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Citation for published version (APA):

Coupier, G., Kaoui, B., Podgorski, T., & Misbah, C. (2008). Noninertial lateral migration of vesicles in bounded Poiseuille flow. *Physics of Fluids*, 20(11), 111702-1/4. [111702]. <https://doi.org/10.1063/1.3023159>

DOI:

[10.1063/1.3023159](https://doi.org/10.1063/1.3023159)

Document status and date:

Published: 01/01/2008

Document Version:

Publisher's PDF, also known as Version of Record (includes final page, issue and volume numbers)

Please check the document version of this publication:

- A submitted manuscript is the version of the article upon submission and before peer-review. There can be important differences between the submitted version and the official published version of record. People interested in the research are advised to contact the author for the final version of the publication, or visit the DOI to the publisher's website.
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Noninertial lateral migration of vesicles in bounded Poiseuille flow

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(Received 22 July 2008; accepted 17 October 2008; published online 17 November 2008)

Cross-streamline noninertial migration of a vesicle in a bounded Poiseuille flow is investigated experimentally and numerically. The combined effects of the walls and of the curvature of the velocity profile induce a movement toward the center of the channel. A migration law (as a function of relevant structural and flow parameters) is proposed that is consistent with experimental and numerical results. This similarity law markedly differs from its analog in unbounded geometry. The dependency on the reduced volume ν and viscosity ratio λ is also discussed. In particular, the migration velocity becomes nonmonotonous as a function of ν beyond a certain λ . © 2008 American Institute of Physics. [DOI: 10.1063/1.3023159]

Flow of confined soft entities, such as vesicles (closed quasi-inextensible lipid membranes) or blood cells in the circulatory system and in microfluidic devices, is a problem of paramount importance with both fundamental and practical interests. While inertial effects can induce lateral migration of any flowing body in a channel,^{1–3} the ability of these soft entities to adapt their shapes under nonequilibrium conditions gives them the possibility to migrate transversally even at low Reynolds number. Transverse migrations induce non-uniform lateral distributions of the suspended entities, which has important consequences on the rheology of a confined suspension (e.g., the Fahraeus–Lindquist effect in blood vessels⁴), or should impact on transport efficiency in the various sorting microfluidic devices that are now being developed.⁵

Despite the considerable interest for transverse migration in many circumstances, there is, to our knowledge, yet no quantitative law that would allow one to relate the lateral migration velocity of a deformable entity flowing in a channel, even isolated, with its position, its mechanical properties, and the flow parameters. We propose a law for the case of a single vesicle placed in a bounded Poiseuille flow, from experiments in microfluidic devices as well as simulations based on the boundary integral method.

The behavior of vesicles under unbounded shear flow has been the subject of several theoretical^{6–10} and experimental^{11–13} studies. When the viscosity ratio between the inner and the outer fluids is small, vesicles perform a tank-treading dynamics where the orientation of the main axis of the vesicle is constant and the membrane undergoes a tank-treading motion. In a bounded Poiseuille flow, tank-treading vesicles experience a transverse force and reach the center where they assume a steady shape. The latter stage has been described in several papers.^{14–16} Migration in Poiseuille flows has been also reported on capsules,^{17–19} red blood cells,^{18,19} and drops.^{20,21} The latter seem to have a very dif-

ferent behavior: Depending on the viscosity ratio and the confinement, the reported equilibrium positions are not always on the centerline. In addition, a drop interface and a vesicle membrane are mechanically different: A vesicle has a constant surface area and its equilibrium shape is not a sphere in general. As a consequence of these intrinsic differences the vesicle shape under flow is described (in the co-moving frame), to leading order, by a nonlinear shape equation while a drop obeys a linear equation.⁸

Lateral migration has two distinct sources. (i) A wall-induced lift force.^{22–25} In agreement with the numerical and theoretical studies for simple shear flows,^{22,24} we showed recently that the migration velocity decreases like $1/y^2$, where y is the distance to the wall of the center of mass of the vesicle.²⁶ (ii) The nonconstant shear rate in a parabolic velocity profile (even unbounded) leads to a subtle interplay between the gradient of shear and the shape,²⁷ resulting in migration toward the center with a constant drift velocity except near the centerline. In a realistic channel, both effects coexist and we shall see that this leads to a new and non-trivial noninertial migration law.

The considered microfluidic channel is straight and has a rectangular cross section. The flow direction is Ox , and we investigate lateral migration along Oy . Let $2w$ denote the channel width in the y -direction, and v_0 the imposed flow velocity at the center of the channel in the absence of vesicle. The two walls are located at $y=0$ and $y=2w$.

A vesicle is characterized by two geometrical parameters: Its effective radius R_0 , determined from its constant volume $\mathcal{V}$ by $R_0=(3\mathcal{V}/4\pi)^{1/3}$, and its reduced volume $\nu=\mathcal{V}/[4\pi(S/4\pi)^{3/2}/3]$ (S is the constant area of the vesicle) characterizing vesicle deflation. Volumes are calculated at lift-off (see below) by assuming axisymmetric shape about the vesicle's main axis. The viscosity ratio is defined as $\lambda=\eta_{\text{in}}/\eta_{\text{out}}$, where η_{in} , η_{out} denote the inner and the outer viscosities. Relevant space and time scales are the vesicle radius R_0 and the characteristic time needed by the vesicle to relax to its equilibrium shape (in the absence of imposed flow),

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which is given by $\tau = \eta_{\text{out}} R_0^3 / \kappa$, where $\kappa \sim 20k_B T$ is the membrane's bending rigidity (typically, $\tau \sim 10$ s).

Therefore dynamics depends *a priori* on the four dimensionless parameters ($\hat{w} \equiv w/R_0$, $\hat{v}_0 \equiv v_0 \tau / R_0$, ν , λ). We consider first the case $\lambda \approx 1$. The strategy is to vary $\hat{w}$ and the imposed velocity $\hat{v}_0$ and investigate the migration law $\hat{y}(\hat{t}) = y(t/\tau)/R_0$ for each value of ν . Then we discuss the influence of ν and λ .

In the experiments, we used straight channels of height $h_0 = 66.6 \mu\text{m}$ (in the direction of gravity z) and width $2w$ (rectangular cross section) between 70 and $140 \mu\text{m}$. The walls of the channels are made of polydimethylsiloxane glued to a glass slide. The flow is induced by gravity, by connecting the inlet and the outlet to reservoirs at different heights. Vesicles are prepared following the electroformation method. They are made of a dioleoylphosphatidylcholine lipid bilayer enclosing an inner solution of sugar (sucrose or glucose) in water or in a 1:4 glycerol-water ($w:w$) mixture. Samples are diluted in a slightly hyperosmotic outer solution of the same type, in order to deflate them by osmosis. Dextran can be added to one of the solutions to modify the viscosity ratio λ . Vesicle size R_0 lies in the range of $7\text{--}37 \mu\text{m}$ while v_0 varies between 200 and $1100 \mu\text{m s}^{-1}$. Note that for our solutions of viscosity and density close to the one of water, the Reynolds number $Re = \rho v_0 R_0 / \eta_{\text{out}}$ is always lower than 4×10^{-2} .

A particular design of the upstream channel creates an initial condition where incoming vesicles touch the $y=0$ wall in the observation area and start to be lifted away from it. In particular, they have already developed a nearly ellipsoidal shape tilted with respect to the wall.^{23–25} The two-dimensional (2D) fluid velocity profile in the xy plane where their center of mass lies is nearly parabolic, since the rectangular cross section of the three-dimensional (3D) channel obeys $2w/h_0 \leq 3$.²⁸ Moreover, we wait for the flow to be established for a long time, resulting in preliminary centering of the vesicles in the z direction. The imposed velocity profile is thus written as $v_x^\infty(\mathbf{r}) = c(yw - y^2/2)$, where $c = 2v_0/w^2$ is the curvature. A vesicle is tracked along its trajectory with a phase contrast microscope, and the position y of its center of mass is determined by image processing, starting with $y(t=0) = y_0$, where y_0 is the position just before lift-off, which is close to R_0 .

The evolution with time of the y position of two vesicles with $\lambda = 1.1$ is shown in Fig. 1(a). The vesicles quickly move away from the wall, then the migration velocity decreases to zero as they approach the centerline. Along their trajectory, they continuously deform from a tilted ellipsoid to a symmetric bulletlike shape. For a given ν , the function $\hat{y}(\hat{t})$ depends *a priori* on both parameters $\hat{w}$ and $\hat{v}_0$. In order to determine this functional dependence, which is not known *a priori*, we rescale the time variable. The choice of a relevant time scale is not obvious, however. Indeed, while the inverse of the shear rate yields a natural scale, this is not an adequate choice since the shear rate is not constant along the trajectory. The trick is to rescale each infinitesimal time step dt around the time t by the local shear rate $\dot{\gamma}(y) = dv^\infty/dy = c(w - y)$ of the unperturbed flow at the position $y(t)$. The new dimensionless timelike parameter is then obtained by

FIG. 1. (Color online) (a) Experimental time evolution of the lateral position y for three vesicles of similar size ($19 \pm 1 \mu\text{m}$) and imposed flow velocity $v_0 = 920 \mu\text{m s}^{-1}$ but different ν and λ . The dashed line indicates the centerline (which will be reached much later by two of the vesicles). The solid line shows the $y(t)$ curve obtained from the fit by the numerical solution of Eq. (1). (b) Evolution of $\hat{y} - \hat{y}_0$ vs $\hat{t}$ for vesicles with $\lambda = 1.1$ and different ν . For each ν interval, the different symbols correspond to different vesicles, whose $\hat{w}$ and $\hat{v}_0$ vary in the explored intervals, that are $1.8 < \hat{w} < 9.6$ and $400 < \hat{v}_0 < 14\,800$. The corresponding curves clearly collapse on a single one. For clarity, the sets of curves corresponding to different ν intervals are switched vertically with an increment of 0.5.

integrating the rescaled time steps: $\tilde{t} = \int_0^t \dot{\gamma}(y) dt' = c \int_0^t [w - y(t')] dt'$. $\tilde{t}$ accounts for the history of the shear rates experienced by the vesicle along its trajectory. The raw data (not shown) for the migration velocity spread over more than a decade in the parameters space. Interestingly, as shown in Fig. 1(b), all experimental curves $\hat{y}(\tilde{t})$ for a given ν (or rather, a tiny interval around it) collapse, whatever the values of $\hat{w}$ and $\hat{v}_0$ within the explored range. A log-log plot (not shown) of each master curve $\hat{y}(\tilde{t}) - \hat{y}_0$ is linear, a clear signature of a power law behavior $\hat{y}(\tilde{t}) - \hat{y}_0 = \beta \tilde{t}^\alpha$, where the dimensionless parameters α and β are thus independent from $\hat{w}$ and $\hat{v}_0$. The lateral migration velocity $\hat{v}_m \equiv \dot{\hat{y}}$ as a function of the position $\hat{y}$ and ($\hat{w}, \hat{v}_0$) is then easily extracted,

$$\hat{v}_m = \xi \frac{\dot{\gamma}(\hat{y})}{(\hat{y} - \hat{y}_0)^\delta}, \quad \text{that is,} \quad \dot{y} = \xi \frac{R_0^{\delta+1} \dot{\gamma}(y)}{(y - y_0)^\delta}. \quad (1)$$

This law constitutes the central result of our finding. In the range $0.970 < \nu < 0.975$ we find for instance $\xi \equiv \alpha \beta^{1/\alpha} = 1.2 \times 10^{-2} \pm 0.2 \times 10^{-2}$ and $\delta \equiv 1/\alpha - 1 = 1 \pm 0.1$. The error bars for these coefficients are mainly due to the uncertainties on the measure of ν , of order ± 0.005 , since, as we shall see, the velocity depends on the reduced volume. Note that the differential equation (1) has no analytical solution but can be easily solved numerically and the result used to fit the raw data $y(t)$ without rescaling procedure [Fig. 1(a)].

In the simulations, we studied 2D neutrally buoyant vesicles (the 2D geometry captures the essential features)

FIG. 2. (Color online) Simulations. (a) Migration velocity $\hat{v}_m$ vs lateral position for different reduced volumes. Solid lines show the fits to Eq. (1). (b) log-log plot of $\hat{v}_m$ vs $\hat{y}-1$ for different $\hat{w}$ and $\hat{v}_0$ and $\nu=0.97$.

having no viscosity contrast ($\lambda=1$). The fluid flows inside and outside the vesicle are governed by the Stokes equations ($\mathbf{r}_m \in \partial\Omega$ is a membrane point)

$$-\nabla p(\mathbf{r}) + \eta \nabla^2 \mathbf{v}(\mathbf{r}) = -\delta(\mathbf{r} - \mathbf{r}_m) \mathbf{f}(\mathbf{r}), \quad \nabla \cdot \mathbf{v}(\mathbf{r}) = 0, \quad (2)$$

where p is the pressure, $\mathbf{v}$ is the velocity, and $\mathbf{f}$ the membrane force, given by Eq. (8) of Ref. 27. Thanks to the linearity of Eq. (2), we solve them using a boundary integral method²⁹ adapted to vesicle problems.^{7,24,27,30} The membrane velocity is then given by the following integral equation, which we solve numerically:

$$v_i(\mathbf{r}_m) = \frac{1}{4\pi\eta} \oint_{\partial\Omega} \mathbf{G}_{ij}^W(\mathbf{r}_m, \mathbf{r}') f_j(\mathbf{r}') ds(\mathbf{r}') + v_i^\infty(\mathbf{r}_m), \quad (3)$$

where $\mathbf{G}_{ij}^W$ is the Green's function for a fluid bounded by a steady infinite plane wall located at $y=0$,

$$\mathbf{G}_{ij}^W(\mathbf{r}, \mathbf{r}') = \mathbf{G}_{ij}(\mathbf{r} - \mathbf{r}') - \mathbf{G}_{ij}(\mathbf{r} - \mathbf{r}'_I) + 2r'_y \mathbf{G}_{ij}^D(\mathbf{r} - \mathbf{r}'_I) - 2r'_y \mathbf{G}_{ij}^{SD}(\mathbf{r} - \mathbf{r}'_I). \quad (4)$$

$\mathbf{G}_{ij}(\mathbf{r}) = -\delta_{ij} \ln r + (r_i r_j / r^2)$ is the Green's function for an unbounded fluid, or Stokeslet, $\mathbf{r}'_I = (r'_x, -r'_y)$ is the image of $\mathbf{r}'$ with respect to the wall. The function

$$\mathbf{G}_{ij}^D(\mathbf{r}) = (\delta_{ix} - \delta_{jy}) \left(\frac{\delta_{ij}}{r^2} - 2 \frac{r_i r_j}{r^4} \right) \quad (5)$$

is the Stokeslet doublet, and the source doublet is

$$\mathbf{G}_{ij}^{SD}(\mathbf{r}) = r_y \mathbf{G}_{ij}^D(\mathbf{r}) + (\delta_{ix} - \delta_{jy}) \frac{\delta_{iy} r_i - \delta_{ix} r_j}{r^2}. \quad (6)$$

The evolution of the vesicle's shape and location are obtained by updating every membrane point using a Euler scheme: $\mathbf{r}_m(t+\Delta t) = \mathbf{v}(\mathbf{r}_m, t) \Delta t + \mathbf{r}_m(t)$.

Note that we only consider one wall at $y=0$. Provided $\hat{w} \geq 8$, the vesicle reaches and stays on the $\hat{y}=\hat{w}$ line at long times, even without the symmetric wall at $\hat{y}=2\hat{w}$. This seems to indicate that for $\hat{w} \geq 8$, migration forces due to the curvature dominate over wall effects near the centerline.

The variations of $\hat{v}_m$ with $\hat{y}$ are shown in Fig. 2(a) for four different reduced volumes and given width and flow velocity. They are well described by Eq. (1). The adequation

FIG. 3. (Color online) Reduced migration velocity $\hat{v}_m$ of a vesicle at position $\hat{y}=4$ vs its reduced volume. For readability, the simulations data are uniformly rescaled by a factor ~ 0.1 .

to this law is confirmed by considering varying $8 < \hat{w} < 12$ and $600 < \hat{v}_0 < 800$. Following Eq. (1), it is convenient to rescale the migration velocity in such a way that it should not depend either on $\hat{w}$, nor on $\hat{v}_0$: $\tilde{v}_m \equiv \hat{v}_m / \hat{y}(\hat{y}) = \xi / (\hat{y} - \hat{y}_0)^\delta$. The variations of $\tilde{v}_m$ with $\hat{y}-1$ are shown in Fig. 2(b) for $\nu=0.97$. The collapse on a single line (in log-log scale) is in agreement with Eq. (1). We find $\delta \approx 0.8 \pm 0.1$ and $\xi \approx 0.1$. The agreement between experiments and simulations regarding the exponent δ is quite satisfactory. However, numerical studies overestimate the amplitude ξ . This is attributed to the 2D character (actually a translationally invariant form in the z direction), causing an enhancement of the lift force. While 2D simulations have captured some interesting facts, a 3D simulation is necessary before drawing general conclusive answers, and we plan to investigate this problem in the future.

We now discuss the dependencies on ν and λ ; for all the values of ν and λ explored here, the experimental and numerical curves are still very well fitted by the law given by the resolution of Eq. (1) [see Fig. 1(a)]. Values for $\tilde{v}_m$ at $\hat{y}=4$ are reported on Fig. 3. For $\lambda \approx 1$, in the ranges $0.83 \leq \nu \leq 1$ and $0.89 \leq \nu \leq 0.99$ offered, respectively, by the experiments and the simulations, we find an increasing migration velocity with decreasing ν [as seen on Fig. 2(a)].

Results for higher λ are available from the experiments. The new feature is the nonmonotonous behavior of $\tilde{v}_m$ as a function of ν . When ν is decreased from 1, the migration velocity first increases (as for $\lambda=1.1$), then reaches a maximum and decreases back to a very low value (Fig. 3).

This nonmonotonous behavior of the velocity can be understood on a general physical basis. A spherical vesicle ($\nu=1$), does not migrate owing to the fore-aft symmetry. On the other hand, when ν decreases, the vesicle finally switches from a tank treading to a tumbling motion.¹² In the latter regime, no global migration should occur either because the averaging over the different orientations of the vesicle during one rotation period leads to an almost symmetrical configuration. From these considerations we infer a maximal velocity at a given value of ν . Note that when $\lambda \approx 1$, no tumbling motion occurs whatever ν , so that a monotonous evolution of the velocity with ν is observed. The evolution with ν and λ is in qualitative agreement with the predictions made by Olla²² for the migration velocity of a (shape preserving ellipsoidal)

vesicle in the case of a simple shear flow bounded by a wall, although the scaling is different.

In conclusion, our experiments and simulations yield a similarity law for the lateral migration velocity of a vesicle in a bounded Poiseuille flow as a function of its distance to the walls and to the centerline, its effective radius, the channel's width, and the flow velocity. We showed that the effects of the walls and of the curvature of the velocity field are coupled in a nonlinear manner: Curvature not only induces migration²⁷ but also affects the shape and orientation, which affects the lift force. The law $v_m \sim \dot{\gamma}(y)/y$ markedly differs from what the naive extrapolation of the results for a vesicle near a wall and in a linear shear flow would give $v_m \sim \dot{\gamma}(y)/y^2$.

Deflating a spherical vesicle increases its deformability, thus its asymmetry under shear, and leads to higher migration velocities. However, beyond a given viscosity ratio, the tank treading to tumbling transition is approached when the deflation increases, and the migration velocity undergoes a decline which can be understood on the ground of general symmetry considerations.

The authors thank G. Danker and V. Vitkova for fruitful discussions, P. Ballet for technical assistance, and CNES and ANR (MOSICOB) for financial support. Financial support from the PAI Volubilis (Grant No. MA/06/144) is acknowledged. G.C. acknowledges a fellowship from CNES. B.K. acknowledges Ph.D. financial support from the CNRS (Grant No. b4/015).

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