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Unidirectional magnetic coupling induced by chiral interaction and nonlocal damping

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We show that an interlayer Dzyaloshinskii-Moriya interaction in combination with nonlocal damping gives rise to unidirectional magnetic coupling. That is, the coupling between two magnetic layers—say, the left and right layer—is such that the dynamics of the left layer leads to the dynamics of the right layer, but not vice versa. We discuss the implications of this result for the magnetic susceptibility of a magnetic bilayer, electrically actuated spin-current transmission, and unidirectional spin-wave packet generation and propagation. Our results may enable a route towards spin-current and spin-wave diodes and further pave the way to design spintronic devices via reservoir engineering.

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I. INTRODUCTION

Nonreciprocal transmission of electrical signals lies at the heart of modern communication technologies. While semiconductor diodes, as an example of an electronic component that underpins such nonreciprocity, have been a mature technology for several decades, new solutions are being actively pursued [1,2]. Such research is spurred on by the emergence of quantum technologies that need to be read out electrically but should not receive unwanted backaction from their electronic environment.

Complementary to these developments, spintronics has sought to control electronic spin currents and, more recently, spin currents carried by spin waves, i.e., magnons, in magnetic insulators [3]. Devices that implement nonreciprocal spin-wave spin currents have been proposed [4–7]. Most of these proposals rely on dipolar interactions [8–11] or Dzyaloshinskii-Moriya interactions (DMIs) [12–16]. Other proposals involve the coupling of the spin waves to additional excitations such as the spin waves are endowed with non-reciprocity. Examples are the coupling of the spin waves to magnetoelastic, optical, and microwave excitations [17–22].

Most of these proposals have in common that they consider spin-wave dispersions that are asymmetric in wave vectors. For example, due to the DMI, spin waves at one particular frequency have different wave numbers and velocities for the two different directions. There are therefore spin waves traveling in both directions. This may be detrimental for some applications. For example, one would like to shield traveling in both directions. This may be detrimental for frequency have different wave numbers and velocities for

II. MINIMAL MODEL

Let us start with the minimal setup that demonstrates the unidirectional coupling. We first consider two identical homogeneous magnetic layers that are coupled only by an interlayer DMI with Dzyaloshinskii vector $D$ [24,25] and by interlayer spin pumping (see Fig. 1) and then show that the essential physics also holds when a Heisenberg exchange, Gilbert damping, and magnetic anisotropy are included. The magnetization direction in the layers is denoted by $\mathbf{m}_i$, where $i \in \{1, 2\}$ labels the two layers. We also include an external field $H$. The magnetic energy is given by

$$E[m_1, m_2] = D \cdot (m_1 \times m_2) - \mu_0 M_s H \cdot (m_1 + m_2),$$

where $M_s$ is the saturation magnetization of both layers and $\mu_0$ is the vacuum susceptibility. The magnetization dynamics of layer 1 is determined by the Landau-Lifshitz-Gilbert (LLG) equation

$$\frac{\partial m_1}{\partial t} = \gamma M_s m_1 \times \frac{\delta E}{\delta m_1} + \alpha_m m_1 \times \frac{\partial m_2}{\partial t},$$

where $\gamma$ is the gyromagnetic ratio and $\alpha_m$ characterizes the strength of the nonlocal damping that in this setup results from the combination of spin pumping and spin transfer torques, as described in the Introduction. The equation of motion for the magnetization dynamics of the second layer is found by
interchanging the labels 1 and 2 in the above equation. Working out the effective fields \( \delta E/\delta m_i \) yields

\[
\frac{\partial m_1}{\partial t} = \frac{\gamma}{M_s} m_1 \times (m_2 \times D - \mu_0 M_i H) + \alpha_{nl} m_1 \times \frac{\partial m_2}{\partial t}, \tag{3a}
\]
\[
\frac{\partial m_2}{\partial t} = \frac{\gamma}{M_s} m_2 \times (D \times m_1 - \mu_0 M_i H) + \alpha_{nl} m_2 \times \frac{\partial m_1}{\partial t}, \tag{3b}
\]
where the sign difference in the effective-field contribution from the DMI stems from the asymmetric nature of the DMI. We show now that depending on the magnitude and direction of the effective field, this sign difference leads for one of the layers to cancel the torques due to interlayer DMI and nonlocal damping. As the cancellation does not occur for the other layer, and because the DMI and nonlocal damping are the mechanisms that couple the layers in the model under consideration, this leads to unidirectional magnetic coupling.

Taking the external field to be much larger than the interlayer DMI, i.e., \( \mu_0 |H| \gg |D|/M_s \), and taking \( \alpha_{nl} \ll 1 \), we may replace \( \partial m_i/\partial t \) by \( -\gamma \mu_0 m_i \times \mathbf{H} \) on the right-hand sides of Eqs. (3) because the external field then is the dominant contribution to the precession frequency. For the field \( \mathbf{H} = D/\alpha_{nl} \mu_0 M_i \), one then finds that

\[
\frac{\partial m_1}{\partial t} = -\frac{\gamma}{\alpha_{nl} M_s} m_1 \times D, \tag{4a}
\]
\[
\frac{\partial m_2}{\partial t} = \frac{2\gamma}{M_s} m_2 \times (D \times m_1) - \frac{\gamma}{\alpha_{nl} M_s} m_2 \times D. \tag{4b}
\]

Hence, the coupling between the two magnetic layers is unidirectional at the field \( \mathbf{H} = D/\alpha_{nl} \mu_0 M_i \): The magnetization dynamics of layer 1 leads to the dynamics of layer 2 as evidenced by Eq. (4b), but not vice versa as implied by Eq. (4a). This one-way coupling is reversed by changing the direction of the field to \(-\mathbf{H}\) or the sign of the nonlocal coupling \( \alpha_{nl} \), which depends on the intrinsic properties of the materials and the distance between the neighboring spins [26].

### III. MAGNETIC SUSCEPTIBILITY

Let us now take into account the Gilbert damping within the layers, exchange interaction, and magnetic anisotropy and discuss the influence of the unidirectional coupling on the magnetic susceptibility. The energy now reads

\[
E[m_1, m_2] = -J m_1 \cdot m_2 + D \cdot (m_1 \times m_2) - \mu_0 M_i H \cdot (m_1 + m_2) - \frac{K}{2} (m_{1z}^2 + m_{2z}^2), \tag{5}
\]

with the constant \( K \) characterizing the strength of the anisotropy and \( J \) the exchange. Here, the anisotropy may include contributions from spin-orbit coupling and the dipolar fields. The nonuniform part of the dipolar interaction does not play a significant role because the magnetization of each layer is polarized by the strong magnetic fields. We shall focus on the ferromagnetic coupling \( J > 0 \) without loss of generality. The LLG equation now becomes

\[
\frac{\partial m_1}{\partial t} = \frac{\gamma}{M_s} m_1 \times \frac{\partial E}{\partial m_1} + \alpha m_1 \times \frac{\partial m_1}{\partial t} + \alpha_{nl} m_1 \times \frac{\partial m_2}{\partial t}, \tag{6}
\]

with \( \alpha \) the Gilbert damping constant of each layer, and where the equation for the second layer is obtained from the above by interchanging the labels 1 and 2. Here, the Gilbert damping includes the contribution from nonlocal damping, magnon-magnon, and magnon-phonon interactions. In general, it should be larger than the nonlocal damping to guarantee the stability of the system [27]. We take the external field in the same direction as the Dzyaloshinskii vector and \( D = D \hat{z} \), \( \hat{H} = H \hat{z} \), while \( \mu_0 M_i H, K \gg D \), so that the magnetic layers are aligned in the \( \hat{z} \) direction. Linearizing the LLG equation around this direction we write \( m_i = (m_{i,x}, m_{i,y}, 1) \) and keep terms linear in \( m_{i,x} \) and \( m_{i,y} \). Writing \( \phi_i = m_{i,x} - im_{i,y} \), we find, after Fourier transforming to frequency space, that

\[
\chi^{-1}(\omega) \begin{pmatrix} \phi_1(\omega) \\ \phi_2(\omega) \end{pmatrix} = 0. \tag{7}
\]

To avoid lengthy formulas, we give explicit results below for the case that \( J = 0 \), while plotting the results for \( J \neq 0 \) in Fig. 2. The susceptibility tensor \( \chi_{ij} \), or magnon Green’s function, is given by

\[
\chi(\omega) = \frac{1}{\left[ (1 + i\alpha)\omega - \omega_H \right]^2 - (\gamma D/M_s)^2 - \alpha_{nl}^2 \omega^2} \times \begin{pmatrix} 1 & \left[ 1 + i\alpha \omega - \omega_H \right] i(\gamma D/M_s - \alpha_{nl} \omega) \\ -i(\gamma D/M_s + \alpha_{nl} \omega) & (1 + i\alpha)\omega - \omega_H \end{pmatrix}. \tag{8}
\]
with \( \omega_H = \gamma(\mu_0 H + K/M_s) \) the ferromagnetic-resonance (FMR) frequency of an individual layer. The poles of the susceptibility determine the FMR frequencies of the coupled layers and are, for the typical case that \( \alpha, \alpha_{nl} \ll 1 \), given by

\[
\omega_{\pm} = \omega_{r,\pm} - i\omega_{r,\pm}.
\] (9)

with resonance frequency

\[
\omega_{r,\pm} = \gamma(\mu_0 H + K/M_s \pm D/M_s).
\] (10)

When \( \gamma \mu_0 H = (1 \mp \alpha_{nl} D)/(\alpha_{nl} M_s) - K/M_s \approx D/(\alpha_{nl} M_s) - K/M_s \), we have for \( J = 0 \) that \( \chi_{12}(\omega_{\pm}) = 0 \) while \( \chi_{21}(\omega_{\pm}) \neq 0 \), signaling the nonreciprocal coupling.

IV. ELECTRICALLY ACTUATED SPIN-CURRENT TRANSMISSION

In practice, it may be challenging to excite the individual layers independently with magnetic fields, which would be required to probe the susceptibility that is determined above. The two layers may be more easily probed independently by spin-current injection/ extraction from adjacent contacts. Therefore, we consider the situation that the two coupled magnetic layers are sandwiched between heavy-metal contacts [see Fig. 3(a)]. In this setup, spin current may be transmitted between the two contacts through the magnetic layers.

Following the Green’s function formalism developed by Zheng et al. [28], the spin current from the left (right) lead to its adjacent magnetic layer is determined by the transmission function of the hybrid system \( T_{12}(\omega) \) given by

\[
T_{ij}(\omega) = \text{Tr}[\Gamma_i(\omega)G^{(+)}(\omega)\Gamma_j(\omega)G^{(-)}(\omega)].
\] (11)

Here, \( G^{(+)}(\omega) \) is the retarded Green’s function for magnons in contact with the metallic leads that is determined by Dyson’s equation \( [G^{(+)}]^{-1}(\omega) = \chi^{-1}(\omega) - \Sigma_1^{(+)}(\omega) \), where the retarded self-energy \( \Sigma_1^{(+)}(\omega) \) accounts for the contact with the metallic lead \( i \). These self-energies are given by

\[
\hbar \Sigma_1^{(+)}(\omega) = -i\hbar \alpha_i'(\omega) = \left( \begin{array}{cc} 0 & 1 \\ 0 & 0 \end{array} \right).
\] (12)

and

\[
\hbar \Sigma_2^{(+)}(\omega) = -i\hbar \alpha_{nl}'(\omega) = \left( \begin{array}{cc} 0 & 0 \\ 0 & \omega \end{array} \right).
\] (13)

The rates for spin-current transmission from the heavy metal adjacent to the magnet \( i \) into it, are given by \( \Gamma_i(\omega) = -2\text{Im}[\Sigma_i^{(+)}(\omega)]/\hbar \). The couplings \( \alpha_i' = \gamma \text{Re}[g_i']/4\pi M_s d_i \) are proportional to the real part of the spin-mixing conductance per area \( g_i' \) between the heavy metal and the magnetic layer \( i \), and further depend on the thickness \( d_i \) of the magnetic layers. Finally, the advanced Green’s function is \( G^{(-)}(\omega) = [G^{(+)}]^{-1} \).

In the analytical results below, we again restrict ourselves to the case where \( J = 0 \) for brevity, leaving the case \( J \neq 0 \) to the plots. Using the above expressions, Eq. (11) is evaluated. Taking identical contacts so that \( \alpha'_i = \alpha'_{nl} = \alpha' \), we find that

\[
T_{12} = 4(\alpha')^2\omega^2(yD/M_s + \alpha_{nl}\omega)^2/|C(\omega)|^2,
\] (14)

while

\[
T_{21} = 4(\alpha')^2\omega^2(yD/M_s - \alpha_{nl}\omega)^2/|C(\omega)|^2,
\] (15)

with

\[
C(\omega) = [\omega_H - [1 + i(\alpha - \alpha_{nl} + \alpha')\omega]\omega_H - [1 + i(\alpha + \alpha_{nl} + \alpha')\omega] - (yD/M_s)]^2.
\] (16)

From the expression for \( C(\omega) \) it is clear that, since \( \alpha, \alpha_{nl}, \alpha' \ll 1 \), the transmission predominantly occurs for frequencies equal to the resonance frequencies \( \omega_{r,\pm} \) from Eq. (9). Similar to the discussion of the susceptibilities, we have for fields \( \gamma \mu_0 H = D/\alpha_{nl} - K/M_s \) that the transmission \( T_{12}(\omega = D/\alpha_{nl}) \neq 0 \), while \( T_{21}(\omega = D/\alpha_{nl}) = 0 \). As a result, the spin-current transmission is unidirectional at these fields. For the linear spin conductances \( G_{ij} \), given by \( G_{ij} = \int \hbar \omega [N(-\hbar \omega)]T_{ij}(\omega) \), we also have that \( G_{12} \neq 0 \), while \( G_{21} = 0 \). Here, \( N(h\omega) = (e^{h\omega/k_BT} - 1)^{-1} \) is the Bose-Einstein distribution function at thermal energy \( k_BT \). For the opposite direction of the external field we have \( G_{12} = 0 \), while \( G_{21} \neq 0 \). As in the case of the susceptibility discussed in the
previous section, a finite but small exchange coupling makes the spin-current transport no longer purely unidirectional, while maintaining a large nonreciprocity [see Fig. 3(b)].

V. SPIN-WAVE PROPAGATION

Besides the unidirectional coupling of two magnetic layers, the above results may be generalized to a magnetic multilayer, or, equivalently, an array of coupled magnetic moments that are labeled by the index \( i \) such that the magnetization direction of the \( i \)th layer is \( m_i \). This extension allows us to engineer unidirectional spin-wave propagation as we shall see below. We consider the magnetic energy

\[
E[m] = \sum_k \left[ D \cdot (m_k \times m_{k+1}) - \mu_0 M_s H \cdot m_k \right],
\]

(17)

and find—within the same approximations as for our toy model above—for the magnetization dynamics that

\[
\frac{\partial m_k}{\partial t} = \frac{2\gamma}{M_s} m_k \times (D \times m_{k-1}) - \frac{\gamma}{\alpha_d M_s} m_k \times D,
\]

(18)

for the field \( H = D/\alpha_d \mu_0 M_s \). This shows that for these fields the magnetic excitations travel to the right—corresponding to increasing index \( k \) only. The direction of this one-way propagation is reversed by changing the magnetic field to \(-H\) or by changing the sign of the nonlocal damping.

To study how spin waves propagate in an array of coupled magnetic moments described by the Hamiltonian in Eq. (17), we start from the ground state \( m_k = (0, 0, 1)^T \) and perturb the leftmost spin (\( k = 0 \)) to excite the spin waves. Since the dynamics of this spin is not influenced by the other spins for the field \( H = D/\alpha_d \mu_0 M_s \), its small-amplitude oscillation can be immediately solved as \( \phi_k(t) = \phi_0(t = 0) \exp(-t\omega_0 - \alpha_\omega_0 t) \)

with \( \phi_k = m_k - im_k \) as used previously. The dynamics of the spins to the right of this leftmost spin is derived by solving the LLG equation (18) iteratively, which yields

\[
\phi_k(t) = \phi_0(t = 0)e^{-\omega_0 t}e^{-\alpha_0 t} \frac{1}{k!} (-2\alpha_0 \omega_0 t)^k,
\]

(19)

where \( k = 0, 1, 2, \ldots, N - 1 \).

To guarantee the stability of the magnetization dynamics, the dissipation matrix of the \( N \)-spin system should be negative-definite, which imposes a constraint on the relative strength of Gilbert damping and nonlocal damping, i.e., \( \alpha > 2\alpha_0 \cos \frac{\pi}{N+1} \). For an infinitely long chain \( N \to \infty \), we have \( \alpha > 2\alpha_0 \). Physically, this means that the local dissipation of a spin has to be strong enough to dissipate the spin current pumped by its two neighbors. For a spin chain with a finite number of spins, \( \alpha = 2|\alpha_0| \) is always sufficient to guarantee the stability of the system. Taking this strength of dissipation simplifies Eq. (19) to

\[
\phi_k(t) = \phi_0(t = 0)e^{-\omega_0 t}e^{-t/\tau} \frac{1}{k!} (-t/\tau)^k,
\]

(20)

where \( t^{-1} = \omega_0 \tau \) is the inverse lifetime of the FMR mode. This spatial-temporal profile of spins is the same as a Poisson distribution with both mean and variance equal to \( \sigma = t/\tau \) except for a phase modulation, and it can be further approximated as a Gaussian wave packet on the timescale \( t \gg \tau \), i.e.,

\[
\phi(z) = \frac{\phi_0(t = 0)e^{-z^2/(2\sigma^2)}}{\sqrt{2\pi \sigma}}e^{-iz^2/2\gamma}.
\]

(21)

Such a similarity suggests that any local excitation of the leftmost spin will generate a Gaussian wave packet propagating along the spin chain. The group velocity of the moving wave packet is \( v = a/\tau \), where \( a \) is the distance between the two neighboring magnetic moments. The width of the wave packet spreads with time as \( \sigma \sqrt{t/\tau} \), which resembles the behavior of a diffusive particle. After a sufficiently long time, the wave packet will collapse.

On the other hand, the excitation is localized and cannot propagate when the rightmost spin (\( k = N - 1 \)) is excited, because its left neighbor, being in the ground state, has zero influence on its evolution. These results demonstrate the unidirectional properties of spin-wave transport in our magnetic array.

VI. DISCUSSION, CONCLUSION, AND OUTLOOK

We have shown that the ingredients for unidirectional coupling between magnetic layers or moments are that they are coupled only by DMI and nonlocal damping. While in practice it may be hard to eliminate other couplings, the DMI and nonlocal coupling need to be sufficiently larger than the other couplings to observe unidirectional coupling.

There are several systems that may realize the unidirectional coupling we propose. A first example is that of two magnetic layers that are coupled by a metallic spacer. Such a spacer would accommodate nonlocal coupling via spin pumping and spin transfer. For a spacer that is much thinner than the spin relaxation length, we find, following Refs. [29–31], that \( \alpha_{\text{sl}} = \gamma \hbar \text{Re}[\gamma^{\uparrow \downarrow}/4\pi d M_s] \), with \( \gamma^{\uparrow \downarrow} \) the spin-mixing conductance of the interface between the magnetic layers and the spacer, and \( d \) the thickness of the magnetic layers. For simplicity, we took the magnetic layers to have equal properties. The two magnetic layers may be coupled by the recently discovered interlayer DMI [24,25], tuning to a point (as a function of thickness of the spacer) where the ordinary Ruderman-Kittel-Kasuya-Yosida (RKKY) exchange coupling is small. We estimate \( \alpha_{\text{sl}} = 4.5 \times 10^{-3} \) for \( d = 20 \text{ nm} \), \( \text{Re}[\gamma^{\uparrow \downarrow}] = 4.56 \times 10^{14} \text{ A m}^{-2} \), and \( M_s = 1.92 \times 10^5 \text{ A/m} \) (YIG/Pt). The required magnetic field for unidirectional magnetic coupling falls into the range of 0.9–9.3 T for the reported values of interlayer DMI [32]. Such a magnitude of external fields is accessible with the current experimental techniques [33–35]. Another possible platform for realizing unidirectional coupling is the system of Fe atoms on top of a Pt substrate that was demonstrated recently [36] and the detection of spin waves in a relevant spin chain was also observed using inelastic electron tunneling spectroscopy [37]. Here, the relative strength of the DMI and exchange is tuned by the interatomic distance between the Fe atoms. Though not demonstrated in this experiment, the Pt will mediate nonlocal coupling between the atoms as well, which may be intuitively understood as based on the spin pumping and spin transfer mechanism [38]. Hence, this system may demonstrate the unidirectional coupling that we proposed.
Furthermore, our recent results show that the nonlocal damping between two neighboring spins can be mediated by a common bath which may be composed of phonons, electrons, and other carriers [39]. This mechanism is quite general and thus it is expected that the nonlocal damping is generically present in any magnetic material and does not require special tuning, though it may be hard to determine its strength experimentally. Hence, an attractive implementation of the unidirectional coupling would be a magnetic material with spins that are coupled only via DMI, without exchange interactions. While such a material has to the best of our knowledge not been discovered yet, it is realized transiently in experiments with ultrafast laser pulses [40]. Moreover, it has been predicted that high-frequency laser fields may be used to manipulate DMI and exchange, even to the point that the former is nonzero while the latter is zero [41,42].

Possible applications of our results are spin-wave and spin-current diodes and magnetic sensors, where a weak field signal can be amplified and transported through the unidirectional coupling to the remote site to be read out without unwanted backaction. Finally, we remark that the unidirectional magnetic coupling that we propose here may be thought of as reservoir engineering (cf. Ref. [43]). In our proposal, the reservoir is made up by the degrees of freedom that give rise to the nonlocal damping, usually the electrons. We hope that this perspective may pave the way for further reservoir-engineered magnetic systems.

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[32] Note that the typical values of DMI in Refs. [24,25] ranges from 0.1 to 1 meV per atom. Here, we transfer it to our unit system by making the correspondence $D \rightarrow D/(a^2d)$.


