

Impact Sensitivity Analysis of Cooperative Adaptive Cruise Control Against Resource-Limited Adversaries

Citation for published version (APA):

Huisman, M., Murguia, C., Lefeber, E., & Wouw, N. V. D. (2023). *Impact Sensitivity Analysis of Cooperative Adaptive Cruise Control Against Resource-Limited Adversaries*. arXiv.org.
<https://doi.org/10.48550/arXiv.2304.02395>

Document license:

CC BY

DOI:

[10.48550/arXiv.2304.02395](https://doi.org/10.48550/arXiv.2304.02395)

Document status and date:

Published: 07/09/2023

Document Version:

Publisher's PDF, also known as Version of Record (includes final page, issue and volume numbers)

Please check the document version of this publication:

- A submitted manuscript is the version of the article upon submission and before peer-review. There can be important differences between the submitted version and the official published version of record. People interested in the research are advised to contact the author for the final version of the publication, or visit the DOI to the publisher's website.
- The final author version and the galley proof are versions of the publication after peer review.
- The final published version features the final layout of the paper including the volume, issue and page numbers.

[Link to publication](#)

General rights

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal.

If the publication is distributed under the terms of Article 25fa of the Dutch Copyright Act, indicated by the "Taverne" license above, please follow below link for the End User Agreement:

www.tue.nl/taverne

Take down policy

If you believe that this document breaches copyright please contact us at:

openaccess@tue.nl

providing details and we will investigate your claim.

Impact Sensitivity Analysis of Cooperative Adaptive Cruise Control Against Resource-Limited Adversaries

Mischa Huisman, Carlos Murguia, Erjen Lefeber, and Nathan van de Wouw

Abstract— Cooperative Adaptive Cruise Control (CACC) is a technology that allows groups of vehicles to form in automated, tightly-coupled platoons. CACC schemes exploit Vehicle-to-Vehicle (V2V) wireless communications to exchange information between vehicles. However, the use of communication networks brings security concerns as it exposes network access points that the adversary can exploit to disrupt the vehicles' operation and even cause crashes. In this manuscript, we present a sensitivity analysis of CACC schemes against a class of resource-limited attacks. We present a modelling framework that allows us to systematically compute outer ellipsoidal approximations of reachable sets induced by attacks. We use the size of these sets as a security metric to quantify the potential damage of attacks affecting different signals in a CACC-controlled vehicle and study how two key system parameters change this metric. We carry out a sensitivity analysis for two different controller implementations (as given the available sensors there is an infinite number of realizations of the same controller) and show how different controller realizations can significantly affect the impact of attacks. We present extensive simulation experiments to illustrate the results.

I. INTRODUCTION

Connected and Automated Vehicles (CAVs) have become a promising technology in the automotive industry, offering potential improvements in safety, mobility, and environmental sustainability. Cooperative Adaptive Cruise Control (CACC) is a well-explored technology within CAVs that allows groups of vehicles to form tightly-coupled platoons by exchanging inter-vehicle data through Vehicle-to-Vehicle (V2V) wireless communication networks [1]. However, the use of communication networks brings security concerns as it exposes network access points that the adversary can exploit via cyberattacks, resulting in new safety and security challenges that were not encountered in traditional vehicle systems [2]-[5]. Therefore, a pressing need arises for technologies that can quantify the potential impact of cyberattacks on platooning behavior. Moreover, quantify the impact sensitivity against the potentially compromised elements, e.g., sensors, actuators, networks, and software, and provide guidelines to allocate security resources to minimize the impact of attacks.

New technologies in this field focus on the prevention and detection of cyberattacks, which are well-explored research

fields, where different sorts of attacks and methods are applied to increase the security of the system [5]-[8]. However, prevention and detection methods are bounded by unknown process and measurement disturbances, leaving space for the adversary to perform resource-limited stealth attacks [9].

There is limited research regarding the potential impact such a resource-limited attack has on platooning behavior. In [2] and [10], the authors present simulation studies where they compare the impact of particular types of attacks on cooperative driving systems. Although interesting, it lacks generality in terms of the variety of attacks that can be considered. To overcome these limitations, reachable sets induced by general resource-limited attacks (referred hereto as adversarial reachable sets) can be used to analyze attackers' capabilities to drive the platoon to unsafe states. In [11], adversarial reachable sets are approximated in a simulation environment for a class of bounded attacks. In [12] and [13], for a general class of linear-time invariant dynamical systems driven by peak-bounded disturbances, ellipsoidal outer approximations of the reachable sets are obtained using first-principles models and convex optimization techniques.

In this manuscript, we develop a framework to analyze the impact of cyberattacks by a general class of resource-limited adversaries on standard CACC schemes, using the outer ellipsoidal approximation of the adversarial reachable set. Using the size of these sets as a security metric, we quantify the potential damage of attacks affecting different signals in a CACC-controlled vehicle. In this scope, we investigate how the use of different sensors and key system parameters affects the reachable set, where a difference in size can indicate a more resilient implementation. The notion of critical states is introduced, which characterize states that, if reached, compromise the safety and integrity of the vehicle. To support our claims, we have conducted an extensive simulation study on two different realized CACC controllers. Our findings reveal that the impact of attacks can significantly vary depending on the type of controller implementation used.

The structure of the paper is as follows: Section II introduces some preliminary results necessary for the subsequent sections. Section III describes the platooning model, the CACC scheme, and the available measurements. Section IV presents the adversarial LTI systems derived from the system description. In Section V, an extensive simulation study is conducted to demonstrate how different implementations and system parameters can significantly affect the impact of attacks. Finally, Section VI provides the concluding remarks.

The research leading to these results has received funding from the European Union's Horizon Europe programme under grant agreement No 101069748 – SELFY project.

M. Huisman, C. Murguia, E. Lefeber, and N. van de Wouw are with the Department of Mechanical Engineering, Eindhoven University of Technology, The Netherlands. [m.r.huisman, C.G.Murguia, A.A.J.Lefeber, N.v.d.Wouw]@tue.nl

II. MATHEMATICAL PRELIMINARIES

A. Notation

The symbol \mathbb{R} stands for the real numbers, $\mathbb{R}_{>0}$ ($\mathbb{R}_{\geq 0}$) denotes the set of positive (non-negative) real numbers. The symbol \mathbb{N} stands for the set of natural numbers, including zero. The $n \times m$ matrix composed of only zeros is denoted by $\mathbf{0}_{n \times m}$, or simply $\mathbf{0}$ when its dimension is clear. Consider a finite index set $\mathcal{L} := \{l_1, \dots, l_\rho\} \subset \mathbb{N}$ with cardinality $\text{card}[\mathcal{L}] = \rho$, e.g., $\mathcal{L} = \{1, 3, 7, 15\}$ with $\text{card}[\mathcal{L}] = 4$, the notation $\text{diag}[B_j]$ and (B_j) , $j \in \mathcal{L}$, stand for the diagonal block matrix $\text{diag}[B_{l_1}, \dots, B_{l_\rho}]$ and stacked block matrix $(B_{l_1}, \dots, B_{l_\rho})$, respectively. The notation $A \geq 0$ (resp., $A \leq 0$) indicates that the matrix A is positive (resp., negative) semidefinite, i.e., all the eigenvalues of the symmetric matrix A are positive (resp. negative) or equal to zero, whereas the notation $A > 0$ (resp., $A < 0$) indicates the positive (resp., negative) definiteness, i.e., all the eigenvalues are strictly positive (resp. negative). We often omit implicit time dependencies of signals for simplicity of notation.

B. Definitions and Preliminary Results

Definition 1 (Reachable Set) [12] Consider the perturbed Linear Time-Invariant (LTI) system:

$$\zeta(k+1) = A\zeta(k) + \sum_{i=1}^N B_i \omega_i(k), \quad (1)$$

with $k \in \mathbb{N}$, state $\zeta(k) \in \mathbb{R}^{n_\zeta}$, perturbation $\omega_i \in \mathbb{R}^{p_i}$ satisfying $\omega_i^\top W_i \omega_i \leq 1$ for some positive definite matrix $W_i \in \mathbb{R}^{p_i \times p_i}$, $i = \{1, \dots, N\}$, $N \in \mathbb{N}$, and matrices $A \in \mathbb{R}^{n_\zeta \times n_\zeta}$ and $B_i \in \mathbb{R}^{n_\zeta \times p_i}$. The reachable set $\mathcal{R}^\zeta(k)$ at time $k \geq 0$ from the initial condition $\zeta_0 \in \mathbb{R}^{n_\zeta}$ is the set of states reachable in k steps by system (1) through all possible disturbances satisfying $\omega_i^\top W_i \omega_i \leq 1$, i.e.,

$$\mathcal{R}^\zeta(k) := \left\{ \zeta \in \mathbb{R}^{n_\zeta} \mid \begin{array}{l} \zeta = \zeta(k), \zeta(k) \text{ solution to (1),} \\ \text{and } \omega_i(k)^\top W_i \omega_i(k) \leq 1, \end{array} \right\}. \quad (2)$$

Lemma 1 (Ellipsoidal Approximation) [12] Consider the perturbed LTI system (1) and the reachable set $\mathcal{R}^\zeta(k)$ in Definition 1. For a given $a \in (0, 1)$, if there exist constants a_1, \dots, a_N and matrix P that is the solution of the convex program:

$$\begin{cases} \min_{P, a_1, \dots, a_N} -\log \det[P], \\ \text{s.t. } a_1, \dots, a_N \in (0, 1), a_1 + \dots + a_N \geq a, \\ P > 0, \begin{bmatrix} aP & \mathcal{A}^\top P & \mathbf{0} \\ PA & P & PB \\ \mathbf{0} & B^\top P & W_a \end{bmatrix} \geq 0, \end{cases} \quad (3)$$

with matrices $W_a := \text{diag}[(1-a_1)W_1, \dots, (1-a_N)W_N] \in \mathbb{R}^{\bar{p} \times \bar{p}}$ and $B := (B_1, \dots, B_N) \in \mathbb{R}^{n_\zeta \times \bar{p}}$, and $\bar{p} = \sum_{i=1}^N p_i$; then, for all $k \in \mathbb{N}$, $\mathcal{R}^\zeta(k) \subseteq \mathcal{E}^\zeta(k)$ with $\mathcal{E}^\zeta(k) := \{\zeta^\top(k) P \zeta(k) \leq \alpha^\zeta(k)\}$, with convergent scalar sequence $\alpha^\zeta(k) := a^{k-1} \zeta_0^\top P \zeta_0 + ((N-a)(1-a^{k-1}))/ (1-a)$. Ellipsoid $\mathcal{E}^\zeta(k)$ has the minimum asymptotic volume among all outer ellipsoidal approximations of $\mathcal{R}^\zeta(k)$.

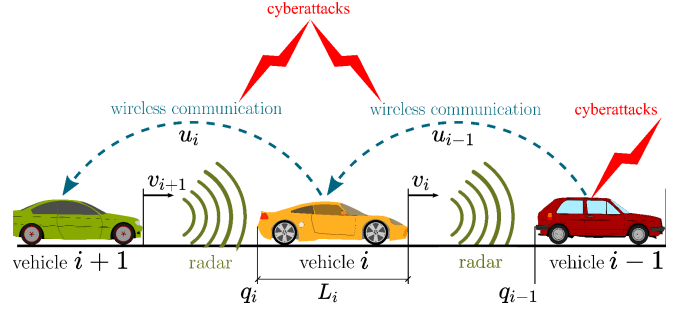


Fig. 1. CACC-equipped vehicle platoon. Each vehicle is equipped with onboard sensors (e.g., radars/LiDARs, cameras, and velocity/acceleration sensors). Vehicles may be subject to FDI attacks.

Lemma 2 (Projection) [12] Consider the ellipsoid:

$$\mathcal{E} := \left\{ x \in \mathbb{R}^n, y \in \mathbb{R}^m \mid \begin{bmatrix} x \\ y \end{bmatrix}^\top \begin{bmatrix} Q_1 & Q_2 \\ Q_2^\top & Q_3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \alpha \right\}, \quad (4)$$

for some positive definite matrix $Q \in \mathbb{R}^{(n+m) \times (n+m)}$ and constant $\alpha \in \mathbb{R}_{>0}$. The projection \mathcal{E}' of \mathcal{E} onto the x -hyperplane is given by the ellipsoid:

$$\mathcal{E}' := \{x \in \mathbb{R}^n \mid x^\top [Q_1 - Q_2 Q_3^{-1} Q_2^\top] x = \alpha\}. \quad (5)$$

III. SYSTEM DESCRIPTION

Consider a platoon of m vehicles, schematically depicted in Fig. 1, with $d_i(t) = q_{i-1} - q_i - L_i$ (q_i reflects the position of the rear bumper of vehicle i and L_i its length) being the distance between vehicle i and its preceding vehicle $i-1$, v_i the velocity of vehicle i . The objective of each vehicle is to keep a desired distance $d_{r,i}$ (the so-called spacing policy) with its preceding vehicle:

$$d_{r,i}(t) = r_i + h v_i(t), \quad i \in S_m, \quad (6)$$

with the headway $h > 0$, standstill distance $r_i > 0$, and $S_m := \{i \in \mathbb{N} \mid 1 \leq i \leq m\}$ (i.e., the set of all vehicles in a platoon of length $m \in \mathbb{N}$). A set of homogeneous vehicles is assumed; therefore, also h is chosen the same for all i . The spacing error is then defined as

$$e_i(t) := d_i(t) - d_{r,i}(t). \quad (7)$$

We adopt the CACC scheme introduced in [1], which considers a longitudinal vehicle model where the dynamics are described as

$$\begin{bmatrix} \dot{q}_i \\ \dot{v}_i \\ \dot{a}_i \end{bmatrix} = \begin{bmatrix} v_i(t) \\ a_i(t) \\ -\frac{1}{\tau} a_i(t) + \frac{1}{\tau} u_i(t) \end{bmatrix}, \quad i \in S_m, \quad (8)$$

where τ is a time constant modelling driveline dynamics, $a_i(t)$ denotes the acceleration of vehicle i , and $u_i(t)$ is its desired acceleration (the control input). The controller in [1] is a dynamic controller of the following form:

$$\mathcal{C} := \dot{u}_i = -\frac{1}{h} u_i + \frac{k_p}{h} e_i + \frac{k_d}{h} \dot{e}_i + \frac{k_{dd}}{h} \ddot{e}_i + \frac{1}{h} u_{i-1}, \quad (9)$$

where k_p, k_d , and k_{dd} are the controller gains. We refer to \mathcal{C} as the base controller.

The real-time realization of any control scheme depends on the available sensors $y_{i,j}$ (sensor number j of vehicle i). We use a combination of sensor data coming from onboard sensors (e.g., radar, LiDAR, cameras, and velocity/acceleration sensors) and received data transmitted wirelessly between adjacent vehicles. We assume that the sensors available to implement control actions are:

$$y_{i,1} := q_{i-1}(t) - q_i(t) - L_i + \delta_{i,1}(t), \quad (10a)$$

$$y_{i,2} := v_i(t) + \delta_{i,2}(t), \quad (10b)$$

$$y_{i,3} := a_i(t) + \delta_{i,3}(t), \quad (10c)$$

$$y_{i,4} := v_{i-1}(t) - v_i(t) + \delta_{i,4}(t), \quad (10d)$$

$$y_{i,5} := a_{i-1}(t) + \delta_{i,5}(t), \quad (10e)$$

$$y_{i,6} := u_{i-1}(t) + \delta_{i,6}(t). \quad (10f)$$

Herein, $\delta_{i,j}(t)$ models potential false data injection attacks and $j \in \{1, \dots, 6\}$. It is important to note that sensors $y_{i,1}$ and $y_{i,4}$ provide relative tracking and relative velocity information, $y_{i,2}$ and $y_{i,3}$ are the onboard measured velocity and acceleration, and sensors $y_{i,5}$ and $y_{i,6}$ model data received wirelessly from the preceding vehicle via V2V communication. Using the measured values in (10), base controller (9) can be implemented as follows:

$$\mathcal{C}_1 := \begin{cases} \dot{\xi}_{i,1} = -\left(\frac{1}{h} + \frac{k_{dd}}{\tau}\right)\xi_{i,1} + \frac{k_p}{h}y_{i,1} - k_p y_{i,2} \\ \quad - \left(k_d + \frac{k_{dh}}{h} - \frac{k_{dd}}{\tau}\right)y_{i,3} + \frac{k_d}{h}y_{i,4} \\ \quad + \frac{k_{dd}}{\tau}y_{i,5} + \frac{1}{h}y_{i,6} - \frac{k_p}{h}r_i \\ u_i = \xi_{i,1}, \end{cases} \quad (11)$$

with controller state $\xi_{i,1} \in \mathbb{R}$.

We remark that the controller implementation in (11) is not unique, and refer to such a controller as a realized controller. An infinite number of equivalent realizations of the base controller \mathcal{C} exist that result in the same control signal $u_i(t)$ at the vehicle for $\delta_{i,j} = 0$. For instance, consider the CACC controller in [15], with a change of coordinates $\frac{\tau}{h}\xi_{i,2} = \frac{\tau}{h}a_{i-1} + (1 - \frac{\tau}{h})a_i - \xi_{i,1}$ and new controller state $\xi_{i,2} \in \mathbb{R}$. Applying this coordinate transformation to (9), and using the available sensors in (10), a second realized controller, \mathcal{C}_2 , can be obtained as

$$\mathcal{C}_2 := \begin{cases} \dot{\xi}_{i,2} = -\frac{1+k_{dd}}{\tau}\xi_{i,2} - \frac{k_p}{\tau}y_{i,1} + \frac{k_p h}{\tau}y_{i,2} \\ \quad + \frac{k_{dh}}{\tau}y_{i,3} - \frac{k_d}{\tau}y_{i,4} + \frac{k_p}{\tau}r_i, \\ u_i = \frac{\tau}{h}y_{i,5} + (1 - \frac{\tau}{h})y_{i,3} - \frac{\tau}{h}\xi_{i,2}. \end{cases} \quad (12)$$

That is, we have two different realizations, \mathcal{C}_1 and \mathcal{C}_2 , of the CACC controller in (9) — each result in the same control signal $u_i(t)$ applied to the vehicle for $\delta_{i,j}(t) = 0$. Note that \mathcal{C}_2 requires the actual acceleration of the preceding vehicle, whereas \mathcal{C}_1 requires the control input of the preceding vehicle. However, when $\delta_{i,j}(t) \neq 0$, for some $t \geq 0$, they will, in general, lead to different control signals $u_i(t)$.

To quantify the impact of the attack on the two different controller realizations, we are interested in the reachable sets induced by the attack signals $\delta_{i,j}(t)$ and use the size of these sets as a security metric. Here, we are interested in assessing whether \mathcal{C}_1 and \mathcal{C}_2 lead to different sensitivity to attacks for

the same class of resource-limited adversaries for varying system and control parameters.

IV. ADVERSARIAL LTI SYSTEM

A. Closed-Loop Platooning Dynamics

Using the above expressions for the vehicle dynamics (8), sensors (10), and realized controllers \mathcal{C}_1 or \mathcal{C}_2 , we can write the closed-loop tracking dynamics in terms of the attack signals $\delta_{i,j}(t)$ introduced in (10). To make a fair comparison between the realized controllers \mathcal{C}_1 and \mathcal{C}_2 , we write them in the same coordinates. First, consider (11) and the change of coordinates $\xi_{i,1} = \frac{\tau}{h}a_{i-1} + (1 - \frac{\tau}{h})a_i - \frac{\tau}{h}\zeta_{i,1}$ (this is the same transformation, though inverse, that relates \mathcal{C}_1 and \mathcal{C}_2 above), with new controller state $\zeta_{i,1} \in \mathbb{R}$. Then, after some computations, (11) can be written in terms of $\zeta_{i,1}$ and $\delta_{i,j}$ as follows:

$$\mathcal{C}_1 := \begin{cases} \dot{\zeta}_{i,1} = -\frac{1+k_{dd}}{\tau}\zeta_{i,1} - \frac{k_p}{\tau}e_i - \frac{k_d}{\tau}\dot{e}_i - \frac{k_p}{\tau}\delta_{i,1} \\ \quad + \frac{k_p h}{\tau}\delta_{i,2} + \left(\frac{k_{dh}+k_{dd}}{\tau} - \frac{k_{dd}h}{\tau^2}\right)\delta_{i,3} \\ \quad - \frac{k_d}{\tau}\delta_{i,4} - \frac{k_{dd}}{\tau}\delta_{i,5} - \frac{1}{\tau}\delta_{i,6}, \\ u_i = -\frac{\tau}{h}\zeta_{i,1} + \frac{\tau}{h}a_{i-1} + \left(1 - \frac{\tau}{h}\right)a_i. \end{cases} \quad (13)$$

Define the stacked state vector $\hat{x}_i := \text{col}[e_i, \dot{e}_i, \zeta_{i,1}, z_i]$, where $z_i(t) := q_{i-1} - q_i - L_i - r_i$. Then, the resulting closed-loop dynamics (8), (10), (12) can be written as follows:

$$\dot{\hat{x}}_i := A^c \hat{x}_i + B_v^c v_{i-1} + \sum_{j \in \mathcal{L}} \hat{\Gamma}_j^c \delta_{i,j} \quad (14)$$

with system matrices

$$A^c := \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ -\frac{k_p}{\tau} & -\frac{k_d}{\tau} & -\frac{1+k_{dd}}{\tau} & 0 \\ -\frac{1}{h} & 0 & 0 & -\frac{1}{h} \end{bmatrix}, B_v^c := \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}, \quad (15)$$

and attack matrices $\hat{\Gamma}_j^c$

$$\left\{ \begin{array}{l} \hat{\Gamma}_1^c := \begin{bmatrix} 0 \\ 0 \\ -\frac{k_p}{\tau} \\ 0 \end{bmatrix}, \hat{\Gamma}_2^c := \begin{bmatrix} 0 \\ 0 \\ \frac{k_p h}{\tau} \\ 0 \end{bmatrix}, \hat{\Gamma}_3^c := \begin{bmatrix} 0 \\ 0 \\ \frac{k_{dh}+k_{dd}}{\tau} - \frac{k_{dd}h}{\tau^2} \\ 0 \end{bmatrix}, \\ \hat{\Gamma}_4^c := \begin{bmatrix} 0 \\ 0 \\ -\frac{k_d}{\tau} \\ 0 \end{bmatrix}, \hat{\Gamma}_5^c := \begin{bmatrix} 0 \\ 0 \\ -\frac{k_{dd}}{\tau} \\ 0 \end{bmatrix}, \hat{\Gamma}_6^c := \begin{bmatrix} 0 \\ 0 \\ -\frac{1}{\tau} \\ 0 \end{bmatrix}. \end{array} \right. \quad (16)$$

Here, we have introduced the index set $\mathcal{L} \subseteq \{1, \dots, 6\}$, which denotes the set of compromised sensors in (10) (i.e. $\delta_{i,j}(t) \neq 0$ for $j \in \mathcal{L}$ and some $t \geq 0$). Similarly, \mathcal{C}_2 can be written as follows:

$$\mathcal{C}_2 := \begin{cases} \dot{\xi}_{i,2} = -\frac{1+k_{dd}}{\tau}\xi_{i,2} - \frac{k_p}{\tau}e_i - \frac{k_d}{\tau}\dot{e}_i - \frac{k_p}{\tau}\delta_{i,1} \\ \quad + \frac{k_p h}{\tau}\delta_{i,2} + \frac{k_{dh}}{\tau}\delta_{i,3} - \frac{k_d}{\tau}\delta_{i,4}, \\ u_i = -\frac{\tau}{h}\xi_{i,2} + \left(1 - \frac{\tau}{h}\right)a_i + \frac{\tau}{h}a_{i-1} \\ \quad + \left(1 - \frac{\tau}{h}\right)\delta_{i,3} + \frac{\tau}{h}\delta_{i,5}. \end{cases} \quad (17)$$

Then, the closed-loop dynamics (8), (10), (17) is given by

$$\dot{\hat{x}}_i := A^c \hat{x}_i + B_v^c v_{i-1} + \sum_{j \in \mathcal{L}} \bar{\Gamma}_j^c \delta_{i,j}, \quad (18)$$

where $\bar{x}_i := \text{col}[e_i, \dot{e}_i, \xi_{i,2}, z_i]$, $\bar{\Gamma}_1^c = \hat{\Gamma}_1^c$, $\bar{\Gamma}_2^c = \hat{\Gamma}_2^c$, $\bar{\Gamma}_4^c = \hat{\Gamma}_4^c$, A^c and B_v^c as defined in (15), and

$$\bar{\Gamma}_3^c := \begin{bmatrix} 0 \\ 1 - \frac{h}{\tau} \\ \frac{k_d h}{\tau} \\ 0 \end{bmatrix}, \bar{\Gamma}_5^c := \begin{bmatrix} 0 \\ -1 \\ 0 \\ 0 \end{bmatrix}, \bar{\Gamma}_6^c := \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}. \quad (19)$$

Because platooning controllers run in discrete time, and attacks operate on sampled signals, discrete-time equivalent models of (14) and (18) are obtained via exact discretization at the sampling time instant, $t = T_s k$, $k \in \mathbb{N}$, with sampling interval $T_s > 0$, assuming zero-order hold on the control input $u_i(t)$. The equivalent discrete-time models for (14) and (18) can be written compactly as:

$$\hat{x}_i(k+1) = A\hat{x}_i(k) + B_v v_{i-1}(k) + \sum_{j \in \mathcal{L}} \hat{\Gamma}_j \delta_{i,j}(k), \quad (20a)$$

$$\bar{x}_i(k+1) = A\bar{x}_i(k) + B_v v_{i-1}(k) + \sum_{j \in \mathcal{L}} \bar{\Gamma}_j \delta_{i,j}(k) \quad (20b)$$

with

$$\begin{cases} A = e^{A^c T_s}, B_v = \left(\int_0^{T_s} e^{A^c(T_s-s)} ds \right) B_v^c, \\ \hat{\Gamma}_j = \left(\int_0^{T_s} e^{A^c(T_s-s)} ds \right) \hat{\Gamma}_j^c, \forall j \in \mathcal{L}, \\ \bar{\Gamma}_j = \left(\int_0^{T_s} e^{A^c(T_s-s)} ds \right) \bar{\Gamma}_j^c, \forall j \in \mathcal{L}. \end{cases} \quad (21)$$

B. Adversarial Reachable Sets

We are primarily interested in resource-limited attacks — attacks that tamper with sensing, actuation, and networked data while being constrained by factors such as physical limitations, computing power, and attack strategy [9]. We model these constraints as hard bounds on attack signals $\delta_{i,j}(k)$. We also impose a hard bound on the velocity of the preceding vehicle, v_{i-1} , as it enters the closed-loop dynamics (see (20)) as an external disturbance that will affect the system trajectories. Having bounded velocity is reasonable as v_{i-1} is constrained by the physical limitations of the vehicle and highway speed limits. The constraints we impose have the following structure:

$$\delta_{i,j}(k) \in \{\delta_{i,j}(k) \mid \delta_{i,j}^2 \leq W_{i,j}^2\}, \forall k \in \mathbb{N}, j \in \mathcal{L}, \quad (22a)$$

$$v_{i-1}(k) \in \{v_{i-1}(k) \mid v_{i-1}^2 \leq \bar{v}^2\}, \forall k \in \mathbb{N}, \quad (22b)$$

for some known constants $W_{i,j} \in \mathbb{R}_{>0}$ and $\bar{v} \in \mathbb{R}_{>0}$. Associated with these constraints, we introduce the notion of adversarial reachable sets for (20a):

$$\mathcal{R}^{\hat{x}_i}(k) := \left\{ \hat{x}_i \in \mathbb{R}^4 \begin{cases} \hat{x}_i = \hat{x}_i(k), \\ \hat{x}_i(k) \text{ solution to (20a),} \\ \delta_{i,j}(k) \text{ satisfies (22a),} \\ v_{i-1}(k) \text{ satisfies (22b),} \end{cases} \right\}, \quad (23)$$

and for (20b):

$$\mathcal{R}^{\bar{x}_i}(k) := \left\{ \bar{x}_i \in \mathbb{R}^4 \begin{cases} \bar{x}_i = \bar{x}_i(k), \\ \bar{x}_i(k) \text{ solution to (20b),} \\ \delta_{i,j}(k) \text{ satisfies (22a),} \\ v_{i-1}(k) \text{ satisfies (22b),} \end{cases} \right\}. \quad (24)$$

To quantify the adversarial capabilities of attacks, the volume of these adversarial reachable sets can serve as a security metric [12]. This metric provides insight into the size of the state space portion that can be induced by a series of attacks. However, computing the exact value of $\mathcal{R}^{\hat{x}_i}(k)$ is generally not tractable and k -dependent. Instead, we seek to obtain the outer ellipsoidal approximation $\mathcal{E}^{\hat{x}_i}(k)$ via Lemma 1, where due to $a \in (0, 1)$ in Lemma 1, the sequence $\alpha_i^{\hat{x}_i}(k)$ shaping the ellipsoid $\mathcal{E}^{\hat{x}_i}(k)$ converges to $\alpha_i^{\hat{x}_i}(\infty) := (N - a)/(1 - a)$ exponentially fast. Therefore, in a few steps, $\mathcal{E}^{\hat{x}_i}(k) \approx \mathcal{E}^{\hat{x}_i}(\infty) := \{\hat{x}_i \mid \hat{x}_i^\top \mathcal{P}^{\hat{x}_i} \hat{x}_i \leq (N - a)/(1 - a)\}$, for some positive definite matrix $\mathcal{P}^{\hat{x}_i} \in \mathbb{R}^{4 \times 4}$, and where N is the number of disturbances (according (22)) acting on the system, hence $N = 1 + \text{card}[\mathcal{L}]$, where $\text{card}[\cdot]$ denotes cardinality. The volume of the ellipsoidal approximation $\mathcal{E}^{\hat{x}_i}(\infty)$ (similarly for $\mathcal{E}^{\bar{x}_i}(\infty)$) is used as an over-approximation of the proposed security metric. Note that, as we consider the reachable set at infinity, the security analysis is independent of the initial condition.

V. SECURITY ASSESSMENT

In this section, we use Lemma 1 to find the smallest ellipsoidal approximation of the adversarial reachable sets (23) and (24) for different subsets of sensors (10) being attacked. We introduce the notion of critical states, denoted as \mathcal{D}^{x_i} , which characterizes states that, if reached, compromise the safety and integrity of the vehicle. These critical states may include situations such as collisions between vehicles or a vehicle exceeding the speed limit on the highway. If the intersection between the set of critical states and a reachable set $\mathcal{R}^{x_i}(k)$ is not empty; then, there exist attack signals $\delta_{i,j}(k)$ satisfying (22a) that can drive the vehicle to a critical state. Consider the inter-vehicle distance state z_i , and note that $q_{i-1} - q_i - L_i = z_i + r_i \leq 0$ indicates that a collision between vehicles i and $i-1$ has occurred. Therefore, a subset of states \hat{x}_i and \bar{x}_i that represents collision can be written as $z_i \leq r_i$. Similarly, the vehicle velocities v_i exceeding a speed limit, say \bar{v}_i , can be formulated as $\frac{1}{h} z_i - \frac{1}{h} e_i > \bar{v}_i$.

These two sets of critical states and ellipsoidal approximations, projected onto the v_i - z_i plane via Lemma 2 and applying a coordinate transformation $\tilde{x} = [v_i \ z_i \ \dot{e}_i \ \zeta_{i,1}]^\top = S\hat{x}$, (similarly for $\tilde{\bar{x}}$), such that, $\mathcal{E}^{\tilde{x}_i}(\infty) := \{\tilde{x}_i \mid \tilde{x}_i^\top (S^{-1})^\top \mathcal{P}^{\hat{x}_i} S^{-1} \tilde{x}_i \leq (N - a)/(1 - a)\}$. This transformation allows the characterizing of security using the size of the ellipsoids and their intersection with critical states. Note that the proposed critical states are used as an example, but the analysis can also be applied to different safety constraints.

We consider the closed-loop dynamics (20a), (21) for \mathcal{C}_1 , and (20b), (21) for \mathcal{C}_2 , with a desired inter-vehicle distance of

$r_i = 3$ m, driveline dynamics constant $\tau = 0.1$ s, time headway constant $h = 0.5$ s, controller gains of $(k_p, k_d, k_{dd}) = (0.2, 0.7, 0)$, and sampling rate of $T_s = 0.01$ s. Additionally, we assume a speed limit of $\bar{v}_i = 35.83$ m/s. For the resource-limited FDI attacks $\delta_{i,j}(k)$, we assume that the attacks remain within the bound specified by (22a) with $W_{i,j} = 1$, for all $j \in \mathcal{L}$. The bound $W_{i,j}$ is an arbitrarily chosen value, as we are only interested in the differences in the proposed metrics between the two controller realizations.

A. Sensor Sensitivity

The first case study focuses on individual sensor attacks, offering valuable insights into the importance of protecting specific sensors during cyber attacks. This case study also indicates which sensors are more critical to be protected when there are resource limitations and not all sensors can be secured. In Table I, the numerical values of volumes of $\mathcal{E}^{\hat{x}_1}(\infty)$ and $\mathcal{E}^{\bar{x}_1}(\infty)$ (i.e., for both realized controllers \mathcal{C}_1 and \mathcal{C}_2) are given. Upon comparing the different individual attacks, \mathcal{C}_2 proves to be highly sensitive to an attack on the onboard acceleration measurement $y_{i,3}$. As for the realization it holds that $k_{dd} = 0$, resulting in an equivalent attack on ξ_i when comparing $\hat{\Gamma}_3^c$ and $\bar{\Gamma}_3^c$. However, due to the different realization, the error dynamics \ddot{e} in \mathcal{C}_2 is also affected by an attack on $y_{i,3}$, hence the non-zero entry in $\bar{\Gamma}_3^c$, resulting in an increased sensitivity to an attack on this particular sensor. In Fig. 2, the projection of $\mathcal{E}^{\hat{x}_1}$ and $\mathcal{E}^{\bar{x}_1}$ (onto the v_i - z_i plane) for $\mathcal{L} = 3$ is shown. The orange dashed lines indicate the boundaries of the critical states, where it can be observed that \mathcal{C}_2 suffers significantly more as the number of states the attack can induce is much larger.

Based on the comparison of the different volumes in Table I, it can be concluded that \mathcal{C}_1 has greater overall robustness against resource-limited attacks. The attack in which \mathcal{C}_2 outperforms \mathcal{C}_1 is in the case of a cyber-attack on u_{i-1} ($\mathcal{L} = 6$). However, it should be noted that an attack on u_{i-1} is equivalent to an attack on a_{i-1} , as both values are typically obtained through V2V communication. As a result, the comparison between scenarios $\mathcal{L} = 5$ and $\mathcal{L} = 6$ does not indicate any advantage of using one realization over the other. Furthermore, it is worth noting that for \mathcal{C}_1 , the information of the predecessor — namely v_{i-1} and u_{i-1} — is important to protect, especially when resources are limited. This emphasizes the need for enhanced security against cyber-attacks, highlighting the importance of safeguarding such critical information.

\mathcal{L}	1	2	3	4	5	6
$\text{Vol}(\mathcal{E}^{\hat{x}_i})$	192.92	96.46	337.64	675.59	0.01	965.73
$\text{Vol}(\mathcal{E}^{\bar{x}_i})$	192.92	96.46	3523.42	675.59	951.81	0.01

TABLE I

NUMERICAL VALUES OF VOLUMES OF $\mathcal{E}^{\hat{x}_i}(\infty)$ AND $\mathcal{E}^{\bar{x}_i}(\infty)$ (I.E., FOR BOTH REALIZED CONTROLLERS \mathcal{C}_1 AND \mathcal{C}_2).

B. Varying Constant Headway h

In this section, we present a second case study, which explores the impact of the time headway constant h on the

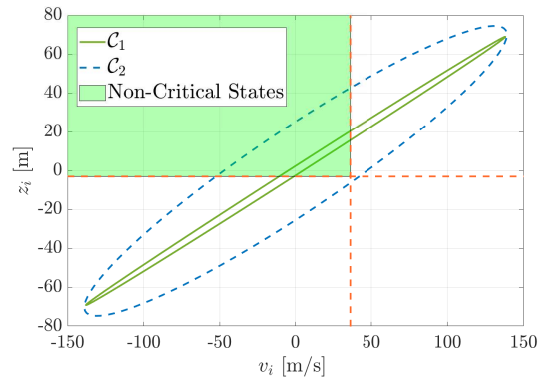


Fig. 2. Projection of $\mathcal{E}^{\hat{x}_i}(\infty)$ and $\mathcal{E}^{\bar{x}_i}(\infty)$ for an attack on acceleration sensor $y_{i,3}$, hence $\mathcal{L} = 3$.

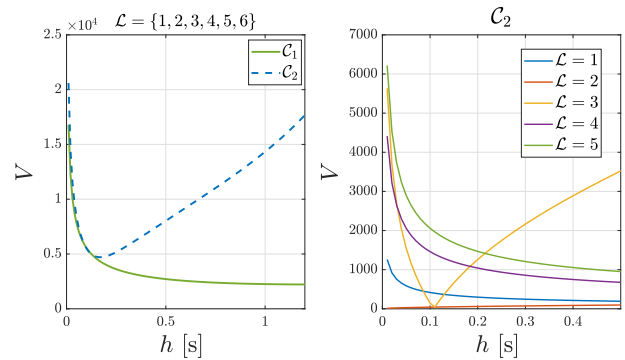


Fig. 3. (Left) The volume of $\mathcal{E}^{\hat{x}_i}(\infty)$ and $\mathcal{E}^{\bar{x}_i}(\infty)$ for $\mathcal{L} = \{1, 2, 3, 4, 5, 6\}$ for varying headway constant h . (Right) The volume of $\mathcal{E}^{\bar{x}_i}(\infty)$ for varying headway constant h and individual sensor attacks.

ellipsoidal approximation of the adversarial reachable set for the same system introduced in section V-A.

We assume that $\mathcal{L} = \{1, 2, 3, 4, 5, 6\}$, indicating that all sensors in (10) are compromised. The left plot in Fig. 3 shows the projected ellipsoids' volume of both $\mathcal{E}^{\hat{x}_i}(\infty)$ and $\mathcal{E}^{\bar{x}_i}(\infty)$ on the v_i - z_i plane for different values of $h \in [0.01, 0.02, \dots, 1.2]$. The results show that the volume of $\mathcal{E}^{\hat{x}_i}$ has an exponential decay for $h < 1$, indicating more resiliency, however for $h > 1$ the volume slightly increases. It is observed that the volume of $\mathcal{E}^{\hat{x}_i}$ is always smaller than $\mathcal{E}^{\bar{x}_i}$, but decays more slowly. However, for $h > 0.1$, the volume of $\mathcal{E}^{\bar{x}_i}$ increases exponentially. To analyze this behavior, the right plot in Fig. 3 shows the volume of $\mathcal{E}^{\bar{x}_i}$ for single sensor attacks. It is clear that for $\mathcal{L} = 3$ and $h > 0.1$, the volume begins to increase exponentially. Since k_{dd} is set to be zero, the only difference between $\hat{\Gamma}_3$ and $\bar{\Gamma}_3$ is the additional term $1 - \frac{h}{\tau}$, where the volume starts increasing when this term switches to a negative term. Future work should include an analysis of why the additional term in $\bar{\Gamma}_3$ causes exponential growth of the volume.

Additionally, it is noted that the volume alone does not provide a representative metric for selecting the optimal value of h . In Fig. 3 $\mathcal{E}^{\hat{x}_i}(\infty)$ and $\mathcal{E}^{\bar{x}_i}(\infty)$ are projected onto the v_i - z_i plane, showing that the orientation of the ellipsoids are affected for different values of h . Thus, the optimal controller does not necessarily have the smallest volume, but has the smallest intersection with the critical

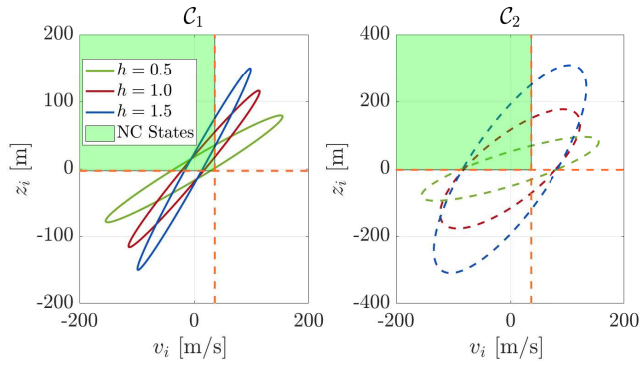


Fig. 4. (Left) Projection $\mathcal{E}^{\hat{x}_i}(\infty)$ onto v_i - z_i plane for different h and $\mathcal{L} = \{1, 2, 3, 4, 5, 6\}$. (Right) Projection $\mathcal{E}^{\bar{x}_i}(\infty)$ onto v_i - z_i plane for different h and $\mathcal{L} = \{1, 2, 3, 4, 5, 6\}$. The green area represents the Non-Critical States (NC-States).

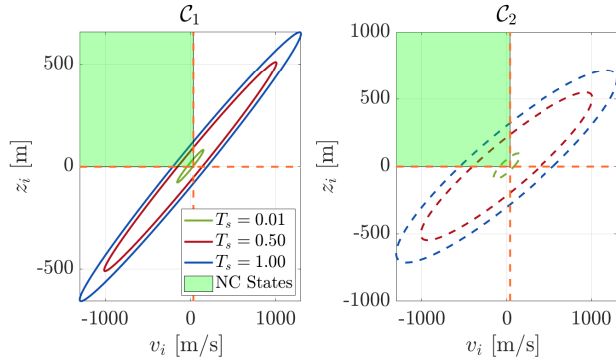


Fig. 5. (Left) Projection $\mathcal{E}^{\hat{x}_i}(\infty)$ onto v_i - z_i plane for different T_s and $\mathcal{L} = \{1, 2, 3, 4, 5, 6\}$. (Right) Projection $\mathcal{E}^{\bar{x}_i}(\infty)$ onto v_i - z_i plane for different T_s and $\mathcal{L} = \{1, 2, 3, 4, 5, 6\}$. The green area represents the Non-Critical States (NC-States).

states, indicating a potential new security metric.

C. Varying Sampling Constant T_s

This section discusses the final case study, where the effect of the sampling rate T_s on $\mathcal{E}^{\hat{x}_i}(\infty)$ and $\mathcal{E}^{\bar{x}_i}(\infty)$ is examined. Since the CACC can be applied to various vehicles / operating systems, it is most likely for the sampling rate to differ. Assuming a zero-order hold for the controller input, the closed-loop system performance can be affected.

The obtained results are similar to the previous two case studies, where in Fig. 5 $\mathcal{E}^{\hat{x}_i}(\infty)$ and $\mathcal{E}^{\bar{x}_i}(\infty)$ are projected onto the v_i - z_i plane for different values of T_s , indicating that C_1 is more resilient against attacks than C_2 for varying T_s . However, where h also affected the orientation of the ellipsoid, T_s only affects the size of the ellipsoid. Since T_s only alters the input rate, it is expected to only affect the volume, as changing h results in a different control goal and increased distance between vehicle i and its predecessor $i-1$.

VI. CONCLUSIONS AND FUTURE WORKS

CACC schemes must ensure safety and reliability in adversarial environments. In this paper, we have argued that for a given dynamic CACC scheme, an infinite number of real-time realizations of the same controller exist given the available sensors. It is shown that different controller realizations can significantly affect the impact of resource-limited attacks. Two different controller realizations are

compared by computing outer ellipsoidal approximations of reachable sets induced by attacks, and evaluated how the sampling and headway constant change these sets. As a result, it is concluded that the sensitivity of the system changes significantly for the same class of attacks. Therefore, these results indicate that there exist optimal controllers that minimize the system sensitivity to resource-limited attacks.

In this manuscript, we have also highlighted the importance of incorporating new security metrics. Changing the controller affects the orientation of the ellipsoidal approximation, resulting in different intersections between critical states and adversarial reachable sets. Therefore, comparing different controller realizations by means of these intersections provides more insight into the vulnerabilities of the system in terms of safety. Additionally, future work should incorporate an analysis of how an attack propagates through the platooning behavior by considering more vehicles.

REFERENCES

- [1] J. Ploeg, D. P. Shukla, N. van de Wouw, and H. Nijmeijer, "Lp String Stability of Cascaded Systems: Application to Vehicle Platooning", *IEEE Trans. on Control Syst. Techn.*, vol. 22, p. 786–793, 2014
- [2] M. Amoozadeh, A. Raghuramu, C. Chuah, D. Ghosal, M. Zhang, J. Rowe, and K. Levitt, "Security vulnerabilities of connected vehicle streams and their impact on cooperative driving", *IEEE Communications Magazine*, vol. 63, p. 126–132, 2015
- [3] Z.-E. El-Rewini, K. Sadatsharan, D. F. Selvaraj, S. J. Plathottam, and P. Ranganathan, "Cybersecurity Challenges in Vehicular Communications", *Vehicular Communications*, vol. 23, 2020
- [4] Z. Ju, H. Zhang, L. Ziang, C. Xiaoguang, H. Jinpeng, and M. Yang, "A Survey on Attack Detection and Resilience for Connected and Automated Vehicles: From Vehicle Dynamics and Control Perspective," *IEEE Transactions on Intelligent Vehicles*, vol. 7, p. 815–837, 2022
- [5] X. Sun, F. R. Yu, and Z. Zhang, "A Survey on Cyber-Security of Connected and Autonomous Vehicles (CAVs)", in *IEEE Transactions on Intelligent Transportation Systems*, vol. 23, no. 7, p. 6240-6259, Jul. 2022
- [6] A. Teixeira, I. Shames, H. Sandberg, and K. H. Johansson, "A Secure Control Framework for Resource-Limited Adversaries, in *Automatica*, vol. 51, p. 135-148, Jan. 2015
- [7] A. Chowdhury, G. Karmakar, J. Kamruzzaman, A. Jolfaei, and R. Das, "Attacks on Self-Driving Cars and Their Countermeasures: A Survey", in *IEEE Access*, vol. 8, p. 207308 - 207342, 2020
- [8] Z. Ju, H. Zhang, X. Li, X. Chen, J. Han, and M. Yang, "A Survey on Attack Detection and Resilience for Connected and Automated Vehicles: From Vehicle Dynamics and Control Perspective", in *IEEE Transactions on Intelligent Vehicles*, vol. 7, no. 4, p. 815-837, Dec. 2022
- [9] X.-M. Zhang, Q.-L. Han, X. Ge et al., "Networked Control Systems: A Survey of Trends and Techniques", in *IEEE/CAA Journal of Automatica Sinica*, p. 1-17, 2019
- [10] Z. van der Heijden, T. Lukaseder, and F. Kargl, "Analyzing Attacks on Cooperative Adaptive Cruise Control (CACC)", *2017 IEEE Vehicular Networking Conference (VNC)*, p. 45–52, 2017
- [11] S. Dadras, S. Dadras, and C. Winstead, "Reachable Set Analysis of Vehicular Platooning in Adversarial Environment", *2018 Annual American Control Conference (ACC)*, p. 5568–5575, 2018
- [12] C. Murguia, I. Shames, J. Ruths, and D. Nešić, "Security metrics and synthesis of secure control systems," *Automatica*, vol. 115, p. 108757, 2020
- [13] S. H. Kafash, J. Giraldo, C. Murguia, A. A. Cardenas, and J. Ruths, "Constraining Attack Capabilities Through Actuator Saturation", in *2018 Annual American Control Conference (ACC)*, p. 986-991, Jun. 2018
- [14] S. Boyd, L. El Ghaoui, E. Feron, and V. Balakrishnan, "Linear Matrix Inequalities in System and Control Theory", *SIAM*, 1994
- [15] E. Lefeber, J. Ploeg, and H. Nijmeijer, "Cooperative Adaptive Cruise Control of Heterogeneous Vehicle Platoons", in *IFAC-PapersOnLine*, vol. 53, no. 2, pp. 15217 - 15222, 2020