy can be stored and retrieved by changing the forward velocity. It is beneficial for fuel consumption to optimize the velocity trajectory in two ways; i) to assist the driver in tracking an optimal velocity trajectory (e.g. input to an Adaptive Cruise Controller); ii) to estimate the future power request trajectory which can be used to optimize the hybrid components use. Taking advantage of satellite navigation, together with the vehicles current mass and road load parameters, an optimization problem is formulated, and solved for a driver defined time constraint. Despite tight velocity constraints, this can result in 5% fuel saving compared to a Cruise Controller with constant velocity setpoint. The benefit of velocity trajectory optimization is indicated with experimental results.

I. INTRODUCTION

Hybrid Electric Vehicles (HEVs) enable fuel savings by re-using kinetic and potential energy that was recovered and stored in a battery during braking or driving down hill. Besides the HEV battery, the vehicle itself can be seen as a storage device, where kinetic energy can be stored and retrieved by changing the forward velocity. Therefore, the velocity trajectory can be optimized for certain vehicle operating conditions [1]. The velocity trajectory optimization problem can be defined as: finding a velocity trajectory that minimizes the fuel consumption subject to a time constraint.

In literature several useful contributions can be found regarding velocity trajectory optimization in conventional vehicles. In [2] it is suggested to use Dynamic Programming (DP) to numerically solve the optimal control problem in a hilly environment. This approach is successfully adapted and implemented by [3] using Model Predictive Control (MPC) in combination with an Adaptive Cruise Control (ACC). Ref. [4] suggests to solve the optimal control problem with a strategy of first deriving analytical optimality conditions and evaluating them numerically afterwards. In [5] Pontryagin’s Minimum Principle is used to obtain an optimal velocity trajectory. It was concluded that for conventional vehicles, under constant load conditions (e.g. constant road grade), the optimal velocity trajectory subject to a time constraint consists of, full pedal acceleration, followed by a constant velocity part, a coast part and finally a hard deceleration.

Several remarks can be made to the current literature on velocity trajectory optimization. First, optimal velocity trajectories of conventional vehicles are not necessarily optimal for HEVs [6]. Since these vehicles can recover kinetic energy during braking or driving down hill, the above mentioned conclusions do not automatically hold. Secondly, considering that under constant load conditions the solution shape consists of, a.o., constant velocity, solving the optimization problem with an equidistant grid has an unnecessary high numerical load. Therefore, data aggregation and velocity trajectory optimization methods that adapt to the route and vehicle characteristics can be beneficial.

The contribution of this paper is a method that solves the velocity optimization problem for HEVs, based upon information from a Global Navigation Satellite-based System (GNSS). Furthermore, it allows the driver to make a balanced choice between fuel economy and traveling time. Assuming a predefined shape of the velocity trajectory allows construction of an optimization problem with relatively low computational effort. Nonlinear programming techniques are explored to solve the optimization problem. The resulting velocity trajectory is used as input for an ACC system, and to estimate the future power trajectory, which enables optimization of the hybrid component use. The benefit of velocity trajectory optimization is indicated with experimental results.

II. VELOCITY TRAJECTORY OPTIMIZATION

Determination of the energy-time optimal velocity trajectories requires a combination of route information and vehicle conditions, see Fig. 1. The relevant route information consists of velocity limitations, curvature and road grade. This information can be derived from a Geographic Information System (GIS) in combination with a route planner for the destination indicated by the driver. A GNSS with map-matching algorithms can then be used to locate the vehicle in the map.

The map data could be transferred, e.g. using a CANbus system [7], with a certain horizon. The CAN messages contain information for small parts of the route, and cannot directly be used by the optimization algorithm. The method outlined in this paper accumulates the h messages, and divides a route into n segments with constant velocity limitations and constant road grade as function of the traveled distance. Segments can also be divided by stopping points. This approach requires a rounding of the GIS data and calculation of relevant curvature and road grade, and is further discussed in Section II-A.

Depending on the vehicle operating conditions, electric machine size and battery capacity, velocity trajectories can be determined that minimize the energy use. In Section II-B it is motivated that these solutions have an approximate solution with a fixed solution shape. Algebraic equations are derived that express the equivalent fuel consumption and traveling time as function of cruising and end velocity, and of electric machine and service brake use in one segment, see Section II-C. An optimization problem is obtained by adding up the results of all segments, see Section II-D. It
is shown that this optimization problem can be effectively solved using nonlinear programming techniques.

Output of the velocity trajectory optimization is a velocity trajectory and a power trajectory. Perfect tracking of an optimal velocity trajectory will not be possible in actual traffic. Therefore, an ACC system may be employed that consist of an automated cruise control as well as automated adaptation of the vehicle velocity to actual (preceding) traffic [9]. For this, the vehicle can be equipped with a radar, that can provide information about the velocity and distance to a preceding vehicle. In case of a preceding vehicle, the CC could trigger a recalculation of an optimal velocity trajectory. Besides the velocity trajectory, also a prediction of the future power trajectory is available. This trajectory can be used to optimize the power split trajectory between primary and secondary power converter [10], often referred to as Energy Management Systems (EMS), see [11] for a general overview.

A. Map Data Conversion

Let us consider a highway trajectory, see Fig. 2 for the topography. From the GIS and routeplanner we obtained CAN messages describing the route ahead. From these messages, the velocity limitation \( v_{\text{max}}(h) \), road curvature \( \kappa(h) \) and road grade \( \beta(h) \) are expressed as function of the traveled distance \( l(h) \) with message number \( h \).

1) Assumptions on vehicle model: to enable calculation of the optimal velocity trajectory \( \hat{v}_{\text{opt}}(x) \), a vehicle model and an estimation of the road load force \( \hat{F}_r(h, v) \) is required. Parameters indicated with a hat are estimated values. The road load force depends on the vehicle mass and the route characteristics:

\[
\hat{F}_r(h) = \hat{c}_0(h) + \hat{c}_1(h)v + \hat{c}_2(h)v^2
\]

(1)

where \( \hat{c}_0(h) \) is the drag force independent of velocity \( v \):

\[
\hat{c}_0(h) = \hat{F}_r(h) + \hat{F}_g(h)
\]

(2)

with \( F_r \) the rolling resistance:

\[
\hat{F}_r(h) = c_r \hat{m} g \cos \beta(h)
\]

(3)

in which \( c_r \) is the rolling resistance coefficient, \( g \) is the gravitational constant, \( \hat{m} \) is the estimated vehicle mass and \( \beta \) is the road grade. The gravitational force is estimated with:

\[
\hat{F}_g = \hat{m} g \sin \beta(h).
\]

(4)

Furthermore, \( \hat{c}_1 \) is the coefficient for drag force linearly depending on velocity, \( \hat{c}_2(h) \) is the coefficient for the drag force depending on vehicle velocity squared:

\[
\hat{c}_2(h) = \frac{1}{2} \rho_a(h) A_f c_d
\]

(5)

here, \( \rho_a \) is the air density, \( A_f \) is the vehicle frontal area and \( c_d \) is the aerodynamic coefficient.

It is assumed that the measured relation between the produced engine power and the fuel consumption can be approximated with an affine relation:

\[
\hat{m}_f = \hat{m}_{f0} + \frac{k_{\text{ice}}}{h_f} P_{\text{ice}}
\]

(6)

here, \( \hat{m}_f \) is the approximated fuel mass flow, \( \hat{m}_{f0} \) is the fuel mass flow at zero torque, \( k_{\text{ice}} \) corresponds to the combustion efficiency and engine internal losses, and \( h_f \) is the lower heating value of the fuel. The engine power is constrained to the set \( P_{\text{ice}} \in [P_{\text{drag}}, P_{\text{max}}] \), here, \( P_{\text{drag}} \) is the engine drag power, and \( P_{\text{max}} \) is the maximum available propulsion power. It is known [12] that disregarding the engine rotational velocity dependent ICE losses might lead to suboptimal results.

The electric machine efficiency is approximated as constant and independent of rotational velocity with \( \eta_{\text{em}} \):

\[
P_{\text{s}}(t) = \eta_{\text{em}} P_{\text{em}}(t)
\]

(7)

in which \( P_{\text{s}} \) is the electric power, and \( P_{\text{em}} \) is the electric machine mechanical power, where we assume that \( P_{\text{em}} \in [0, P_{\text{em}}] \). The battery efficiency is quadratic with the power throughput.

\[
P_{\text{s}}(t) = P_{\text{b}}(t) - P_{\text{b}}^2(t) \frac{R_{\text{SOC}=0.5}}{V_{\text{bat}}^2}\frac{1}{\text{SOC}=0.5}
\]

(8)

Here, \( P_{\text{s}} \) is the effective storage power, \( R \) is the battery internal resistance at \( \text{SOC} = 0.5 \) and \( V_{\text{bat}} \) is the voltage of the battery in equilibrium at \( \text{SOC} = 0.5 \). The use of the recovered energy, and therefore the average battery efficiency during discharge is governed by the real-time EMS, therefore a constant linear estimation \( \eta_{\text{bat}} \) of the battery discharge efficiency is made.

\[
P_{\text{b}}(t) = \eta_{\text{bat}} P_{\text{b}}(t)
\]

(9)

2) Velocity limitations: the maximum legal velocity \( v_{\text{max}} \) on the traject is 80/3.6 m/s for heavy-duty vehicles. The traject in Fig. 2 does not have road curvature. Nevertheless it can be expected, on different routes, that vehicles need to slow down, such that they do not exceed a maximum centrifugal acceleration:

\[
v_{\text{curvature}}(h) < \sqrt{\alpha_{\text{cf}} \kappa(h)}
\]

(10)

Here, \( v_{\text{curvature}} \) is the maximum vehicle cornering velocity, \( \kappa(h) \) is the curve radius, and \( \alpha_{\text{cf}} \) the maximum centrifugal acceleration for comfortable and save driving. The influence of road banking, which data might be available in a modern
routeplanner, is omitted for simplicity. The velocity limitation is defined as the minimum of the maximum (legal) velocity \(v_{\text{max}}\), the maximum cornering velocity \(v_{\text{curv}}\) and, possibly, the congestion dictated velocity \(v_{\text{traffic}}\).

\[
v_{\text{lim}}(h) = \min(v_{\text{max}}(h), v_{\text{curv}}(h), v_{\text{traffic}}(h))
\]

Here \(v_{\text{lim}}\) is the velocity limitation. Curvature is rounded with an accuracy of \(\delta_{\text{curv}}\) m\(^{-1}\). Rounding is required to arrive at segments with a constant velocity limitation. The value of \(\alpha_{\text{fg}}\) should be chosen such that even with maximum rounding error, the vehicle will corner safely. Clearly, decreasing \(\alpha_{\text{fg}}\) will increase the number of segments required for velocity limitations. Next, road grade segmentation is discussed.

3) Road grades: to arrive at a suitable optimization problem, some assumptions are required. It is assumed here that the velocity dependent loss term \(\dot{c}_1\), does not change with road grade, unlike [5]. Moreover, the engine efficiency is not depending on the rotational velocity, as in (6). Using these simplifications, gravitational resistance uphill requires a constant amount of fuel, that has to be delivered in any case. Therefore, the road grades can be aggregated, unless the maximum power constraint is reached; so if

\[
\beta_{\text{up}} = \arcsin \left( \frac{\gamma_{\text{eng}} P_{\text{max}}}{\dot{v}_{\text{lim}}} - F_r - \dot{c}_1 v_{\text{lim}} - \dot{c}_2 v_{\text{lim}}^2 \right) \frac{\dot{m} g}{\dot{h}}
\]

here, the power discontinuities during gearshifts, and torque limitations, are accounted for by reducing the maximum available power with constant factor \(\gamma_{\text{eng}}\), and \(\cos \beta = 1\) in (3). Moreover, the road grade is rounded with an accuracy of \(\delta_{\text{grade}}\), see the lower part of Fig. 2.

The same kind of reasoning as for uphill driving holds for driving downhill; downhill driving does not change the solution shape, and thus can be aggregated, unless a negative power request is obtained; so if

\[
\beta_{\text{dn}} = \arcsin \left( \frac{P_{\text{eng}}}{\dot{v}_{\text{lim}}^2} + F_r + \dot{c}_1 \gamma v_{\text{lim}} + \dot{c}_2 \gamma v_{\text{lim}}^2 \right) \frac{\dot{m} g}{\dot{h}}
\]

here, \(\gamma v_{\text{lim}}\) is the lower velocity constraint.

Road grades \(\beta_{\text{dn}} < \beta(h) < \beta_{\text{up}}\) are aggregated and averaged. In the example of Fig. 2, the 9 initial segments can be reduced to 7 segments. This results in an approximated elevation, see dashed line in upper part of Fig. 2.

B. Segment Solution

Using the segments with constant road grade and velocity constraints and based upon assumptions outlined in this section, it is suggested that the velocity trajectory for each segment is described with four phases; \(\text{max. power acceleration, constant velocity, coast, and max. power deceleration}\), see Fig. 3. Determination of the velocity trajectory boils down to finding the parameters that describe the length of each phase, subject to the segment velocity and distance constraints, and route time constraint.

The physical motivation for this shape is as follows: as indicated before, \(\dot{c}_0\) is a velocity independent term. Therefore, provided that the distance of the route is constrained, the energy necessary to overcome \(\dot{c}_0\) is fixed. Since distance and time are constrained, the energy required to overcome \(\dot{c}_1\) is also fixed along the route. Therefore, minimizing fuel economy comes down to minimizing the losses that quadratically depend on the velocity \(\dot{c}_2\), and the loss of kinetic and potential energy in the service brakes and hybrid system. With this reasoning, the time constrained velocity trajectory optimization can be solved by introducing four variables, for each segment, that describe this solution shape: the constant velocity \(v_{\text{cr}}\), electric machine use \(P_{\text{em}}\) during coasting, starting velocity \(v_{\text{a}}\) of max. power deceleration, and end velocity \(v_{\text{e}} = v_{\text{a}}\) of next segment.

Finally, note that a segment could also start with a deceleration, if \(v_{\text{a}} > v_{\text{cr}}\). In that case a \(\text{coast}\) and \(\text{max. power deceleration}\) phase is substituted for the \(\text{max. power acceleration}\).

C. Cost Function Construction

The cost, in terms of fuel consumption and traveling time, for each phase is calculated in this section.

1) Acceleration phase: in [5] it is shown that full throttle accelerations lead to fuel optimal velocity trajectories. Fortunately, real-life driving behavior of heavy-duty vehicles is to use the full power of the vehicle, even for an unloaded vehicle, as was indicated in [13]. Therefore, this approach is
especially relevant for heavy-duty vehicles. The force at the vehicle wheels is described with:

\[ \hat{F}_m(n) = \frac{\gamma_{eng} P_{\text{max}}}{v} - \hat{F}_t(n). \] (14)

The vehicle longitudinal equation of motion becomes:

\[ \frac{dv}{dt} = \frac{\hat{F}_m(n)}{m_e} \] (15)

here, \( \hat{m}_e \) is the estimated effective vehicle mass, including the rotational inertia of all rotating parts. Rewriting (15), substituting (14), and integrating from the starting velocity \( v_a \) to cruising velocity \( v_{cr} \) gives the acceleration time:

\[ \Delta t^{v_a}_{\text{fa}} = \hat{m}_e \int_{v_a}^{v_{cr}} \frac{1}{\hat{F}_m(n)} dv \] (16)

This has the solution:

\[ \Delta t^{v_a}_{\text{fa}} = \hat{m}_e \sum_{q_{a-b}=1}^{3} \frac{R_{q_{a-b}} \ln \left( \frac{v_{cr} - R_{q_{a-b}}}{\gamma_{eng} P_{\text{max}} - R_{q_{a-b}}} \right)}{c_0(n) + 2c_1(n)R_{q_{a-b}} + 3c_2(n)R^2_{q_{a-b}}} \] (17)

here \( R_{q_{a-b}} \) is the \( q_{a-b} \)th root of the cubic equation:

\[ -\gamma_{eng} P_{\text{max}} + c_0(n)z + c_1(n)z^2 + c_2(n)z^3 = 0. \] (18)

Equation (18) can be solved analytically. The fuel consumption, required during the acceleration part, is expressed algebraically in the start velocity \( v_a \) and cruise velocity \( v_{cr} \):

\[ m_{fa-b} = \left( \hat{m}_f_0 + \frac{k_{icc}}{h_f} \gamma_{eng} P_{\text{max}} \right) \Delta t^{v_a}_{\text{fa}}. \] (19)

The covered distance \( \Delta s^{v_a}_{ \text{fa} } \) is calculated similarly by multiplying (31) \( v \). Note that both \( \Delta t^{v_a}_{\text{fa}} \) and \( \Delta s^{v_a}_{ \text{fa} } \) are functions of the form \( x \ln y \). When the end velocity of the previous section is equal to the \( v_{cr} \) of the current section, the acceleration part is ignored, and \( \Delta t^{v_a}_{\text{fa}} \) and \( \Delta s^{v_a}_{ \text{fa} } \) are zero.

2) Coast phase: it is assumed that the vehicle does not change gear during the coast. The electric machine has a constant torque bound \( T_{em} \) at low velocities \( v < v_{rm} \) and a constant power bound \( P_{em} \) at high rotational velocities. The force that decelerates the vehicle can then be expressed as:

\[ F_{p_{\text{e-d}}} = -\frac{P_{em} + P_{\text{drag}}}{v} - \hat{F}_t(n) \] (20)

for \( v \geq v_{rm} \), and

\[ F_{e_{\text{d}}} = -\frac{P_{\text{drag}}}{v} - \frac{T_{em} i_{gb} i_f}{r_w} - \hat{F}_t(n) \] (21)

for \( v < v_{rm} \). Here, \( r_w \) is the wheel radius, \( i_{gb} \) is the actual gearbox ratio, \( i_f \) is the final drive ratio. The value of \( P_{em} \) is an optimization variable. The deceleration time becomes:

\[ \Delta t^{v_{\text{e-d}}}_{\text{fa}} = \hat{m}_e \int_{v_{\text{e-d}}}^{v_{\text{e}} \text{e-d}} \frac{1}{F_{p_{\text{e-d}}}} dv + \hat{m}_e \int_{v_{\text{e-d}}}^{v_{\text{e}}} \frac{1}{F_{e_{\text{d}}}} dv. \] (22)

This has the solutions:

\[ \Delta t^{v_{\text{e-d}}}_{\text{fa}} = \hat{m}_e \sum_{q_{e-d}=1}^{3} \frac{R_{q_{e-d}} \ln \left( \frac{v_{\text{e-d}} - R_{q_{e-d}}}{\gamma_{eng} P_{\text{max}} - R_{q_{e-d}}} \right)}{c_0(n) + 2c_1(n)R_{q_{e-d}} + 3c_2(n)R^2_{q_{e-d}}} \] (23)

The equivalent fuel consumption is:

\[ m_{f_{e-d}} = \frac{E_{c-d}}{h_f}. \] (28)

3) Deceleration phase: in [5] it is shown that strong deceleration braking leads to fuel optimal velocity trajectories. However, this optimum may not be valid for HEV, since they can recover energy during braking. The following procedure for the deceleration path description is suggested.

The electric machine has a constant torque bound \( T_{em} \) at low velocities \( v < v_{rm} \) and a constant power bound \( P_{em} \) at high rotational velocities. The force that decelerates the vehicle can then be expressed as:

\[ F_{p_{\text{d-e}}} = -\frac{P_{em} + P_{\text{drag}}}{v} - \frac{T_{ser}}{r_w} - \hat{F}_t(n) \] (29)

for \( v \geq v_{rm} \), and

\[ F_{d_{\text{e}}} = -\frac{P_{\text{drag}}}{v} - \frac{T_{ser} + T_{em} i_{gb} i_f}{r_w} - \hat{F}_t(n) \] (30)

for \( v < v_{rm} \). Here, \( T_{ser} \) is the (maximum) brake torque of the service brakes. It is assumed that there is no change of gear during the deceleration. Note that braking with \( T_{em} < T_{em_{\text{max}}} \) and \( P_{em} < P_{em_{\text{max}}} \) is in any case suboptimal, when disregarding the electric machine internal efficiency, and assuming that the battery is not fully charged. The values of \( T_{em} \) and \( P_{em} \) are then known a priori. The deceleration time becomes:

\[ \Delta t^{v_{\text{e-d}}}_{\text{fa}} = \hat{m}_e \int_{v_{\text{e-d}}}^{v_{\text{e}}} \frac{1}{F_{p_{\text{e-d}}}} dv + \hat{m}_e \int_{v_{\text{e}}}^{v_{\text{e}}} \frac{1}{F_{e_{\text{d}}}} dv. \] (31)

This has the solutions:

\[ \Delta t^{v_{\text{e-d}}}_{\text{fa}} = \hat{m}_e \sum_{q_{e-d}=1}^{3} \frac{R_{q_{e-d}} \ln \left( \frac{v_{\text{e-d}} - R_{q_{e-d}}}{\gamma_{eng} P_{\text{max}} - R_{q_{e-d}}} \right)}{c_0(n) + 2c_1(n)R_{q_{e-d}} + 3c_2(n)R^2_{q_{e-d}}} \] (32)
\[ \Delta t^t_{t_{e}} = \frac{R_{q_{r-m-e}}}{m_c} \sum_{r=1}^{3} \left( c_0(n) + 2c_1(n) R_{q_{r-m-e}} + 3c_2(n) R_{q_{r-m-e}}^2 \right) \ln \left( \frac{v_e - R_{q_{r-m-e}}}{v_{r-m-e} - R_{q_{r-m-e}}} \right), \] (33)

Here \( R_{q_{d-r-m}} \) is the \( q_d-r_m \)th root of the cubic equation:

\[ (P_{em} + P_{drag}) + \frac{(T_{ser} + \dot{c}_0(n))}{T_h} z + \dot{c}_0(n) z^2 + \dot{c}_1(n) z^3 = 0. \] (34)

And, \( R_{q_{r-m-e}} \) is the \( q_{r-m-e} \)th root of the cubic equation:

\[ P_{drag} + \frac{(T_{ser} + T_{em}b_{i})}{T_h} z + \dot{c}_0(n) z^2 + \dot{c}_1(n) z^3 = 0. \] (35)

The equivalent fuel consumption is:

\[ m_{f-d-e} = \frac{E_{d-e}}{h_f}. \] (37)

4) Constant velocity phase: from the covered distance in the acceleration, coast, and deceleration part, follows the distance to be covered with constant velocity:

\[ \Delta s|_{s_b} = (s_e - s_a) - \Delta s|_{s_a} \] (38)

The travel time in this part follows from:

\[ \Delta t^t_{t_b} = \frac{\Delta s|_{s_b}}{v_{cr}} \] (39)

The power required to overcome the road load forces is:

\[ P_{req} = \dot{c}_0(n) v_{cr} + \dot{c}_1(n) v_{cr}^2 + \dot{c}_2(n) v_{cr}^3 \] (40)

Using (6), the fuel consumption on the constant velocity path becomes:

\[ m_{f_{c-e}} = \left( m_{f_0} + \frac{k_{ice} P_{req}}{h_f} \right) \Delta t^t_{t_b} \] (41)

5) Segment cost: the equivalent fuel consumption \( m_f \) and traveling time \( t_n \) on a segment can both be expressed as a function of the constant velocity \( v_{cr} \), electric machine use \( P_{em} \), service brakes appliance velocity \( v_d \), and end velocity \( v_e \):

\[ m_{f_{a-b}}(v_{cr}, P_{em}, v_d, v_e) = m_{f_{a-b}} + m_{f_{b-c}} + m_{f_{c-d}} + m_{f_{d-e}} \] (42)

The travel time for the segment becomes:

\[ t_n(v_{cr}, P_{em}, v_d, v_e) = \Delta t^t_{t_a} + \Delta t^t_{t_b} + \Delta t^t_{t_c} + \Delta t^t_{t_d} \] (43)

D. Optimization Problem Formulation

In the previous section it is shown that fuel consumption and traveling time on one segment can be expressed, analytically, in vehicle velocity on the constant velocity part, electric machine and service brake use. Therefore, the segment cost can be computed with little computational effort given the four aforementioned parameters. This result is used to construct an optimization problem formulation for the velocity trajectory of the entire route subject to a time constraint.

1) Time constraint as driver input: the driver parameter \( \alpha \) is introduced. \( \alpha \) allows the driver to make a balanced choice between fast and economic driving. The requested travel time \( t_{driver} \) becomes:

\[ t_{driver} = t_{fast} - \alpha(t_{slow} - t_{fast}) \] (44)

In which \( \alpha \) is a driver input on the interval \([0, 1]\). \( t_{fast} \) is the shortest traveling time that can be obtained. For calculation of \( t_{fast} \) the upper constraints for every segment are used to solve (43), while for \( t_{slow} \) the lower constraints are used.

2) Optimization over several segments: the cost function is obtained by adding up the segment costs, (42), of all \( n \) segments. Solution of this optimization provides the constant velocity \( v_{cr} \), electric machine use on the coast part \( P_{em} \), start velocity of max. power deceleration \( v_d \) and end velocity \( v_e \) for each segment. Therefore a nonlinear optimization problem can be defined:

\[ \min \{ m_{f_{1}} + m_{f_{2}} + \ldots + m_{f_{n}} \} \] (45)

subject to:

\[ \{ v_{cr1}, v_{cr2}, \ldots, v_{crn} \} \]

\[ \{ P_{em1}, P_{em2}, \ldots, P_{emn} \} \]

\[ \{ v_{d1}, v_{d2}, \ldots, v_{dn} \} \]

\[ \{ v_{e1}, v_{e2}, \ldots, v_{en} \} \]

The problem is solved using the Matlab® function fmincon.

III. EXPERIMENTAL RESULTS

The highway route presented in Fig. 2, is used to indicate the fuel benefit of velocity trajectory optimization in a hilly environment. Two situations are evaluated on a chassis dynamometer, with 8 runs each: 1) standard CC use with constant velocity setpoint, 2) an adaptive optimized velocity ACC setpoint with the same time constraint as in case 1.

Fig. 4 shows the velocity trajectories, with dashed the (adaptive) CC setpoints, in solid dark the standard CC results are depicted and in solid gray the optimized results. The equivalent fuel consumption (corrected for SOC deviation) as function of time is depicted in Fig. 5. Typically, the optimized velocity trajectories obtain a fuel consumption benefit due to:

- downhill driving, by decreasing the vehicle velocity in front of the descent, and then to increase the vehicle
velocity during the descent. In this way potential energy is directly converted to kinetic energy. Converting potential energy into kinetic energy proves to be more beneficial than using the hybrid system to store it in the battery.

- a larger average velocity in the first part of the route, to create time for a longer period of regenerative braking/coasting. This longer period outweighs an increase in aerodynamic losses due to a higher constant velocity before the deceleration, in order to obtain an identical traveling time. The average measured fuel consumption benefit is approximately 5%.

IV. CONCLUSIONS AND FUTURE WORK

A velocity trajectory optimization method is presented that takes advantage of real-life geographical data, is adaptive for vehicle conditions like mass, and computes the optimal velocity trajectory for HEVs, with a computational load that is suitable for real-time implementation. It allows the driver to make a balanced choice between travel time and fuel consumption.

The computed velocity trajectory could be exploited by an adaptive cruise control system. The experimental results show a fuel consumption benefit of 5% due to velocity trajectory optimization compared to a standard cruise control with constant velocity setpoint. The results show that due to the limited efficiency of the hybrid system, conversion of potential energy into kinetic energy in this situation is preferred over storage in the battery.

Future work will focus on the use of different solvers for the optimization problem, and the integration with the vehicle’s real-time energy management.

V. ACKNOWLEDGMENTS

The research leading to these results has received funding from the ENIAC Joint Undertaking and from Senter-Novem in the Netherlands under Grant Agreement number 120009, and is part of a more extensive project in the development of advanced energy management control for urban distribution trucks which has been made possible by TNO Business Unit Automotive in cooperation with DAF Trucks NV.

The N.V. Westerschelde tunnel is acknowledged for supplying topographic data of the Westerschelde tunnel route.

Fig. 4: Velocity trajectories.

Fig. 5: Equivalent fuel consumption trajectories.

REFERENCES