Microscopic model for ultrafast magnetization dynamics of multisublattice magnets

Citation for published version (APA):

DOI:
10.1103/PhysRevB.87.020407

Document status and date:
Published: 01/01/2013

Document Version:
Publisher’s PDF, also known as Version of Record (includes final page, issue and volume numbers)

Please check the document version of this publication:
• A submitted manuscript is the version of the article upon submission and before peer-review. There can be important differences between the submitted version and the official published version of record. People interested in the research are advised to contact the author for the final version of the publication, or visit the DOI to the publisher’s website.
• The final author version and the galley proof are versions of the publication after peer review.
• The final published version features the final layout of the paper including the volume, issue and page numbers.

Link to publication

General rights
Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

• Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
• You may not further distribute the material or use it for any profit-making activity or commercial gain
• You may freely distribute the URL identifying the publication in the public portal.

If the publication is distributed under the terms of Article 25fa of the Dutch Copyright Act, indicated by the “Taverne” license above, please follow below link for the End User Agreement:
www.tue.nl/taverne

Take down policy
If you believe that this document breaches copyright please contact us at:
openaccess@tue.nl
providing details and we will investigate your claim.

Download date: 19. Apr. 2019
Microscopic model for ultrafast magnetization dynamics of multisublattice magnets

A. J. Schellekens and B. Koopmans

Department of Applied Physics, Center for NanoMaterials (cNM), Eindhoven University of Technology, P.O. Box 513, 5600 MB Eindhoven, The Netherlands

(Received 29 October 2012; revised manuscript received 6 December 2012; published 25 January 2013)

We introduce a microscopic model to describe the ultrafast response of magnetic materials with two sublattices to heating by a femtosecond laser pulse. Even though the model is based on a set of simple Hamiltonians, it readily reproduces experimental observations such as ultrafast reversal of ferrimagnets and delayed demagnetization of one sublattice in ferromagnetic alloys. The calculations give insight into the microscopic mechanisms and thermodynamics governing the complex dynamics of these multisublattice magnets.

DOI: 10.1103/PhysRevB.87.020407 PACS number(s): 75.78.Jp, 75.60.Jk, 75.50.Gg, 75.50.Bb

Controlling the magnetic state of ferromagnetic materials by femtosecond laser pulses has drawn significant attention from the scientific community since the first pioneering experiments by Beaurepaire et al.1 In these experiments it was shown that the magnetization of ferromagnetic nickel can be quenched on subpicosecond time scales. This discovery lead to intense theoretical2–9 and experimental10–16 investigations on the origin of these ultrafast magnetization dynamics, however, the dominant microscopic mechanism is still under debate.

Parallel to the research on the dynamics of homogeneous ferromagnets, more exotic materials were being investigated. A breakthrough in the field was made by Stanciu et al.17 who have shown that the direction of the magnetization of the sublattices in the ferrimagnetic alloy GdFeCo can be changed by the use of a femtosecond laser pulse and a small applied field. Recently, the origin of this magnetization reversal has been unraveled by separately measuring the dynamics of the Gd and FeCo sublattices.18 It was concluded that a different heating efficiency of the two sublattices puts the system in a strong nonequilibrium state, making it possible for the magnetization to switch its orientation. This result was corroborated by further experiments and atomistic spin simulations, showing that even without an external field the mutual orientation of the sublattices can be switched,19 paving the way for all optical recording.

Recently, it was shown that also the magnetic moments of Ni and Fe in permalloy show strong nonequilibrium dynamics after pulsed laser excitation.20 Element-specific measurements show that the demagnetization of Ni is delayed with respect to Fe, which is a surprising observation considering the large hybridization of the electronic states around the Fermi level in permalloy. This begs the question what microscopic processes govern these different dynamics and under which conditions they occur.

In this Rapid Communication, we derive a model describing the longitudinal relaxation of magnetic materials with two sublattices. The main difference between existing methods in the literature21,22 is that it is based on microscopic scattering Hamiltonians. Our approach finds its origin in the microscopic 3 temperature model (M3TM),23 which describes three interacting subsystems of (spinless) electrons, phonons, and \( S = 1/2 \) spin excitations. We extend the model to \( S = N/2 \), introduce more than one spin system, and drop the restriction that the spin systems are in internal equilibrium. First the response of a ferrimagnetic material is investigated, where the two sublattices are aligned antiparallel. Experimentally observed switching of the sublattices through a transient ferromagnetic state is readily reproduced. Second, the same model is applied to permalloy, where the Fe and Ni sublattices are coupled ferromagnetically. It is demonstrated that, under certain assumptions, a delay in the demagnetization of one of the sublattices can be observed indeed, again corresponding to the experimental observations. The nature of the assumptions reveals important information on the microscopic processes governing ultrafast magnetization dynamics in these strongly coupled ferromagnetic alloys.

The equations of motion we derive are aimed to be the simplest microscopic description of a multisublattice magnet, but accurate enough to keep contact with experimental observations. To this end, while we treat separate spin subsystems, for simplicity we let them interact with only one common electron system, which is assumed to be a noninteracting Fermi sea of spinless fermions with a constant density of states \( D_F \) around the Fermi level. The phonon bath is described by a Debye model, i.e., by assuming a linear dispersion relation for \( D_p \) phonon modes up to a cutoff energy \( E_D = k_B T_D \). The two spin systems \( m_i \) are described by \( 2S + 1 \) discrete energy levels that are split by an energy \( J_{ex} \), where \( S \) is the spin quantum number. This yields the following Hamiltonians for the electron, phonon, and \( i \)th spin systems, respectively:

\[
H_{ex} = \frac{1}{ND_f} \sum_k \frac{k^2}{2m} c_k^\dagger c_k, \tag{1}
\]

\[
H_p = \sum_q \hbar \omega_q \left( \frac{1}{2} + a_q^\dagger a_q \right), \tag{2}
\]

\[
H_{s,i} = J_{ex,i} \sum_j S_{z,j,1,j}, \tag{3}
\]

where \( c_k^\dagger \) (\( c_k \)) describes the creation (annihilation) of an electron in the state \( k \), \( a_q^\dagger \) (\( a_q \)) are similar operators for phonons in the state \( q \), \( D_{s,i} \) is the average atomic spin density, and \( S_{z,j,1,j} \) is the \( z \) spin operator.

For the spin system a Weiss mean-field approach is used, where the exchange splitting of the discrete energy levels is
given by

$$J_{\text{ex},1} = \frac{(\gamma_{1,1}m_1 + \gamma_{1,2}m_2)}{S_1}, \quad (4)$$

$$J_{\text{ex},2} = \frac{(\gamma_{2,2}m_2 + \gamma_{1,2}m_1)}{S_2}, \quad (5)$$

where $m_1$ and $m_2$ are the normalized magnetizations of the two sublattices, and $\gamma_{1,1}$, $\gamma_{2,2}$, and $\gamma_{1,2}$ are the Weiss molecular field constants, which are related to the intra- and intersublattice exchange energies, respectively. When $\gamma_{1,2}$ is positive (negative) the sublattices are ferromagnetically (antiferromagnetically) coupled.

To describe the interactions between the subsystems the contributing scattering Hamiltonians have to be introduced. First of all, it is assumed that $e-e$ and $p-p$ scattering are instantaneous, hence the $e$ and $p$ systems are in internal equilibrium at all times. Second, $e-p$ scattering is taken into account within the random-$k$ approximation. Like in the M3TM, phonon-assisted Elliott-Yafet spin flips couple the spin system to the electronic heat bath, transferring the angular momentum between the spin and phonon subsystems. Finally, exchange scattering is added, where in an interband $e-e$ scattering event angular momentum is transferred between the two magnetic sublattices. This yields the following scattering Hamiltonians:

$$\mathcal{H}_{\text{ep}} = \frac{\lambda_{\text{ep}}}{N} \sum_{k} \sum_{k'} \sum_{q} D_{kq}^{i} c_k^\dagger (a_q^\dagger + a_q), \quad (6)$$

$$\mathcal{H}_{\text{ep},i} = \frac{\lambda_{\text{ep},i}}{N_{3/2}} \sum_{k} \sum_{k'} \sum_{q} \sum_{q'} D_{kq}^{i} D_{k'q'}^{i} c_k^\dagger (a_q^\dagger + a_q)(s_{i,j,+} + s_{i,j,-}), \quad (7)$$

$$\mathcal{H}_{\text{ex}} = \frac{\lambda_{\text{ex}}}{N^3} \sum_{k} \sum_{k'} \sum_{k''} \sum_{v} \sum_{w} \sum_{v'} \sum_{w'} D_{k1}^{i} D_{k2}^{i} D_{k3}^{i} c_k^\dagger c_{k'}^\dagger c_{k''}^\dagger (s_{1,+,-} v_{1,-,-} + s_{1,-,+} v_{1,+,-}), \quad (8)$$

where $s_{i,j,+}$ is a raising (lowering) operator for the $v$th spin of the first spin system, $\lambda_{\text{ep}}$ and $\lambda_{\text{ex}}$ the matrix elements for $e-p$ and exchange scattering, and $\alpha_{\text{ep},i}$ is the probability of a phonon-mediated Elliott-Yafet spin flip.

FIG. 1. (Color online) Schematic overview of the model. (a) Energy flow between the subsystems. (b) Flow of the angular momentum between the subsystems. Due to exchange scattering, the angular momentum can be transported between the two magnetic sublattices. Both sublattices can exchange angular momentum with the lattice by $e-p$ scattering, (c) Spin-flip event due to $e-e$ scattering, transferring angular momentum from one sublattice to the other. (d) Change of occupation of the discrete energy levels due to the exchange scattering event depicted in (c).
microscopic parameters are given in Table I. We would like to stress that these parameters are very realistic for ferromagnetic materials and similar to the ones reported earlier. Finally, the laser pulse is assumed to have a Gaussian profile with a standard deviation of 50 fs.

Figure 2(a) displays the resulting equilibrium magnetization as a function of temperature. The symbols are the equilibrium values obtained by solving the derived differential equations for $T_c = T_p = T_{\text{ambient}}$, whereas the lines are calculated using the Weiss model. The molecular field constants are chosen such that the compensation temperature $T_{\text{comp}}$ of the ferrimagnet is slightly larger than room temperature, as in the first experiments. In Figs. 2(b) and 2(c) the typical time evolution of the electron (phonon) temperature $T_e (T_p)$ and the magnetic moments on the sublattices are displayed, respectively, however, in the calculations exchange scattering is neglected by setting $\lambda_{\text{ex}}$ to zero. Just as in the experiments, the sublattice with the strongest exchange coupling and smallest magnetic moment, $M_1$, demagnetizes more rapidly. This is in line with predictions of the original M3TM, where the demagnetization rate is proportional to the intrasublattice exchange and inversely proportional to the atomic magnetic moment.

Next, in contrast to the calculation in Fig. 2(c), exchange scattering is turned on, allowing for an angular momentum transfer between the subsystems. The corresponding calculations, while keeping other microscopic parameters fixed, are displayed in Fig. 2(d). The main difference from Fig. 2(c) is that the demagnetization rates of both sublattices are enhanced significantly due to the extra transport channel for the angular momentum. While the electron temperature is larger than $T_c$, one would expect that the magnetization of the sublattices would be fully quenched. However, an unexpected ferromagnetic alignment of the sublattices is observed. Since $M_1$ (originally in the negative direction) demagnetizes more rapidly than $M_2$, it reaches zero while $M_2$ still has a relatively large (positive) magnetic moment. $M_2$ will now be further quenched by exchange scattering, however, this inevitably leads to a slightly positive value of $M_1$ and thus a temporary ferromagnetic state. When the electron system cools below $T_c$ due to equilibration with the phonons after $\approx 1$ ps, the magnetization of the sublattice coupled most strongly to the electrons, i.e., $M_1$, starts growing to larger positive values. Then, finally, the antiferromagnetic coupling with $M_2$ acts as the driving force to switch the orientation of $M_2$ from positive to negative.

In the model one parameter is introduced that cannot be easily obtained from experiments, which is $\lambda_{\text{ex}}$. To show that switching does not depend strongly on this parameter but is in fact very robust, we plot the switching time as a function of laser fluence and $\lambda_{\text{ex}}^2$ in Fig. 2(e). The switching time is defined as the delay time where $M_1$ and $M_2$ cross. Switching is observed if $\lambda_{\text{ex}}^2$ is sufficiently large, and the laser fluence is larger than a certain threshold value. The range where switching occurs is reasonably large, and for every value of $\lambda_{\text{ex}}^2/\lambda_{\text{ex},0}^2 > 0.2$ there is a fluence where the sublattices change their mutual orientation. For fluences larger than 1 (arb. units) the final temperature after laser pulse excitation is larger than $T_c$, hence no switching occurs.

After verifying that ultrafast switching of antiferromagnetically coupled sublattices can be described by the presented model, we will investigate the magnetization dynamics of two ferromagnetically coupled sublattices as recently studied experimentally by Mathias et al. Here it was shown that the quenching of the (average) magnetic moment on the Ni atoms in permalloy is delayed with respect to the moments on the Fe atoms. To calculate the magnetization dynamics of permalloy with the introduced model, the exchange coupling between the sublattices is assumed to be ferromagnetic. Furthermore, because the electronic states around the Fermi level of Ni and Fe are strongly hybridized, it is assumed that the inter- and intrasublattice exchange interactions are identical, giving the same temperature dependent equilibrium properties of the sublattices.

For the calculations a fictitious ferromagnetic alloy resembling permalloy is used, which is an 80-20 mixture of Ni ($M_1$) and Fe ($M_2$) with a Curie temperature of 800 K. The spin-flip rate of $M_1$ is chosen to be four times smaller than that of $M_2$, hence without any exchange coupling between the sublattices $M_1$ demagnetizes four times slower due to $e$-$p$ scattering. The other microscopic parameters used, which are chosen to be very similar to the ferrimagnetic case, are given in Table I.

---

**Table I. Microscopic parameters used in the calculations.** The magnetic parameters are mentioned in the main text.

<table>
<thead>
<tr>
<th></th>
<th>$D_F$</th>
<th>$D_p$</th>
<th>$D_4$</th>
<th>$T_D$</th>
<th>$\lambda_{ep}$</th>
<th>$\lambda_{ex,0}$</th>
<th>$\alpha_{sf}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ferrimagnet</td>
<td>3/eV</td>
<td>3</td>
<td>1/1</td>
<td>400 K</td>
<td>20 meV</td>
<td>25 meV</td>
<td>0.1</td>
</tr>
<tr>
<td>Ferromagnet</td>
<td>3/eV</td>
<td>3</td>
<td>0.8/0.2</td>
<td>400 K</td>
<td>20 meV</td>
<td>70 meV</td>
<td>0.1</td>
</tr>
</tbody>
</table>

---

**FIG. 2.** (Color online) (a) Equilibrium magnetic moments of the sublattices of the fictitious ferrimagnet as a function of temperature. The lines are calculated using the self-consistent mean-field approach, whereas the symbols represent the equilibrium values in the Boltzmann scattering equations. (b) Electron and phonon dynamics for the fluence used in (c) and (d). (c) Ultrafast demagnetization of the sublattices neglecting exchange scattering. (d) Ultrafast demagnetization for the same microscopic parameters as in (c), but allowing for an angular momentum transfer between the sublattices by exchange scattering. (e) Switching time as a function of fluence and the matrix element for exchange scattering.
Results of the calculations are displayed in Fig. 3, where the magnetizations of the sublattices $M_1$ and $M_2$ are plotted as a function of time after laser pulse excitation. Note that it is assumed that heating by the laser pulse is instantaneous, heating the electron system to 1600 K at $t = 0$. The calculations show that for the parameters used, $M_2$ and $M_1$ demagnetize at approximately the same rate, but $M_1$ is delayed with respect to $M_2$. This is in full agreement with the experimental results. The same mechanism as in the ferrimagnetic alloy is at play, i.e., transfer of the angular momentum between the subsystems by exchange scattering brings the total system closer to equilibrium, slowing down the demagnetization of $M_2$ but increasing the demagnetization rate of $M_1$ until both rates are approximately equal.

To exemplify this delayed demagnetization, the normalized magnetizations $(M - M_{\text{min}})/(M_0 - M_{\text{min}})$ of both sublattices are plotted on a semilogarithmic scale in the inset of Fig. 3.

The data is fitted by the following simple model:

\[
\frac{dm_1}{dt} = -\frac{m_1}{\tau_1} - \frac{D_{m1} m_1 - m_2}{\tau_{\text{ex}}},
\]

\[
\frac{dm_2}{dt} = -\frac{m_2}{\tau_2} - \frac{D_{m2} m_2 - m_1}{\tau_{\text{ex}}},
\]

where $\tau_1$ and $\tau_2$ are the time constants for demagnetization of the two individual sublattices, while $\tau_{\text{ex}}$ is the time scale of the exchange interaction. Note that this fit function is almost identical to the one used by Mathias et al., except the fraction of the atomic spin densities is added to the exchange interaction term, as the total angular momentum should be conserved in the exchange scattering process. It can be observed from the inset of Fig. 3 that the simple model fits the data reasonable well, and $\tau_{\text{ex}} = 44 \pm 2$ fs is obtained from the fits. Furthermore, $\tau_1/\tau_2$ is found to be $\approx 4$. We can thus conclude that the derived microscopic model shows similar dynamics to the experimental ones when assuming that the magnetic moments of the Ni atoms are less strongly coupled to the electronic system compared to Fe. The origin of such a difference, which is rather unexpected due to the large hybridization of the electronic system, remains to be elucidated.

To conclude, we have introduced a simple microscopic model to describe the ultrafast dynamics of magnetic materials with ferro- or antiferromagnetically coupled sublattices. Both ultrafast switching of a ferrimagnet and the magnetization dynamics of a strongly hybridized ferromagnetic alloy are readily reproduced by using realistic values for the microscopic material parameters. Although within the present Rapid Communication we only discussed two cases where the two spin sublattices are associated with different atomic positions, our approach is much more general, and can be extended easily to cases with more sublattices, or sublattices representing different orbitals on the same atom. Treating the coupled dynamics of $d$ and $f$ magnetic moments in rare-earth ferromagnets would provide an intriguing example thereof.

This work was supported by the Foundation for Fundamental Research on Matter (FOM), which is part of the Netherlands Organization for Scientific Research (NWO).

---