Nonequilibrium rovibrational energy distributions of hydrogen isotopologues in an expanding plasma jet

O. Gabriel, J. J. A. van den Dungen, D. C. Schram, and R. Engeln

Department of Applied Physics, Eindhoven University of Technology, P.O. Box 513, 5600 MB Eindhoven, The Netherlands

(Received 16 December 2009; accepted 9 February 2010; published online 9 March 2010)

State resolved densities of high rovibrationally excited hydrogen isotopologues H$_2$, HD, and D$_2$ in the electronic ground state have been measured in a supersonically expanding plasma jet. The obtained state distributions differ substantially from thermal equilibrium. Moreover, the distributions are not the same for H$_2$, HD, and D$_2$ indicating different formation and relaxation rates for each isotopologue. Mechanisms for this deviation from a Boltzmann distribution are given and compared to hydrogen reactions in other environments. The difference between the measured highest occupied rovibrational states in H$_2$, HD, and D$_2$ is ascribed to an isotope effect in the dissociation process. © 2010 American Institute of Physics. [doi:10.1063/1.3352550]

I. INTRODUCTION

Hydrogen is the most abundant and simplest neutral molecule. Therefore, it is an often used subject in quantum mechanical models. Due to its vibrational ($v$) and rotational ($J$) energy levels in its electronic ground state $X^1\Sigma_g^+$, molecular hydrogen is important for the cooling of interstellar gas clouds, eventually resulting in the formation of stars and planets. While in the extremely cold regions of our cosmos, usually, only the lower energy levels of molecular hydrogen are occupied. In extremely hot regions, e.g., in an experimental fusion reactor, high rovibrationally excited states of hydrogen molecules have been found close to the reactor walls. Gas phase and surface reactions of atomic and molecular hydrogen also play a vital role in applications such as the deposition of ultrahard diamondlike films or microcrystalline silicon layers in thin film solar cell production, where hydrogen controls the crystallinity during the deposition process.

It has been shown that under low pressure conditions, surface association processes, e.g., on walls of a fusion reactor or the surface of interstellar dust grains, lead to high rovibrationally excited hydrogen molecules. These highly excited molecules transfer their internal energy to other molecules and atoms within the gas phase by inelastic collisions and chemical reactions. Cross sections depend strongly on the internal energy of the collision partners, thus the reaction dynamics is influenced by the internal energy and its distribution. Depending on the internal energy of the molecules, the corresponding rate coefficients can vary over several orders of magnitude. Therefore, understanding of the plasma chemistry requires a detailed knowledge of the internal energy distribution of molecules, which is very often deviating from thermal equilibrium, both in technological plasmas and in environments such as the interstellar medium.

A direct spectroscopic measurement of the distribution of the internal energy of rovibrationally excited hydrogen molecules is difficult. Transitions between rovibrationally excited states within the electronic ground states of homonuclear H$_2$ and D$_2$ are dipole-forbidden, while the heteronuclear HD molecules have only a very weak dipole moment. Furthermore, emission spectroscopy yields only densities of the upper states, and ground state densities can only be derived indirectly from collisional-radiative models.

We measured the distributions of the internal energy of H$_2$, HD, and D$_2$ molecules in their electronic ground states by means of vacuum ultraviolet (VUV)-laser-induced fluorescence spectroscopy. The high rovibrationally excited molecules were formed in a plasma source and detected in a supersonically expanding hydrogen jet directly after leaving the plasma source.

II. EXPERIMENT

A direct measurement of $X^1\Sigma_g^+$ state densities by excitation to electronically excited states requires radiation with an energy in the order of 10 eV, which has to be tunable over an energy range of several electronvolts with a bandwidth narrow enough to resolve individual transitions ($\approx 10^{-5}$ eV). We use stimulated anti-Stokes (AS) Raman scattering in hydrogen to produce simultaneously ten laserlike beams in the VUV. Every beam is shifted up in energy with respect to...
the pump beam by a multiple of the fundamental vibrational Raman shift of H$_2$, i.e., 4155.22 cm$^{-1}$. All beams are focused simultaneously into the vacuum chamber, where they excite hydrogen molecules via Lyman transitions (X $^1\Sigma_g^+ \rightarrow B$ $^1\Sigma_g^+$). The AS radiation has a bandwidth of 0.15 cm$^{-1}$ and covers a spectral range from 115 to 165 nm, i.e., about 2/3 of the spectral range of the Lyman band system of molecular hydrogen. By tuning the frequency of the pump beam, all ten AS-beams are scanned simultaneously; this multiplex scheme drastically decreases the recording time of the Lyman spectra and allows for simultaneous measurement of many (v, J) states of the three isotopologues. The fluorescence radiation due to spontaneous emission of the excited hydrogen molecules is collected by a mirror and focused onto a photomultiplier tube (PMT).

Analysis of recorded spectra is performed using transition energies and probabilities of H$_2$, HD, and D$_2$ Lyman lines provided by Abgrall and Roueff. A radiative model includes the excitation by AS beams and the de-excitation by spontaneous emission (X $^1\Sigma_g^+ \rightarrow B$ $^1\Sigma_g^+$) leading to a system of rate equations, which has been solved analytically. A fluorescence yield is calculated for each possible excitation taking into account the excitation rate, spontaneous and stimulated emission probabilities, optical properties of the spectrometer, and saturation effects. Other influences such as cascading processes from higher excited levels can be neglected because the measurement has been performed in the nonactive part of the plasma jet. Moreover, the time resolution of the PMT (around 1 ns) is high enough to resolve the emission peak (around 10 ns long) and to subtract any possible background signal.

The minimal detectable hydrogen state density depends on the fluorescence yield and is around 10$^{12}$ m$^{-3}$. This is, at least in the case of a hot hydrogen gas/plasma, low enough to detect rovibrationally excited hydrogen molecules with internal energies close to the dissociation limit at 4.5 eV internal energy. A lower limit for the detectable internal energy exists at 1 eV because the required radiation with wavelengths below 115 nm is blocked by the MgF$_2$ windows that are used to separate plasma chamber and VUV spectrometer.

Rovibrationally excited H$_2$, HD, and D$_2$ molecules are produced in a wall-stabilized thermal arc plasma source operated with 7 kW of dc power. A 50:50 mixture of H$_2$ and D$_2$ gas enters the arc channel of 4 mm diameter and 4 cm length at a total flow rate of 1.25 x 10$^{21}$ s$^{-1}$ (Fig. 1). Within the thermal plasma in the arc channel (p $\approx$ 9000 Pa and T $\approx$ 6000 K), almost all hydrogen molecules are dissociated, while H and D atoms recombine within the gas phase and associate at the surface of the channel and nozzle walls to hydrogen molecules. Rovibrationally excited H$_2$, HD, and D$_2$ molecules are leaving the plasma source through a straight nozzle (6-mm-long) with a 1:2:1 ratio of the total densities.

Using this type of nozzle and a chamber background pressure of 100 Pa, there is no light emission from the plasma jet due to H$_2$ Fulcher band or H atom Balmer line series, but only the emission due to the excitation by the laser AS beams. The plasma expands supersonically into a vacuum chamber, which is kept at a pressure of 100 Pa. The densities of rovibrationally excited hydrogen molecules are measured 8 mm downstream in the center of the plasma jet, i.e., in the supersonic part of the plasma expansion. A shock front is formed about 12 mm downstream, where the expansion undergoes a transition to subsonic, diffusion dominated flow.

### III. ROVIBRATIONAL DENSITY DISTRIBUTIONS OF H$_2$, HD, AND D$_2$

In the measured spectral range from 60 000 to 85 000 cm$^{-1}$, 170 recorded lines have been identified as Lyman transitions of H$_2$, 159 lines of HD and 65 lines of D$_2$, respectively. From measured line intensities, hydrogen state densities have been calculated in this work using the radiative model. The resulting state distributions of rovibrationally excited H$_2$, HD, and D$_2$ in the electronic ground state X $^1\Sigma_g$ are shown in the Boltzmann plots in Fig. 2, where the state densities n(v,J) divided by the statistical weight g(v,J) are plotted over the total internal energy.

The distributions differ from a Boltzmann distribution, i.e., the rotational states are not populated according to thermal equilibrium. This is more clear in Fig. 3, where only the rotational state densities for the vibrational state v=6 are shown, normalized to the density of the first rotational state J=0 of H$_2$, HD, and D$_2$, respectively. While the lower rotational states J$<7$ follow a temperature $T_{\text{low}}$ of several hundred Kelvin, the higher rotational states J$\approx8$ are distributed according to a rotational temperature $T_{\text{high}}$ of several thousand Kelvin. The temperatures have been derived from linear regression fits applied to the lower rotational state densities and higher rotational state densities, respectively, for each vibrational state v of H$_2$, HD, and D$_2$. However, it should be mentioned that the term “temperature” is not strictly defined in cases where the states are not populated according to thermal equilibrium. Therefore, we use it as a measure of the rotational distribution in certain rotational states (“low J” and “high J”). These derived temperatures are summarized in Table 1.

As shown in Fig. 2, the shape of the rotational distributions are similar in all detected vibrational states v in case of H$_2$ and D$_2$, while for HD the non-Boltzmann character of the rotational distribution is increasing with increasing vibrational states. HD is different from H$_2$ and D$_2$ in two ways; in contrast to H$_2$ and D$_2$ molecules, which are already in the feed gas, all HD molecules have to be newly formed in the
plasma source. Moreover, HD has a small dipole moment resulting in different selection rules for radiative and collisional transitions, leading to different excitation and relaxation processes.

Although the detection limit is around $10^{12} \text{ m}^{-3}$, $\text{H}_2$ molecules with internal energies of up to 4 eV were detected, which is only 0.5 eV lower than the dissociation limit. At the kinetic conditions inside the plasma jet (some 1000 K or 0.1 eV), these highly excited molecules are effectively dissociated, leading to anomalously high H and D atom densities.

The highest internal energy found for HD is lower around 3.5 eV, indicating an isotope effect on the dissociation rates as suggested in Ref. 10 and references therein. The distribution of $\text{D}_2$ molecules could be detected for internal energies up to 3 eV, where $\text{D}_2$ densities reach the detection limit of the setup.

IV. EXCITATION OF MOLECULAR HYDROGEN

Similar nonequilibrium distributions were found for $\text{H}_2$ in other kinds of gas discharges, but also for $\text{H}_2$ in the interstellar medium. However, despite the similarity in distributions, the proposed mechanisms leading to non-Boltzmann state distributions are very different. Lower rotational states of $\text{H}_2$ are, in interstellar media as well as in gas discharges, commonly believed to be populated according to the kinetic gas temperature of the medium. The kinetic temperature at the detection point within the plasma expansion, i.e., $z=8 \text{ mm}$ behind the nozzle exit of the plasma source, has been determined from the line widths of detected lines and was found to be very similar: 1600 ± 100 K in case of $\text{H}_2$, 1650 ± 100 K for HD, and 1800 ± 200 K for $\text{D}_2$, respectively. It is well known that the kinetic temperature is fast decaying within the supersonic expansion, implying even higher kinetic temperatures at earlier positions in the expansion and within the plasma source. This is interesting because the lower rotational states of $\text{H}_2$, HD, and $\text{D}_2$ are populated according to temperatures three times lower than the kinetic temperature, while the higher rotational states are populated according to higher temperatures (3000–4000 K).

It indicates that thermalization within the plasma gas phase is far from complete even for low $J$ states, at least for the detected vibrational states $v=2–8$.

Higher rotational states resemble a higher temperature, which has to be due to an additional pumping process. For interstellar media, this pumping is assumed to be due to surface association on dust grains, where the desorbing $\text{H}_2$ molecules have an additional internal energy up to 4.5 eV.

TABLE I. Parameters $T_{\text{low}J}$ and $T_{\text{high}J}$ for $\text{H}_2$, HD, and $\text{D}_2$ molecules derived from distributions shown in Fig. 2.

<table>
<thead>
<tr>
<th>Molecule</th>
<th>$T_{\text{low}J}$ (K)</th>
<th>$T_{\text{high}J}$ (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\text{H}_2$</td>
<td>700 ± 100</td>
<td>3800 ± 200</td>
</tr>
<tr>
<td>HD</td>
<td>500 ± 100</td>
<td>3400 ± 200</td>
</tr>
<tr>
<td>$\text{D}_2$</td>
<td>300 ± 100</td>
<td>3000 ± 200</td>
</tr>
</tbody>
</table>
FIG. 4. Rotational distribution of HD ($v=4$) measured at five different axial positions within the plasma jet.

electrons of low energy ($\approx 1$ eV) direct to higher rovibrational states within the $X^1\Sigma^+$ state (E-V process), or by electrons of higher energy ($\approx 10$ eV) via an excitation to the electronic excited states (E-V). The situation is different in the plasma source and in the plasma expansion used in this work, where the electron densities are not high enough and the temperatures are too low ($<1$ eV) for excitation of molecular hydrogen via E-V processes. Although an electron energy of about 1 eV is high enough for E-V excitation to lower ($v,J$) states, the high rotational excitation ($J>20$) found in this work cannot be explained by E-V processes due to a lack of a sufficient numbers of collisions.

Since the energy distribution of hydrogen at the end of the arc channel is thermal with high temperatures of several thousand Kelvin, an excitation process via surface association of H atoms at the copper walls of arc channel and nozzle has been proposed for H$_2$.\cite{16,21} which leads to H$_2$ in high $v$ and $J$ states.\cite{7,8} As visible in Figs. 2 and 3, the distributions are not the same for H$_2$, HD, and D$_2$. Both the lower and the higher part of the rotational distributions follow different temperatures indicating different formation and relaxation rates for each isotopologue. Taking into account that the kinetic temperatures are very similar for H$_2$, HD, and D$_2$, we assume that gas phase collisions are not responsible for the difference in rotational distribution, but the difference in surface association rates for the different isotopologues.

V. RELAXATION OF MOLECULAR HYDROGEN

The relaxation of the internal energy of rovibrationally excited hydrogen molecules in a plasma jet originates from surface collisions in the nozzle\cite{21} or from collisions in the gas phase of the plasma jet itself at larger distances from the source.\cite{26} In the latter case, the redistribution of the internal energy is due to molecule-molecule collisions, since atom, electron, and ion densities are orders of magnitude lower than that of the neutrals. The same effect has been measured for rotational states in vibrational state $v=4$ of HD molecules (Fig. 4). Compared to previous results on H$_2$,\cite{26} the relaxation of rotational states of HD is increasing with rotational states $J$ and becomes almost constant for $J \geq 8$.

With a simple model\cite{26} including cross sections calculated by Flower and Roueff,\cite{27} the relaxation of a H$_2$ gas at 5500 K and 6000 Pa via collisions of H$_2$ molecules with ground state H$_2(0,0)$ has been calculated (Fig. 5). This kind of relaxation leads to a non-Boltzmann shape of the distribution, as those shown in Fig. 2, but the necessary time of $4 \times 10^{-4}$ s is a factor of 100 higher than the available time within the jet between nozzle exit and the detection location. A more realistic modeling of the relaxation of internal energies would include state-to-state molecular collisions of H$_2$, HD, and D$_2$, but relevant cross sections have not been published in detail for high rovibrational states for any of the hydrogen isotopologues.\cite{11,13,27} However, the high densities of hydrogen molecules in highly excited rovibrational states in connection with the enhanced rate coefficients of gas phase $^+$ and surface reactions for these states emphasize the vital role of excited hydrogen molecules, both in neutral gas and plasma. Another possible extension of the model are molecule-atom collisions, which cannot be neglected at close distances towards the plasma source, since high dissociation degrees have been measured using this type of nozzle.\cite{16,21}

Another influence on the densities of high rovibrationally excited H$_2$ molecules could be the presence of low energetic electrons, which leads to dissociative attachment of excited molecules.\cite{10}

VI. CONCLUSIONS

The distribution of the internal energy of H$_2$, HD, and D$_2$ molecules has been measured in a plasma jet driven by a 50:50 mixture of H$_2$ and D$_2$ gas. A high amount of the H$_2$, HD, and D$_2$ molecules are high rovibrationally excited due to surface association processes within the plasma source. The distributions are not according to thermal equilibrium and vary for each isotopologue, indicating different production and relaxation rates. The distribution of the rotational energy shows a similar shape for H$_2$, HD, and D$_2$ and can be described by a low temperature of several hundred Kelvin for low lying rotational states, while higher rotational states follow a temperature of several thousand Kelvin. The relaxation of the internal energy within the plasma jet due to molecule-molecule collisions has been modeled. The resulting time scale is too long if only collisions with ground state molecules are included. This result shows that molecule-molecule collisions of highly excited hydrogen isotopo-
logues have to be included to model the relaxation. However, information on state resolved cross section data for these collisions is missing.

ACKNOWLEDGMENTS

This work is part of the research program of the Dutch Foundation for Fundamental Research on Matter (FOM). The work is also supported by the Euratom Foundation. Skillful technical assistance of M.J.F. van de Sande, J.J.A. Zeebregts, and H.M.M. de Jong is greatly appreciated.