Description of a pin-pulling process with aid of dimensional analysis

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Description of a Pin-Pulling process with aid of dimensional analysis.

Prof. dr. ir. H.L. Muller
Ir. W.Th. Kregting
Dr. J. Smit

The total process of pin-pulling consists of two main processes.
1. The thermal behaviour of an electrically heated piece of wire clamped on both ends.
2. The construction occurring when the wire is overstretched, and many interrelated effects such as change in dimension because of plastic flow, change in heat intensity resulting in different temperature-time relations at different places. Direct mathematical analysis is very difficult; therefore an empirical approach is used, whereby the test results are processed for practical application by means of dimensional analysis. The following process-description shows a way to determine the required current, warming-up time and tensile force for different materials. Though the experiments have been performed in the sphere of the factory practice and thus could not get that kind of attention that is usual for laboratory tests, the question if it is possible to describe this process with aid of dimensional analysis seems answered to us quite well in the affirmative.
DESCRIPTION OF A PIN-PULLING PROCESS
WITH AID OF DIMENSIONAL ANALYSIS

by

PROF. DR. IR. H.L. MULLER
IR. W. TH. KREGTING
DR. J. SMIT

TECHNOLOGICAL UNIVERSITY EINDHOVEN
HOLLAND

Presented to the C.I.R.P. conference 1967
by P.C. Veenstra
Materialien.

Obgleich die Versuche unter Betriebsverhältnissen durchgeführt wurden, und daher keine labormäßige Aufmerksamkeit in Anspruch nehmen konnten, haben die Aussichten auf eine dimensionsanalytische Beschreibung dieses Prozesses sich unseres Erachtens verhältnismäßig gut bestätigt.

**Sommaire**

Le procédé de "pin-pulling" se compose de deux processus principaux:

1. la conduite thermique d'une pièce de fil chauffée électriquement et fixée par serrage à deux côtés.
2. la contraction se présentant en cas que le fil sera surtendu et beaucoup d'effets se tenant se produisent, comme modification de dimension en conséquence de fluidité plastique, modification d'intensité de chaleur, concentrant en temperature-temps relations différentes à places différentes.

L'application de l'analyse mathématique directe est difficile; pour cette raison une méthode empirique est choisie pour les résultats d'essai applicables pratiquement, et bien l'analyse dimensionnelle.

Le procédé concernant fait voir une voie de fixer le courant requis, le temps de chauffage et la force de tension pour des matériaux différents.

Bien que les expériences sont faites au milieu de l'organisation d'atelier, impliquant que cela n'appelle pas l'attention désirée pour les résultats, la question de la possibilité de résoudre ce procédé à l'aide de l'analyse dimensionelle doit être répondu affirmativement.
Summary

The total process of pin-pulling consists of two main processes:

1. The thermal behaviour of an electrically heated piece of wire clamped on both ends.
2. The construction occurring when the wire is overstretched, and many interrelated effects such as change in dimension because of plastic flow, change in heat intensity resulting in different temperature-time relations at different places.

Direct mathematical analysis is very difficult; therefore an empirical approach is used, whereby the test results are processed for practical application by means of dimensional analysis. The following process description shows a way to determine the required current, warming-up time and tensile force for different materials.

Though the experiments have been performed in the sphere of the factory practice and thus could not get that kind of attention that is usual for laboratory tests, the question if it is possible to describe this process with aid of dimensional analysis seems answered to us quite well in the affirmative.

Zusammenfassung

Der gesamte Stift-Ziehprozess setzt sich zusammen aus zwei wichtigen Teilvorgängen,

1. dem thermodynamischen Verhalten eines elektrisch geheizten Drahtstückes, dass mit beiden Seiten eingeklemmt ist.
2. der eintretenden Einschnürung bei stossartiger Überbelastung des Dratstücks und mehreren damit zusammenhängenden Effekten, wie z.B. plastische Massenänderung und örtliche Unterschiede in der Heizwirkung, woraus sich von Ort zu Ort ungleiche Temperatur-Zeitbeziehungen ergeben.

Eine unmittelbare mathematische Analyse ist mit grossen Schwierigkeiten verbunden; daher wurde versuchsmässig an die Aufgabe herangetreten.

Die Versuchsergebnisse wurden mittels Dimensionsanalyse für praktische Verwendung zugänglich gemacht. Die Prozessbeschreibung zeigt eine Möglichkeit zur Bestimmung des erforderlichen Stromes, der Erwärmungsdauer und der benötigten Zugbelastung für verschiedene
Introduction

In the electronic component industry pins are widely used as parts for radio tubes and transistors. The pins vary in diameter from 0.2 to 2.0 mm and in length from 8 to 72 mm. If they are to be handled by vibratory hoppers and inserting equipment, the pins must meet the following requirements:
- The pin must have pointed ends and a sufficiently smooth point surface.
- Length variation of the pin must be limited (normal tolerance ± 0.2 mm).

Drawing of a pin is shown in fig. 1.

These pins can be manufactured by various methods such as cutting, rolling and pulling. Of these three methods the last will be dealt with more in detail. The machine used for pulling apart the wire, works on the following principle: A length of wire is clamped between two chucks that can be moved in relation to each other. A current is passed via the chucks through the wire as a result of which its temperature will increase. The heated wire is stretched and separated by moving the chucks apart.

Two different processes are involved, viz.
- a. The thermal behaviour of an electrically heated piece of wire clamped on both ends.
- b. The constriction occurring when the wire is overstretched.

The two processes are interrelated by a number of effects such as change in dimension because of plastic flow, change in heat intensity resulting in different temperature-time relations at different places.

For different products the material and pin dimensions are given within certain limits.

The practical problem was to find
1. the optimal conditions for the process
2. a practical way to bring the machine setting as close as possible to these conditions.

First the stretching process will be studied; the results will then be worked out to dimensionless numbers. With help of these numbers the setting of the machine in practical cases can be done more systematically.
The method chosen to solve the problem

As was already outlined above, the total process consists of many interrelated effects. Direct mathematical analysis is very difficult; therefore an empirical approach is used, whereby the test results are processed for practical application by means of dimensional analysis.

Readers are referred concerning this method to lit. 1, 2.

The use of dimensional analysis for a practical problem depends on the hypothesis that its solution can be expressed in terms of certain variables by means of a homogeneous (dimensional) equation. This hypothesis is based on the trivial fact that physical equations are homogeneous in dimension and that relations can be deduced from these equations and must therefore be homogeneous in dimension too.

However, if an equation is homogeneous in dimension, it can be reduced to a relation between a complete set of dimensionless products (Buckingham theorem). It is obviously necessary that an adequate physical model is used in which all important relevant factors are taken into consideration.

The physical model

Constriction of the wire begins once the stress has exceeded a certain critical value. This stress is temperature dependent and, generally speaking, it may be said that the required critical stress decreases with increasing temperature. As the temperature reaches a maximum in the plane of symmetry, the critical value will be exceeded first in this plane. The physical quantities determining the temperature at a certain place are:

a. the power supplied $P$

b. the dissipated heat $Q$

c. the heat capacity $C$

If we now consider the total length of wire between clamping points and simplify the situation by using average values of temperature etc., then the power supplied

$P_{\text{tot}} = I^2R = \frac{I^2/\rho \cdot L}{\pi/4 \cdot d^2}$

will depend on

1. $\rho I^2$ with $\rho =$ electrical resistivity

2. $I$ with $I =$ current

3. $d$ with $d =$ wire diameter
For the purpose of finding dimensional quantities this simplification may be justified. The wire temperature is considered to be only variable with x and the time t.

The dissipated heat for an element in the middle of the wire \( (Q = \lambda . A . dT . t) \) will depend on \( \frac{dx}{dx} \)

1. \( \lambda \) with \( \lambda = \text{heat conductivity} \)
2. T \( T = \text{temperature of the middle of the wire} \)
3. t \( t = \text{warming-up time} \)
4. l \( l = \text{distance between the chucks} \)
5. d \( d = \text{wire diameter} \)

The constriction is determined by
1. the deformation energy / unit volume \( E \)
2. the tensile strength at \( T^\circ C \) \( \sigma_T \)

\[ E = \frac{F}{A} \cdot \varepsilon \]

The deformation energy depends on:
1. \( F \) with \( F = \text{applied force} \)
2. \( A \) \( A = \text{surface of a plane, perpendicular on the wire} \)
3. \( \varepsilon \) \( \varepsilon = \text{strain} \)

In considering these simplified equations, we supposed to have the following variables to be of importance for our dimensional analysis.

1. \( I^2 \) in Watt.m \( \text{M.L}^{-3}.T^{-3} \)

   It is permissible to combine \( I \) with \( \rho \), because they are the only variables containing the electrical basic units of charge for current.

2. \( E = \text{deformation energy / unit volume in Nm/m}^3 \)

   \( \text{M.L}^{-1}.T^{-2} \)

3. \( C = \text{heat capacity / unit volume in Nm/m}^3.\text{C} \)

   \( \text{M.L}^{-1}.T^{-2}.\theta^{-1} \)

4. \( \lambda = \text{heat conductivity in Nm/msec}^\circ \text{C} \)

   \( \text{M.L}.T^{-3}.\theta^{-1} \)

5. \( d = \text{wire diameter in m} \)
6. \( l = \text{distance between the chucks in m} \)
7. \( T = \text{temperature of the middle of the wire} \)
8. \( t = \text{warming-up time in sec} \)
9. \( \sigma_T = \text{tensile strength of the wire at } T^\circ \text{C} \)

\( \text{M.L}^{-1}.T^{-2} \)
Table 1. Dimensional matrix of the variables

<table>
<thead>
<tr>
<th>E</th>
<th>$\rho I^2$</th>
<th>t</th>
<th>T</th>
<th>d</th>
<th>C</th>
<th>$\lambda$</th>
<th>1</th>
<th>$\sigma_T$</th>
</tr>
</thead>
<tbody>
<tr>
<td>mass</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>length</td>
<td>-1</td>
<td>3</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>-1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>time</td>
<td>-2</td>
<td>-3</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>-2</td>
<td>-3</td>
<td>0</td>
</tr>
<tr>
<td>temperature</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>-1</td>
<td>-1</td>
<td>0</td>
</tr>
</tbody>
</table>

From these variables the following complete set of dimensionless products can be formed.

$$V_1 = \frac{\lambda t}{C I^2}$$

$$V_2 = \frac{\lambda T I^2}{\rho I^2}$$

$$V_3 = \frac{1}{d}$$

$$V_4 = \frac{F}{A \sigma_T}$$

$$V_5 = \frac{\rho I^2 t}{F I^2}$$

The following physical significance can now be given to the dimensionless numbers.

- $V_1$ = dissipated heat / heat capacity
- $V_2$ = dissipated heat / generated heat
- $V_3$ = geometrical proportion
- $V_4$ = force applied / force required
- $V_5$ = energy supplied / mechanical energy

In order to determine the relations between these numbers, it will be necessary to measure some variables by tests on the production machines.

From the literature (see lit. 3 and lit. 4) we derive the following as a function of temperature.

1. the specific electrical resistivity
2. the specific heat
3. the heat conductivity
4. the tensile strength at temperature $T$
The other variables are measured at the machine. The following five materials are at our disposal.

1. Nickel
2. Nickel-Iron 50/50
3. Nickel plated Iron
4. Copper + 2% Ag
5. Molybdenum

All with a diameter of 1 mm.

Tabel 2. Results of measurement

<table>
<thead>
<tr>
<th></th>
<th>Nickel</th>
<th>Nickel-Iron 50/50</th>
<th>Nickel-Plated Iron</th>
<th>Copper + 2% Ag</th>
<th>Molybdenum</th>
</tr>
</thead>
<tbody>
<tr>
<td>I av. Amp.</td>
<td>396</td>
<td>240</td>
<td>297</td>
<td>1131</td>
<td>707</td>
</tr>
<tr>
<td>F N</td>
<td>80</td>
<td>70</td>
<td>70</td>
<td>75</td>
<td>110</td>
</tr>
<tr>
<td>T °C</td>
<td>572</td>
<td>607</td>
<td>465</td>
<td>310</td>
<td>705</td>
</tr>
<tr>
<td>t sec.</td>
<td>0.08</td>
<td>0.08</td>
<td>0.08</td>
<td>0.04</td>
<td>0.04</td>
</tr>
<tr>
<td>C.10^6 Nm/m^3°C</td>
<td>4.63</td>
<td>4.58</td>
<td>5.02</td>
<td>3.74</td>
<td>2.78</td>
</tr>
<tr>
<td>λ Nm/msec°C</td>
<td>50.2</td>
<td>21.4</td>
<td>42</td>
<td>369</td>
<td>113</td>
</tr>
<tr>
<td>ρ.10^8 kg/m^3</td>
<td>36.5</td>
<td>11.5</td>
<td>53</td>
<td>88</td>
<td>23.3</td>
</tr>
<tr>
<td>σ_T.10^6 N/m^2</td>
<td>250</td>
<td>350</td>
<td>250</td>
<td>88</td>
<td>240</td>
</tr>
<tr>
<td>1.10^3 m</td>
<td>2</td>
<td>1.94</td>
<td>1.94</td>
<td>2.0</td>
<td>2.24</td>
</tr>
</tbody>
</table>
Dimensionless numbers that are useful in practice

The dimensionless numbers $V_1$ to $V_5$ incl. are calculated for the five materials mentioned above and are shown in the table below.

Table 3. Values of the dimensionless numbers

<table>
<thead>
<tr>
<th></th>
<th>$V_1$</th>
<th>$V_2$</th>
<th>$V_3$</th>
<th>$V_4$</th>
<th>$V_5$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ni</td>
<td>0.218</td>
<td>2.00</td>
<td>0.463</td>
<td>0.40</td>
<td>14.3</td>
</tr>
<tr>
<td>NiCr</td>
<td>0.1</td>
<td>0.732</td>
<td>0.515</td>
<td>0.246</td>
<td>19</td>
</tr>
<tr>
<td>Fe</td>
<td>0.178</td>
<td>1.58</td>
<td>0.515</td>
<td>0.356</td>
<td>14.1</td>
</tr>
<tr>
<td>Cu</td>
<td>0.986</td>
<td>12.2</td>
<td>0.5</td>
<td>1.08</td>
<td>5.0</td>
</tr>
<tr>
<td>Mo</td>
<td>0.325</td>
<td>3.42</td>
<td>0.446</td>
<td>0.33</td>
<td>8.4</td>
</tr>
</tbody>
</table>

Represented on log-log paper the relations between

- $V_4$ and $V_5$, fig. 3
- $V_2$ and $V_5$, fig. 4
- $V_1$ and $V_2$, fig. 5 are linear.

Simple graphical means deliver the following relations.

- $V_4 = 5.4 V_5^{-1}$
- $V_2 = 271 V_5^{-2}$
- $V_1 = 0.13 V_5^{0.8}$

Substitution in the equations leads to the following expressions.

\[
\frac{F}{A \sigma_T} = 5.4 \left(\frac{21 \mu T}{F^2}ight)^{-1}
\]

\[
\frac{\lambda_1 l^2}{T^2} = 271 \left(\frac{21 \mu T}{T^2}ight)^{-2}
\]

\[
\frac{\lambda_1}{C l^2} = 0.13 \left(\frac{\lambda_1 l^2}{\rho l^2}\right)^{0.3}
\]
The variables occurring in the above relations are:

1. \( \lambda = \lambda(T) \)  o  7. \( I \)  
2. \( C = C(T) \)  o  8. \( A = \pi/4 \, J^2 \)  
3. \( \rho = \rho(T) \)  o  9. \( F \)  
4. \( \sigma_T \)  o  10. \( t \)  
5. \( T \)  o  11. \( I \)  
6. \( I \)  

As a practical example of the use of experimental data the following may serve.

The starting point is wire of a certain diameter. What values must the current, the warming-up time, the tensile force and the distance between the chucks have to obtain the desired shape of the pointed ends? If we proceed from wire with a given diameter, as in our case, the magnitudes marked with \( * \) are given. If we, moreover, assume that the temperature as measured is the only one at which the process can properly take place, the temperature i.e. the magnitudes marked with 0 are also determined.

However, we still have three equations and three unknown variables, so we can calculate \( F, t \) and \( I \) as a function of the diameter.

We find:  
\[ I = I(d) \text{ from fig. 6} \]
\[ F = F(d) \quad \text{" fig. 7} \]
\[ t = t(d) \quad \text{" fig. 8} \]

The results of the above data with \( \frac{1}{2} \approx 0.5 \) are given below.

Table 4. \( F, t \) and \( I \) as a function of the diameter

<table>
<thead>
<tr>
<th>I in Amp.</th>
<th>( t ) in sec.</th>
<th>( F ) in N</th>
<th>( d ) in mm</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ni</td>
<td>428 d</td>
<td>7.41 ( 10^{-2} ) d</td>
<td>98 ( J^2 )</td>
</tr>
<tr>
<td>NiFe</td>
<td>243 d</td>
<td>7.93 ( 10^{-2} ) d</td>
<td>77 ( d^2 )</td>
</tr>
<tr>
<td>Fe</td>
<td>322 d</td>
<td>7.25 ( 10^{-2} ) d</td>
<td>23.34 ( d^2 )</td>
</tr>
<tr>
<td>Cu</td>
<td>1110 d</td>
<td>3.52 ( 10^{-2} ) d</td>
<td>141 ( d^2 )</td>
</tr>
<tr>
<td>Mo</td>
<td>747 d</td>
<td>3.91 ( 10^{-2} ) d</td>
<td>108 ( d^2 )</td>
</tr>
</tbody>
</table>
Discussion of the results

From this limited amount of measuring points, it cannot be expected that more accurate proportions can be determined between the dimensionless numbers. The graphical working out for that purpose has to be limited to the primary stage. Moreover, the values for $\sigma$ in the various text books vary rather considerably.

Nevertheless in practice these numbers give some improvement over the trial and error method applied up till now.

Conclusion:

The foregoing dimensional analysis has shown a way to determine the required correct cutting up time and tensile force of different materials. In order to increase the inaccuracy in the data available up till now, more experimental work of the type described has to be performed to come to sufficient accurate results.

In this further set of investigations, it will be necessary not only to increase the number of materials, but also to vary the diameter.

It may turn out that with these materials a useful shape of the pointed tools can also be obtained at temperatures other than those at which the experiments were done. However, this could not be verified from the results taken from the available production machine, which was not at all intended for fundamental experiments.

Rupture tests on machines built specifically for experiments, may be useful for this purpose.
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Fig. 1  Product drawing.

Fig. 2  Empirically determined ideal shape of the pointed ends.
Fig 3. The relation between the dimensionless numbers $V_4$ and $V_5$. 

\[ V_4 = \frac{F}{A \sigma_0} \]
\[ V_5 = -\frac{\rho I^2 t}{F d^2} \]
Fig 4. The relation between the dimensionless numbers $V_2$ and $V_5$.

\[
V_2 = \frac{\lambda T l^2}{\rho F l^2}
\]

\[
V_5 = \frac{\rho l^2 t}{F l^2}
\]
Fig. 5 The relation between the dimensionless numbers $V_1$ and $V_2$.

\[ V_1 = \frac{\lambda \tau}{C L^2} \]
\[ V_2 = \frac{\lambda \tau L^2}{\rho l^2} \]

\[ \tan \alpha = 0.815 \]
Fig. 6. The relation between the current $I$ and the diameter $d$. 

Ni $I = 428$ d
Ni-Fe $I = 245$ d
Fe  $I = 322$ d
Cu  $I = 1110$ d
Mo  $I = 747$ d

$d$ in mm.
$I$ in Amp
Fig 7 The relation between the tensile force \( F \) and the diameter \( d \).
Fig. 9. The relation between the warming-up time $t$ and the diameter $d$. 

The graph shows the relationship between the warming-up time $t$ in seconds and the diameter $d$ of various materials, including Ni-Fe, Ni, Fe, Mo, Cu, and Mo. The equations for each material are as follows:

- Ni: $t = 0.0741 d^2$
- Ni-Fe: $t = 0.0793 d^2$
- Fe: $t = 0.0725 d^2$
- Cu: $t = 0.0352 d^2$
- Mo: $t = 0.0391 d^2$