Abstract—Plug-in electric vehicle (PEV) is gaining steadily preference among consumers as they offer economically viable and environmentally friendly transportation solutions when compared to their gasoline powered counterparts. A decent charging station network coverage has been identified as the main enabler for the adoption of PEV. Therefore, the availability of ultra-fast charging station (UFCS) is not only a technical prerequisite but also a key enabler for the consumer acceptance to bring the electric mobility to the next level. To facilitate the smooth integration of UFCS in the existing power grid, hence rapid uptake rate of PEV, this article elaborates on the analytical derivation of the norton equivalent for the study of harmonic resonance when several UFCSs are connected to the local medium voltage (MV) grid. The impedance of norton equivalent model explicitly represents the input admittance of power converter under small signal perturbation. A case study is performed on the Dutch Bronsbergen MV grid to which 10 UFCSs are connected and its impact on the grid resonance point is shown with harmonic distortion calculation.

I. INTRODUCTION

PEV is gaining steadily preference among consumers as they offer economically viable and environmentally friendly transportation solutions when compared to their gasoline powered counterparts. Despite improved travel range offered by popular PEV models (e.g. Tesla Model S, Nissan Leaf, General Motor Bolt etc.) the battery charging facility nowadays does not offer the same level of convenience for the PEV owners as opposed to the extensive gasoline station network. Even though the level 1 household plug can easily refill the battery over the night, it does not offer the PEV owner the freedom for long distance travel and “range anxiety” free feeling. The Tokyo electric power company (TEPCO) study published in 2008 and BMW research project “Mini E” conducted in the cities of Los Angeles, Berlin, and London [1] both confirm that the public charging infrastructure such as the ultra-fast charging station (UFCS) plays a key role in the development of the electromobility and transition towards E-mobility travel routine. In a report [2] revealing the historical lessons learnt from Norwegian experience in the deployment of electric vehicle, a decent charging station network coverage has been identified as the main enabler for the adoption of PEV. Therefore, the availability of UFCS is not only a technical prerequisite but also a key enabler for the consumer acceptance to bring the electric mobility to the next level. Recognizing the need for UFCS, numerous literatures investigated the methodology to find the optimal UFCS locations taking into account the spatial and temporal transportation behaviour [3], the service range in combination with the power network constraint [4][5], and the installation cost in specific cases such as Barcelona [6] and Iran [7]. While the optimal location of UFCS present only one side of the equation, the successful deployment of UFCS highly depends on the existing grid hosting capability since the UFCS provides level 3 off-board DC charging slot (output power range from 90kW to 240kW) as specified by the Association of Automotive Engineers (SAE) imposing potential risk of congestion and violation of voltage in the local medium voltage (MV) grid. Stochastic load flow is the typical approach to identify the potential grid voltage profile violation and component overloading in the UFCS integration study as elaborated in [8][9][10][11][12]. Two case study on the Italian MV distribution network is presented in [13][14] suggesting viable mitigation measures such as an UFCS with stationary battery storage. Next to the static analysis for the integration of UFCS, the transient dynamic analysis of UFCS grid integration is also studied in the [15][16]. Despite a paper found on the power quality issues of UFCS, it is only limited to the typical North American residential building level power quality improvement using the UFCS as an innovative multilevel transformerless Hybrid Series Active Filter[17]. To the best knowledge of the author, the impact of UFCS on the MV grid harmonic resonance is not addressed in previous literatures, hence deserve a detailed investigation. A UFCS offering several level 3 charging slots connecting to the MV grid could easily reach MW (250kW x 4) level, its harmonic emission to the MV grid should be assessed. The widespread deployment of UFCSs with an active front end (AFE) can also adversely impact the local MV grid impedance resonance point causing hazardous harmonic resonances threat to the distribution network operators (DNOs). This article focuses on the proper modelling of UFCS with an AFE in the harmonic resonance study and provide additional system impact analysis via a study case of MV grid in Bronsbergen, the Netherlands.
II. UFCS TOPOLOGY AND MODEL

A vast amount of Innovative UFCS converter topologies exists in the literatures as well as the manufacture product offers [18]. When the AFE is directly coupled to the MV grid, three level neutral point clamp [19], cascaded H-bridge [20], matrix [21] inverter topologies are found in the literatures for the active front end realization whilst galvanic isolation is provided by a dual active bridge DC/DC stage interfaced to the PEV battery. When the galvanic isolation is provided by the low frequency MV/LV power transformer, 2-level AFE and its variation are common design approach reported in literatures [22][23]. To ease the impact of UFCS surge current on the power grid, stationary battery storage provides the necessary buffer [24][25][18] with possible application specific bundling options such as: superconducting magnetic energy storage [26], flywheel [27], and supercapacitor bank [28]. For this study, it is not possible to capture all the aforementioned UFCS topologies reported in the literatures. To illustrate the impact of a typical future UFCS on the power grid resonance behaviour, a simple 2-level AFE with stationary battery storage topology is chosen for this study due to its prevailing presence in the literature and technology readiness for the mass production. Fig. 1 demonstrates the generic UFCS topology for this study, where the active front end (1MW) is coupled to the medium voltage grid via a 10/0.4 kV transformer while each level 3 charging slot (250 kW x 4) is connected to the UFCS DC link via a DC/DC converter. The stationary battery storage device is then connected to the UFCS DC link via a dedicated DC/DC converter to reduce the static impact (power grid congestion, component overloading etc.) of UFCS on the local medium voltage grid. Once the generic UFCS topology is determined, an electromagnetic transient (EMT) model of the UFCS can be built in EMTDC/PSCAD V4.6.2 to study its impact on the MV grid to which it connects. Since the UFCS transient dynamic electrical characteristic seen from the power grid is mainly dictated by the AFE, for the EMT model the DC side charging slot and stationary battery storage DC/DC circuit is simplified to an ideal DC current source connected to the DC link of AFE grid side inverter as shown in Fig.2. For this paper, the EMTDC/PSCAD model built for UFCS is only to confirm the AFE controller parameters, based on which the input admittance of AFE is analytically derived in section III-B. The main control and electrical parameter

III. VSC MODEL FOR HARMONIC ANALYSIS

This section starts with a short introduction on the evolution of the power system harmonic distortion calculation and the associated harmonic source model, followed by a discussion
of the issues related to the ideal current source model. Then
the state-of-the-art modelling approach (i.e converter harmonic
model) in representing the input admittance of VSC is given.

A. Background on the harmonic modelling development

The typical method used for the modelling of harmonic-generating
devices is the ideal (constant) current source model. This
approach originated from times when the line commutated
harmonic-generating devices (i.e. load-commutated converters
and diode rectifiers) dominated. It has since been proven
to be inaccurate for the modelling of self-commutated
devices (e.g. VSC high voltage direct current station, doubly-
fed induction generator, photovoltaic, full converter based
wind turbine, UFCS). Even though it is common practice
to measure harmonic current emission at the grid connection
point, such harmonic current emission measurements should
not be used for the representation of VSC based power elec-
tronics as an equivalent ideal current source in the harmonic
resonance analysis [29], as will be substantiated next. The rea-
sons are three folds: firstly, the measurement is not performed
in a clean grid environment, i.e. without background harmonic
distortion. Secondly, an ideal current source fails to capture the
converter control reaction to the background harmonic voltage.
Lastly, for the network impedance scan, an ideal current source
does not present the frequency dependent inner current control
loop and the passive output filter resulting in an inaccurate
network resonance point estimation.

B. Derivation of VSC input-admittance

Frequency domain approach is proposed by the researchers
to represent VSC devices with its input admittance charac-
teristics seen from the AC grid. Early papers published on
the frequency domain input admittance representation of VSC
device has proven to be effective, as the theoretical calculation
demonstrate close agreement with the kW range laboratory
setup validation results. [30] presents the input admittance
derivation of a single phase inverter using only PI control for
the inner current control loop, while [31] advances analysis
to consider a typical three phase grid-connected VSC with
the typical dq synchronous frame control strategy for its
inner current control loop. [32] and [33] further elaborates on
the influence of PLL in the determination of VSC input admittance
characteristic. For the analysis of UFCS, when its PLL is designed with typical low bandwidth, the non-
linear effect of PLL on the grid side VSC input admittance
can be omitted without causing significant errors [33]. Therefore in this paper, we calculates the VSC
input admittance characteristics via analytical transfer function
derivation without considering the PLL effect. For the VSC
converter, its inner current loop transfer function with PLL
impact can be represented as Fig. 3 [33]:

![VSC close loop continuous transfer function diagram](image)

**Fig. 3. VSC close loop continuous transfer function diagram**

C. Converter Impedance Model without PLL Effect

The transfer function without considering the PLL impact
can be first shown as in Fig.4:

![VSC close loop continuous transfer function diagram without PLL](image)

**Fig. 4. VSC close loop continuous transfer function diagram without PLL impact**

For its close loop transfer function, the following equations
can be written:

\[-v_f Y_{ip}(s) - i_{inv} G_{ic}(s) G_d(s) Y_{op}(s) = i_{inv}\]

(1)

\[-i_{inv} - i_{inv} G_{ic}(s) G_d(s) Y_{op} = v_f Y_{ip}(s)\]

(2)

The input admittance of VSC can be determined by solving
(1) and (2) for the \(G_tcl(s) = \frac{-v_f}{-i_{inv}}\) when the current control
reference is maintained the same (i.e. \(i_{ref_{dq}} = 0\) and PLL
effect is not considered (i.e. \(\Delta \theta = 0\)):

\[G_{tcl}(s) = \frac{\frac{v_f}{-i_{inv}}}{-i_{inv}}|_{\Delta \theta = 0, i_{ref_{dq}} = 0} = \frac{G_{ic}(s) G_d(s) Y_{op}(s) + 1}{Y_{ip}(s)}\]

(3)
$G_{ic}(s)$ depicts the proportional resonance controller in $s$ domain:

$$G_{ic}(s) = K_p + \frac{2K_i\omega_c}{s^2 + 2\omega_c s + \omega_0^2}$$  \hspace{1cm} (4)$$

$G_d(s)$ indicates one an half sampling cycle delay caused by the digital computation and the PWM zero-order hold effect respectively [34]:

$$G_d(s) = e^{-1.5T_s s}$$  \hspace{1cm} (5)$$

$Y_{ip}(s)$ and $Y_{op}(s)$ are the admittance of inverter side inductor:

$$Y_{ip}(s) = Y_{op}(s) = \frac{1}{L_1 s + R_1}$$  \hspace{1cm} (6)$$

Applying the parameters from Table I, then the VSC input admittance $G_{tcl}(s)$ shown as norton equivalent (red in Fig. 5(a)) can be plotted in bode diagram (Fig. 5(b)), where inverter side inductor plus the VSC control is shown in blue and inverter side passive inductor frequency characteristic alone is shown in orange. The harmonic current emission from UFCS on the inverter side of inductor is taken from PSCAD simulation and shown in Fig. 5(c), where switching harmonics side bands are clearly visible at the integer times of PWM switching frequency (i.e. 5kHz = 100$^{1th}$ harmonic order)

IV. HARMONIC RESONANCE ANALYSIS IN DUTCH MV GRID

A typical Dutch MV grid in Bronsbergen (Fig. 6) operated by Alliander (Dutch DNO) has been selected for the case study to reveal the potential harmonic resonance risk in the case of massive UFCS grid integration. The UFCSs are connected at the MV bus 12 (Roelofs), where its downstream LV grid is represented in detail.

The impedance sweep is calculated at MV bus 12 (Roelofs) for two scenarios: base case without UFCS connection, 10 UFCS connections with the converter harmonic model. Fig. 7 presents the results of the impedance sweep (blue-base case without the UFCS connection, red-10 UFCS connections with the converter harmonic model). It is clear from the impedance sweep results that the original network resonance point (i.e 1600 Hz) will shift towards 1250 Hz as a result of the UFCS connections despite positively damped resonance peak thanks to the wide control bandwidth of the UFCSs. The new harmonics resonance point at 1250 Hz can be triggered by the characteristic harmonics produced by the 12 pulse variable speed drive.

To illustrate the point, a 12 pulse variable speed drive harmonic current profile taken from field measurement (as shown in Fig. 8) was used. Ideal current source representing the harmonic profile of 10 such 12 pulse variable speed drives are connected via a 10/0.4 kV transformer to the MV grid (blue dashed line in Fig. 6).

Reading from the harmonic voltage distortion calculation results at MV bus 12 (Roelofs) in Fig. 9, it is clearly visible that the characteristic current emission from the 12 pulse variable speed drives got amplified in the case of massive UFCSs integration (blue bar in Fig. 9) in comparison to the base case value (red bar in Fig. 9). Henceforth, when it comes to future integration of UFCS, DNO shall carefully assess the new grid resonance point as a result of UFCS grid integration, and it is of high importance to shift the new grid resonance point away from the characteristic harmonic emissions (e.g. 5th, 7th, 11th, 13th, 23th, 25th etc).

V. CONCLUSIONS AND RECOMMENDATIONS

This article discusses a harmonic resonance risk when a VSC based power converter, such as a UFCS, is introduced in a MV grid. The massive integration of UFCS in the future can possibility shift the original network frequency to the point that coincides with the characteristic harmonics emission from typical 12 pulse motor-drive as illustrated in the Dutch MV grid
case study. The proposed converter harmonic model, compared to the ideal current source approach, delivers the required level of insight for the distribution network operators (DNOs). Future work will focus on benchmarking the harmonic distortion calculation results obtained from powerfactory based on the converter harmonics model with the detailed PSCAD model on the same study case.

REFERENCES
