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Particle-in-cell Monte Carlo simulations of an extreme ultraviolet radiation driven plasma

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A self-consistent kinetic particle-in-cell model has been developed to describe a radiation driven plasma. Collisions between charged species and the neutral background are represented statistically by Monte Carlo collisions. The weakly ionized plasma is formed when extreme ultraviolet radiation coming from a pulsed discharge photoionizes a low pressure argon gas. The presence of a plasma close to optical components is potentially dangerous in case the ions that are accelerated in the plasma sheath gain enough energy to sputter the optics. The simulations predict the plasma parameters and notably the energy at which ions impact on the plasma boundaries. Finally, sputter rates are estimated on the basis of two sputtering models.

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I. INTRODUCTION

To meet the semiconductor industries continuous demand for printing ever-smaller structures on silicon wafers, future lithographic tools are designed to operate using extreme ultraviolet (EUV) radiation in a 2% bandwidth around the central wavelength of 13.5 nm. Since no material is sufficiently transparent to EUV radiation, refractive optics cannot be used and instead multilayer coated mirrors are required [1].

Additionally, as the mean free path of EUV radiation at atmospheric pressures is very short, the whole optical path is contained in a vacuum system. The residual argon background gas at a pressure of 0.1 to 1 Pa, is (partially) photoionized by the EUV radiation, creating a weakly-ionized plasma. The EUV radiation is generated by a hollow cathode discharge [2,3], which generates EUV pulses of approximately 100 ns duration at a repetition rate of typically 1 kHz. Consequently, the plasma will show strong time dependence.

As a result of the low plasma density ($n_e \approx 10^{15} \text{ m}^{-3}$) recombination will occur predominantly on the walls of the tool. Like in any bounded plasma, a plasma sheath will develop in which the ions will be accelerated towards the vessel walls. The plasma is potentially dangerous to the optical elements in case the ions gain enough energy to damage the multilayer mirrors through physical sputtering. A plasma model is applied to calculate the flux and energy of the ions impacting on the mirror.

The low plasma density and the strong time dependence imply that the plasma is far from equilibrium. Furthermore, at such a low pressure the plasma is in the nonlocal regime and a kinetic model is needed for an accurate description. Particle-in-cell (PIC) kinetic models provide a way to self-consistently calculate the fields and the energy and velocity distributions, without the need for equilibrium assumptions

[4,5]. Collisions can be represented statistically by combining PIC methods with Monte Carlo collisions (MCC) [6].

II. DESCRIPTION OF THE MODEL

The plasma is simulated using a PIC Monte Carlo code, which is one dimensional in configuration and three dimensional in velocity space. Electrons and argon ions are computationally represented by “superparticles.” Each superparticle corresponds to typically 10^9 real particles. The computational grid divides the plasma into a number of cells. Each cell must contain at least 100 particles to ensure proper statistics.

The PIC scheme will be described only briefly as this is well documented elsewhere [4,5]. The general scheme of the explicit PIC model is shown in Fig. 1. For each time step Δt we have the following:

- (i) Charges are assigned to the nodes of the computational grid by a linear weighing, the so-called cloud-in-cell scheme [7].
- (ii) The Poisson equation is solved to obtain the electric field at the nodes.
- (iii) To determine the force on each particle a linear weighing is applied to find the electric field at each particle position.

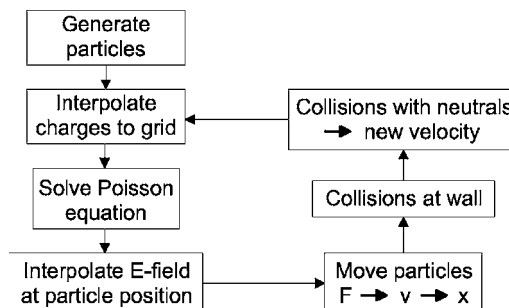


FIG. 1. Particle-in-cell scheme.

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(iv) The Newton equations of motions are applied to advance the position and velocity of the particles. Positions and fields are defined at integral time levels whereas velocities are defined at half-integral time levels.

(v) Particles that have moved beyond the boundaries of the computational grid are removed.

(vi) The MCC routine checks if a particle has collided and adjusts the velocity accordingly.

A. Monte Carlo collisions

In the model, charged particles collide with neutrals only. Because of the low plasma density, collisions between charged particles can be neglected. A collision is treated here as an instantaneous process that only changes the particle's velocity. Assume that the particle species have N types of collisions with the background gas. The total collision cross section $\sigma_T(E)$ is the sum

$$\sigma_T(E) = \sum_{i=1}^N \sigma_i(E), \quad (1)$$

where E is the kinetic energy of the incident particle and $\sigma_i(E)$ the cross-section for the i th type of collision. The flight time between collisions depends on the background density $n(x)$ and the energy and is equal to the inverse of the collision frequency ν

$$\nu(x, E) = n(x) \sigma_T(E) \sqrt{\frac{2E}{m}}, \quad (2)$$

with m the incident particle mass. The probability $P(t)dt$ that a particle will experience a collision within an infinitesimal time interval dt after having traveled through the background gas for a time t is

$$P(t)dt = \nu \exp(-\nu t)dt. \quad (3)$$

To determine when a collision takes place we have to integrate Eq. (3) along the particle trajectory. Numerically this is very time consuming because the background density and the kinetic energy of the particle change along its path and we have to calculate ν after each time step Δt of the PIC loop. Therefore, we use a numerical trick called "null collision method" [6] to speed up the calculations. Hereto, an extra collision type is introduced, which has a cross section such that, when added to Eq. (1), results in a total collision frequency with a constant value ν_m

$$\nu_m = \max_{x, E} \left\{ n(x) \sigma_T(E) \sqrt{\frac{2E}{m}} \right\}. \quad (4)$$

In our case the plasma is only weakly ionized with a homogeneous background density and we only have to obtain the maximum over E . The extra collision type is called "null collision" as no real interaction occurs. To obtain the time t_m to the next collision we integrate the right-hand side of Eq. (3) from zero to t_m replacing ν by ν_m and equate the left-hand side to $R \in [0, 1)$, a random number between zero and one. All random numbers mentioned hereafter, are drawn from this interval. Solving for t_m gives

$$t_m = -\frac{\ln(1-R)}{\nu_m}. \quad (5)$$

Upon creation at time t_0 , each individual particle is assigned a collision time $t_c = t_0 + t_m$. After each time step of the PIC loop it is evaluated whether the particle needs to collide, i.e., it is checked if $t \geq t_c$. If so, the collision frequency $\nu_i(E)$ of each process at t_c is calculated to determine the collision type from

$$\begin{aligned} 0 < R &\leq \nu_1(E)/\nu_m && \text{type 1} \\ \nu_1(E)/\nu_m < R &\leq \sum_{i=1}^2 \nu_i(E)/\nu_m && \text{type 2,} \\ &\vdots \\ \sum_{i=1}^N \nu_i(E)/\nu_m < R &&& \text{null collision} \end{aligned} \quad (6)$$

with R a random number. Once the collision type is determined the velocity of the particle is adjusted accordingly. After the collision the time to the next collision t_m [using Eq. (5)] is added to the particle's collision time.

B. Collision types

The following binary collision types are taken into account.

- (i) Elastic electron-neutral collisions: $e^- + \text{Ar} \rightarrow e^- + \text{Ar}$.
- (ii) Inelastic electron-neutral collisions: $e^- + \text{Ar} \rightarrow e^- + \text{Ar}^*$.
- (iii) Electron-impact ionization collisions: $e^- + \text{Ar} \rightarrow 2e^- + \text{Ar}^+$.
- (iv) Elastic ion neutral collisions: $\text{Ar}^+ + \text{Ar} \rightarrow \text{Ar}^+ + \text{Ar}$.
- (v) Charge-exchange collisions: $\text{Ar}^+ + \text{Ar} \rightarrow \text{Ar} + \text{Ar}^+$.

Cross sections for these processes are the same as the ones used by Phelps [8] for their description of cold-cathode discharges over a wide range of electric field to gas density ratios ($E/n=15$ Td to 100 kTd). The collision frequencies for electron-argon scattering associated with these cross sections are plotted in Fig. 2.

C. Electron-neutral collisions

1. Elastic collisions

In the low energy limit, electron-neutral scattering is isotropic, but at higher energies the scatter angle θ will increasingly be in the forward direction. In the first Born-approximation [9] the quantum mechanical differential cross section $\sigma(\varepsilon, \theta)$ for screened Coulomb electron-neutral scattering is given by [10]

$$\frac{\sigma(\varepsilon, \theta)}{\sigma(\varepsilon)} = \frac{1}{4\pi} \frac{1+8\varepsilon}{(1+4\varepsilon-4\varepsilon \cos \theta)^2}, \quad (7)$$

with $\varepsilon = E/E_0$ a dimensionless energy parameter and $E_0 = 27.21$ eV the atomic unit of energy, which can be expressed in fundamental constants. For atomic collisions, scat-

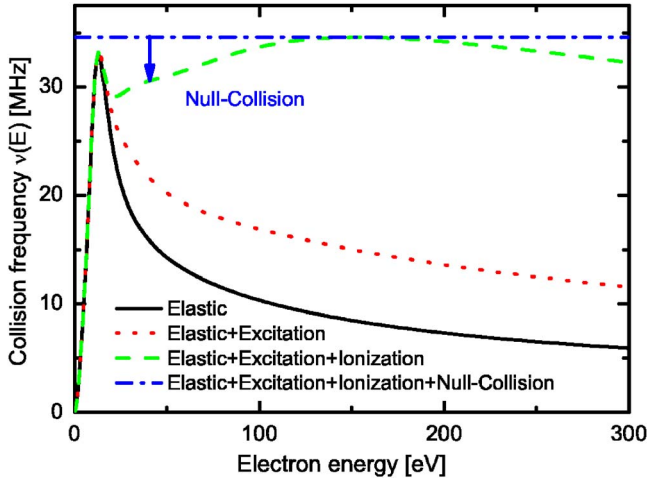


FIG. 2. (Color online) Collision frequencies for electron-argon scattering based on the cross sections of Phelps [8]. Solid line: elastic scattering. Dotted line: sum of elastic and inelastic scattering. Dashed line: sum of elastic, inelastic, and ionization processes. Dashed-dotted line: maximum collision cross section ν_m .

tering is isotropic in the azimuthal direction and therefore the differential cross section does not depend on the φ coordinate. The scattering angle φ in the azimuthal direction is found from $\varphi = 2\pi R$ with R a random number. To find the scattering angle θ of an electron in the polar direction we sample the angle from the differential cross section. Hereto, we first calculate the cumulative probability by integration of Eq. (7) over all solid angles with $\theta' \in [0, \theta]$ and equate the result to a random number

$$R = 2\pi \int_0^\theta \frac{\sigma(\varepsilon, \theta')}{\sigma(\varepsilon)} \sin(\theta') d\theta'. \quad (8)$$

Solving for θ yields

$$\theta = \arcsin\left(1 - \frac{2R}{1 + 8\varepsilon(1-R)}\right). \quad (9)$$

This expression gives the scattering angle for an electron with dimensionless energy ε in the center-of-mass frame. Because the electron-neutral mass ratio is a very small number, energy transfer from the electron to the neutral will be small and the scattering angle in the laboratory frame will be approximately the same.

2. Excitation

In inelastic collisions, energy is transferred to the internal states of the argon atom. In the model all internal states are merged into one single excitation level with an energy of $E_{exc} = 11.5$ eV above the argon ground state [8]. First, the excitation energy is subtracted from the electron kinetic energy after which the scattering angle is determined from Eq. (9).

3. Ionization

If the kinetic energy E_{in} of the incoming electron is above the argon ionization energy E_{ion} an ionizing electron-argon

collision can occur, in which an electron-ion pair is created. The excess energy $E_{in} - E_{ion}$ is carried away by the two electrons, whereas the kinetic energy of the ion will be equal to the initial (thermal) energy of the neutral. In the model, the velocity of the target neutral is sampled from a Maxwellian velocity distribution that corresponds to a temperature of $T = 300$ K.

It is not possible to predict how the excess energy will be distributed between the incoming and ejected electron. Therefore, we apply an empirical formula for the distribution function based on the work of Opal [11] as mentioned in Surendra and Graves [12]

$$S(E_{in}, E_{ej}) = \frac{A}{E_{ej}^2 + B^2(E_{in})}, \quad (10)$$

with A a normalization constant that can be obtained from integration over E_{ej} from 0 to the maximum energy $E_{max} = (E_{in} - E_{ion})/2$, which is half the excess energy due to the indistinguishability of the two electrons involved

$$A = \left\{ \int_0^{E_{max}} S(E_{in}, E_{ej}) dE_{ej} \right\}^{-1},$$

$$= \frac{B(E_{in})}{\arctan[(E_{in} - E_{ion})/2B(E_{in})]}. \quad (11)$$

For argon $B(E_{in}) \approx 10$ eV in the energy range 1 to 70 eV [11].

Upon collision, we first obtain the energy of the ejected electron by drawing a random number R to sample the distribution of Eq. (10) according to

$$E_{ej} = B(E_{in}) \tan[R \arctan(E_{max}/B(E_{in}))]. \quad (12)$$

The ejected electron is created at the position of the incoming electron and the scattering angle is determined by Eq. (9). Next, the energy of the incoming electron is reduced by the sum of the ionization energy and the energy of the ejected electron after which the scattering angle is again determined from Eq. (9).

4. Ion-neutral collisions

Because the masses of ions and neutrals are almost the same, the collisional energy exchange between them is considerable and has to be properly taken into account. Therefore, collisions between ions and argon atoms are treated in the center-of-mass frame. The velocities of the target neutrals are sampled from a Maxwellian velocity distribution at room temperature ($T = 300$ K). For ion collisions we assume scattering to be isotropic with a scattering angle in the center-of-mass frame equal to

$$\theta = \arcsin(1 - 2R), \quad (13)$$

with R a random number. After the collision the velocity of the argon ion is transferred back to the laboratory frame.

D. Generation of particles

Figure 3 shows a schematic of the geometry used in the simulations. The radiation driven plasma is bounded by a

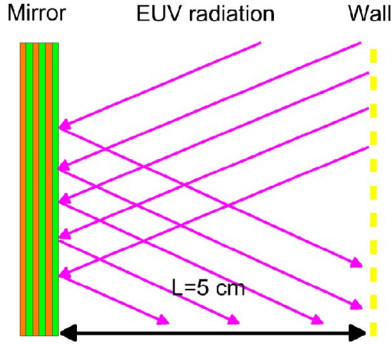


FIG. 3. (Color online) Schematic of the geometry used in simulations. The EUV radiation is partially reflected by the mirror. It is assumed that the EUV radiation between the mirror on the left and a plain wall on the right to be monochromatic and homogeneous in intensity.

multilayer mirror on the left side and a metal wall on the right side. The top layer of the mirror is assumed to be ruthenium, because in EUV lithography this material is often applied as a capping layer (thickness of ≈ 1.5 nm) to provide a barrier against oxidation of the underlying Mo/Si multilayers [13]. Both the multilayer mirror and wall are assumed to be grounded. At the multilayer mirror the EUV radiation is partially reflected, with a reflection coefficient of typically $R_{ml}=68\%$ [14]. The remaining 32% of the radiation is absorbed by the mirror material and is transformed mainly into heat.

The spatial distribution of the EUV radiation is assumed to be homogeneous, whereas the temporal distribution $G(t)$ is modeled with a cutoff Gaussian with a total duration of $2\tau=100$ ns

$$G(t) = \frac{\alpha I_p}{\tau} \exp\left[-\frac{(t-\tau)^2}{2\tau^2}\right] \quad \text{for } 0 < t < 2\tau, \quad (14)$$

with α a numerical constant to normalize $G(t)$ to the pulse-averaged EUV intensity I_p .

Electron-ion pairs are generated as a result of photoionization of the argon background gas. The EUV photon energy of $h\nu=92$ eV is well above the argon ionization energy $E_{ion}=15.8$ eV. Consequently, in the volume argon can be photoionized by EUV radiation, creating a fast electron with kinetic energy $T_e=h\nu-E_{ion}$ and a slow Ar^+ ion, with kinetic energy equal to the thermal energy of argon at room temperature.

The total number N_{pi} of photoionization events per EUV pulse per m^3 is equal to

$$N_{pi} = \frac{I_p}{h\nu L} [1 - \exp(-n_{Ar}\sigma_{ph}L_{opt})], \quad (15)$$

with I_p the pulse averaged EUV intensity, n_{Ar} the argon density, σ_{ph} the photoionization cross section [15], and $L_{opt}=L(1+R_{ml})$ the effective optical path length that takes into account the partial reflection of the EUV beam from the mirror as indicated in Fig. 3.

TABLE I. Simulation parameters.

| | | |
|--------------------|------------|-------------------------------------|
| Background density | n_{Ar} | $1.2 \times 10^{20} \text{ m}^{-3}$ |
| EUV intensity | I_p | $6 \times 10^{-4} \text{ W m}^{-2}$ |
| Time step | Δt | $1 \times 10^{-12} \text{ s}$ |
| Particle weight | PW | 10^9 |
| Number of cells | N_c | 300 |
| Length | L | $5 \times 10^{-2} \text{ m}$ |

III. RESULTS/DISCUSSION

The simulation parameters are listed in Table I. The chosen EUV intensity is typical for our laboratory setup. In our simulations we set the argon background pressure at 0.5 Pa. At this low pressure the plasma will be in the nonlocal regime and the plasma sheath will be almost, but not quite, collisionless, as we estimate the average number of ion-neutral collisions for an ion crossing the sheath with an energy between 20 and 100 eV to be ≈ 0.2 .

We divide the length of the computational domain into $N_c=300$ cells, so that the cell size is smaller than the Debye screening length, which is $\lambda_D \approx 5 \times 10^{-4} \text{ m}$ for our application. Each species is represented by 10^5 superparticles to ensure proper statistics. The time step of the PIC-loop must be small compared to the time it takes a fast electron to travel across a cell, which for a 100 eV electron and for our cell size corresponds to ≈ 30 ps. This is two orders of magnitude smaller than the fastest time scale of the plasma, which is given by the inverse of the plasma electron frequency.

Figure 4 shows the cell-averaged energy of the plasma electrons as a function of position at various times. Initially, the plasma is very hot and the energy of the electrons is close to $h\nu-E_{ion} \approx 76$ eV. The plasma cools mainly due to inelastic and ionizing collisions of electrons with the neutral background. After the 100 ns long EUV pulse the photoionization process ceases and the average electron energy decreases rapidly as no more fast electrons are generated. As can be seen in Fig. 4, the spatial fluctuations of the average electron energy decrease with time as more superparticles are added

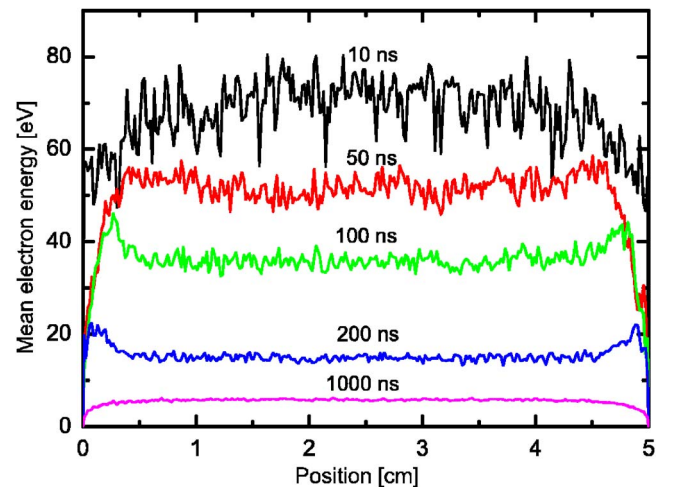


FIG. 4. (Color online) Cell-averaged electron energy profile at five different times.

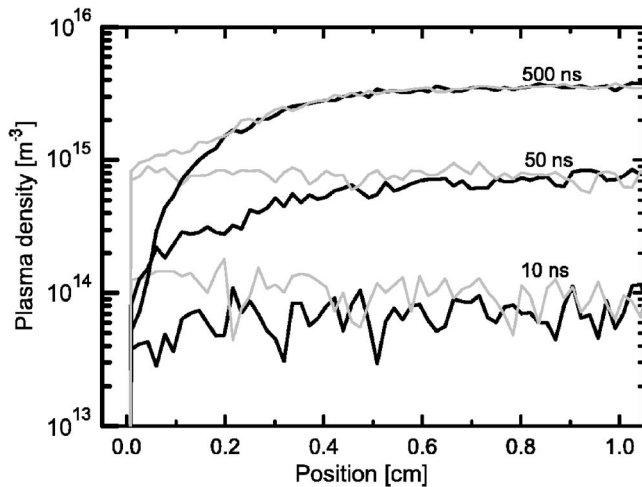


FIG. 5. Plasma density profile near the mirror at three different times. $t=10$ ns (bottom), $t=50$ ns (middle), and $t=500$ ns (top). The thick lines represent electron density, whereas the thin lines indicate ion density.

to the simulation, thereby improving the statistical representation.

The development of the plasma sheath can be seen in Fig. 5, which shows the plasma density profile near the mirror region at three different times. Near the mirror, the ion density exceeds the electron density and a positive space charge region forms as the highly mobile electrons have escaped to the wall, leaving the more inert ions behind. At the end of the EUV pulse, most electrons still have sufficient kinetic energy to cause further ionization processes. That is why the maximum plasma density $n_e=4 \times 10^{15} \text{ m}^{-3}$ is reached long after the EUV pulse at $t=500$ ns. After that, the plasma density starts to decay on a time scale that is short compared to the time between EUV pulses.

The formation of the plasma sheath can also be studied by considering the potential, shown in Fig. 6. The maximum plasma potential of ≈ 80 volts is reached during the EUV pulse. The plasma is at a positive potential with respect to the

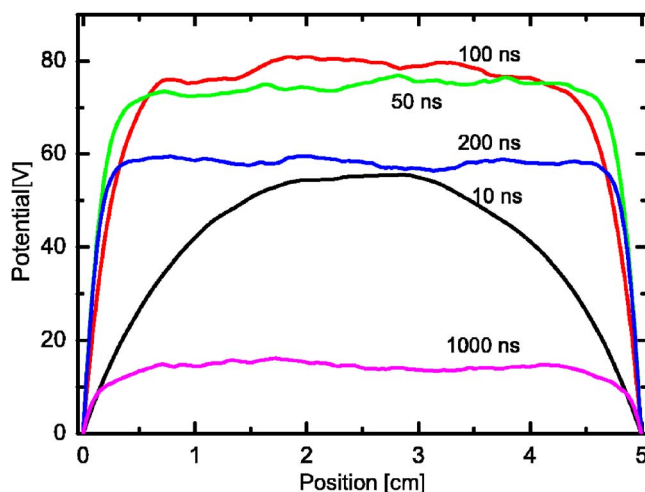


FIG. 6. (Color online) Potential profile at five different times. At $t=10$ ns (thick solid line), $t=50$ ns (dashed line), $t=100$ ns (dotted line), $t=200$ ns (dash-dotted line), and $t=1000$ ns (thin solid line).

walls as a result of the positive space charge in the sheath, thus creating an electric field in the sheath that directs electrons into the plasma and accelerates ions towards the walls. After the EUV pulse ($t > 100$ ns) the plasma potential gradually decreases, because the charge separation in the plasma sheath is reduced as a result of the decrease in average electron energy.

In Fig. 7 the kinetic energy of ions impacting on the mirror is shown as a function of time. For clarity's sake, the moving average over 50 consecutive ion impacts is taken. The dotted line shows the temporal shape of the EUV pulse. Due to their inertia the ions reach the mirror after the EUV-pulse. The ion impact energy reaches a maximum of ≈ 40 eV at $t=270$ ns.

Whether this ion bombardment translates into mirror damage goes beyond this model. It needs to be determined experimentally. However, as a first order estimation we can apply the Bohdanský [16] model for light ion sputtering. This semiempirical model gives the sputter yield $Y(E)$, i.e., the number of atoms removed from the solid per incoming ion with energy E . Only ions with an energy above the sputter threshold contribute. The sputter threshold can be calculated from

$$E_{thr} = \begin{cases} \frac{U_s}{\lambda(1-\lambda)} & \text{for } \left(\frac{m_1}{m_2}\right) < 0.3 \\ 8U_s \left(\frac{m_1}{m_2}\right)^{2/5} & \text{for } \left(\frac{m_1}{m_2}\right) > 0.3, \end{cases} \quad (16)$$

with U_s the surface binding energy of the solid which can be approximated by the sublimation heat and with λ the fraction of energy that is transferred from the projectile (with mass m_1) to the target atom (with mass m_2) in case of a head-on collision

$$\lambda = \frac{4m_1m_2}{(m_1+m_2)^2}. \quad (17)$$

For Ar^+ on Ru $\lambda=0.812$, $U_s=6.74$ eV and $E_{thr}=37.2$ eV.

In Fig. 7 the sputter threshold is indicated by the bold dashed line. Only a fraction of the ions has an impact energy

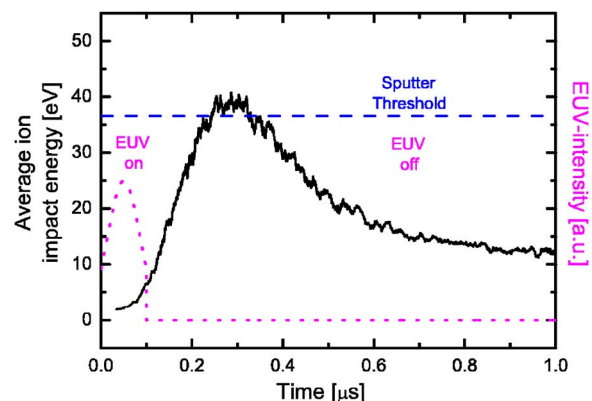


FIG. 7. (Color online) Solid line: the energy in eV's of ions that have impacted on the mirror. For clarity, the depicted energy is the moving average over fifty consecutive ion impacts. Dotted line: the temporal profile of the EUV intensity in arbitrary units. Dashed line: the Bohdanský sputter threshold.

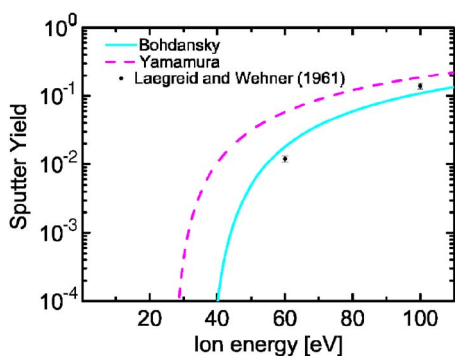


FIG. 8. (Color online) Sputter yield for Ar^+ on Ru as a function of ion energy according to the Bohdansky model (solid line), the Yamamura model (dashed line), and the experimental data of Laegreid and Wehner (circles).

above the sputter threshold. Therefore, we expect the damage to the mirror as a result of physical sputtering to be modest.

A word of caution is in place. Because the ion energies are close to the sputter threshold the calculated sputter rate is very sensitive to the value for the sputter threshold. For instance, the Yamamura [17] model for ion sputtering predicts a sputter threshold that is 10 eV lower. Figure 8 shows the sputter yield according to the Bohdansky and Yamamura model together with the, to our knowledge, only available experimental data set [18] for this specific target-projectile combination.

If we convolute the sputter yield with the ion flux we obtain the total number of atoms removed per EUV pulse. For the Bohdansky and Yamamura model this amounts to, respectively, 6.2 and 205 nm per 10^{12} EUV pulses. Clearly, the Yamamura model predicts higher sputter rates than the Bohdansky model mainly due to the lower sputter threshold. The predicted sputter rates are too low to be experimentally verified. In the calculation of the sputter rate, we have only considered the impact of ions. However, charge-exchange

collisions in the sheath region will result in a flux of fast neutrals to the mirror surface, that will also contribute to the sputter rate. In our low-pressure application, the neutral flux is very low, because the mean free path for charge-exchange collisions for energetic ions ($E=30-100$ eV) is ≈ 10 times higher than the thickness of the plasma sheath. Hence, sputtering by neutrals can be neglected.

IV. CONCLUSIONS

In conclusion, we have demonstrated that with PICMCC simulations it is possible to describe transient plasmas in the nonlocal regime without the need for equilibrium assumptions for the fields or the velocity distributions of the charged particles. Furthermore, the EUV radiation driven plasma is found to be weakly ionized (ionization degree $< 0.1\%$) with a low plasma density ($n_e = 4 \times 10^{15} \text{ m}^{-3}$).

The simulations show that the potential drop across the plasma sheath is dictated by the electron energy. Ions are accelerated across the sheath, but due to their inertia, most ions reach the mirror after the EUV pulse has ended.

Based on two models for the sputter yield, we conclude that only a small fraction of the ions impacting on the optics will have sufficient energy to sputter. However, the calculated sputter rate strongly depends on which model is applied, mainly because the two models employ a different value for the sputter threshold. Further experimental investigation is required to determine the value of the sputter threshold. The predicted sputter rate is very low (< 1 nm per 10^9 EUV pulses) and cannot be measured directly. Future investigations should aim to verify the other predictions of the simulations regarding the ion impact energy distribution, plasma density, and electron energy distribution.

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