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Citation for published version (APA):

DOI:
10.1109/TVT.2007.907308

Document status and date:
Published: 01/01/2008

Document Version:
Publisher’s PDF, also known as Version of Record (includes final page, issue and volume numbers)

Please check the document version of this publication:
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Impact Analysis of Directional Antennas and Multiantenna Beamformers on Radio Transmission

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Abstract—The impact of directional antennas and multiantenna beamformers on radio transmission is formulated in terms of the gain of the Rician $K$-factor, the reduction of the root-mean-squared delay spread, and the gain of the signal-to-noise ratio at the receiver for Rician fading channels in multipath environments. The analysis is based on a double-directional channel model. For the analytical formulation, the joint channel spectrum is assumed to be decomposable into separate spectra in time and angular domains. By way of illustration, closed-form expressions for the impact of hypothetical cosine-shaped antenna patterns and conventional beamformers are derived for channels with uniform angular spectra and an exponential decaying delay spectrum. The impact factors are explicitly related to the antenna beamwidth and the number of antenna elements. In addition, the effect of misalignment between the antenna main beam and the direct path is included in the analysis. The quantitative analysis given in this paper is important for radio system design, particularly for the design of antennas and multiantenna beamformer configurations.

Index Terms—Conventional beamforming, double-directional channel, half-power beamwidth (HPBW), multiantenna beamforming, Rician $K$-factor, root-mean-squared (rms) delay spread (RDS).

I. INTRODUCTION

It is well known that applying directional antennas in wireless communication systems increases the signal power level in the receiver, reduces the multipath dispersive effect, and reduces the cochannel interference from other users [1], [2], [6]–[8]. An alternative but more flexible way is to use multiple antennas for directional beamforming. In particular, for wideband radio systems, such as the multigigabit-per-second system deployed at the frequency band of around 60 GHz, multiantenna beamforming is advantageous to high-data-rate transmission. In indoor line-of-sight (LOS) street environments was experimentally studied in [13] for different beamwidths, and the effect of main beam misalignment was observed as well. In [13], it was found that the reduction of RDS is in the range of 35%–55% for directional antenna configurations in comparison with the omnidirectional one in indoor LOS environments. Extensive measurements and simulations were conducted in [9], [11], [12], and [14] for indoor LOS communication at 19.37 and 60 GHz, respectively. Their results indicated that the use of fairly narrow antenna beamwidths could be accepted as an alternative to adaptive equalization or multicarrier modulation for high-data-rate transmission in indoor LOS and some non-LOS scenarios.

The theory of analyzing the effect of antennas on radio transmission was introduced in [1], in which the effect of directional antennas on the signal-level and level-crossing rates was analyzed. In [15], a general expression was derived to compute the mean effective gain of mobile antennas for Rayleigh fading channels with both vertical and horizontal polarizations taken into account. A theoretical analysis of the mean effective gain of antennas in Rician channels was conducted in [16] and [17]. Clearly, the gain analysis only involves the mutual effect between the antenna power gain pattern and the power angular distribution of the multipath waves.

However, to the best of the authors’ knowledge, the theoretical analysis concerning the reduction of multipath time dispersion caused by directional antennas has not been reported in the literature. The concept of double-directional channels was proposed earlier and applied to take into account the angular information of wave propagation at both the transmitter (TX) and receiver (RX) sides for channel characterization [18], [19]. The description of double-directional channels is particularly important for systems with multiple antennas at both the TX and RX sides. This paper aims to introduce a theoretical analysis on the impact of the antenna pattern on radio transmission, including signal-to-noise ratio (SNR) gain, Rician $K$-factor gain, and RDS reduction, in double-directional Rician channels.

This paper is organized as follows. Section II describes the signal and channel models applied in this paper and formulates the antenna effect on radio transmission. The approach used in Section II will be extended to multiantenna beamforming
in Section III. Based on the channel and antenna assumptions introduced in Section IV, examples are illustrated in Section V for a hypothetical cosine-shaped antenna pattern and a conventional beamformer. Finally, conclusions are discussed in Section VI.

II. SIGNAL MODEL, CHANNEL CHARACTERISTICS, AND ANTENNA EFFECT

Consider a radio transmission system where the signal propagation paths and the antennas at the transmitter and receiver sides are positioned in the spherical coordinate system shown in Fig. 1. Here, \( \Omega \) is the coordinate point on a spherical surface given by \((\theta, \phi)\), where \( \theta \in [0, \pi] \) and \( \phi \in [-\pi, \pi] \) represent the elevation and azimuth angles, respectively. The direction \( \Omega_x = (\theta_x, \phi_x) \) with \( x \in \{t, r\} \) stands for the direction of the departed path at the TX side or the incident path at the RX side, respectively. Here, we assume that the same single-polarized antennas are used at the TX and RX sides. For a wideband transmission system, the baseband received signal at time \( t \) can be expressed as

\[
y(t) = \sum_{n=0}^{N} h_n \sqrt{A_t(\Omega_{t,n}, \Psi_t) A_r(\Omega_{r,n}, \Psi_r)} \cdot s(t - \tau_n) + n(t)
\]

where \( A_x(\Omega_x, \Psi_x) \) for \( x \in \{t, r\} \) are the TX and RX antenna power patterns with \( \Psi_x = (\upsilon_x, \psi_x) \) as the direction of the antenna main lobe, \( s(t) \) is the baseband transmitted signal, and \( n(t) \) is the additive white Gaussian noise (AWGN). The transmit power is \( E\{|s(t)|^2\} = E_s \), and the noise power is \( E\{|n(t)|^2\} = N_0 \), within the receiver bandwidth, where \( E\{\cdot\} \) denotes an expectation operation. The channel parameters \( \{N, h_n, \tau_n, \Omega_{t,n}, \Omega_{r,n}\} \) are the random channel variables, i.e., the number of scattered paths, the complex amplitude, the time of arrival (TOA), the direction of departure (DOD), and the direction of arrival (DOA) of the \( n \)th multipath wave, respectively. The channel parameters of the LOS wave are \( \{h_0, \tau_0, \Omega_{t,0}, \Omega_{r,0}\} \), where \( \Omega_{x,0} = (\theta_{x,0}, \phi_{x,0}) \).

It should be noticed that for physical channels, the channel parameters in (1) are in general randomly time-varying variables because of the arbitrary movements of the transmitter, receiver, or surrounding objects. In practice, it is reasonable to assume that the channel statistic is stationary or quasi-static, i.e., wide-sense stationary (WSS), within the time duration of one transmitted symbol or one data package. For this reason, the time dependency of the channel parameters has been omitted in (1). Moreover, signals coming via different paths will experience uncorrelated attenuations and time delays, which are referred to as uncorrelated scattering (US). The assumption of WSS and US (WSSUS) on physical channels has been experimentally confirmed and widely accepted in the literature [2]–[5]. In the rest of this paper, time-invariant channels in a local area will be considered under the WSSUS assumption.

A. Double-Directional Channel Model Without Antenna Effect

From the received signal model (1), a double-directional channel model can be retrieved to describe the channel behavior in the time, DOD, and DOA domains. For the channel configured with isotropic antennas at both TX and RX sides, the instantaneous delay–DOD–DOA channel function and the instantaneous power delay–DOD–DOA spectrum, respectively, can be written as

\[
h(\tau, \Omega_t, \Omega_r) = \sum_{n=0}^{N} h_n \delta(\tau - \tau_n) \delta(\Omega_t - \Omega_{t,n}) \delta(\Omega_r - \Omega_{r,n}) \tag{2}
\]

\[
P_I(\tau, \Omega_t, \Omega_r) = \sum_{n=0}^{N} |h_n|^2 \delta(\tau - \tau_n) \delta(\Omega_t - \Omega_{t,n}) \delta(\Omega_r - \Omega_{r,n}) \tag{3}
\]

Under the WSSUS assumption, the local-mean power delay–DOD–DOA spectrum can be obtained by taking the average over the instantaneous power spectra in a local area and can be expressed by [19], [20]

\[
P(\tau, \Omega_t, \Omega_r) = E \{P_I(\tau, \Omega_t, \Omega_r)\} = E\{|h_0|^2\} \delta(\tau) \delta(\Omega_t - \Omega_{t,0}) \delta(\Omega_r - \Omega_{r,0}) + P_S(\tau, \Omega_t, \Omega_r) \tag{4}
\]

where

\[
P_S(\tau, \Omega_t, \Omega_r) = E\left\{\sum_{n=1}^{N} |h_n|^2 \delta(\tau - \tau_n) \delta(\Omega_t - \Omega_{t,n}) \delta(\Omega_r - \Omega_{r,n})\right\} \tag{5}
\]

is the power spectrum caused by scattered multipath waves. For convenience, the TOA of the LOS path was set to be \( \tau_0 = 0 \) in (4). Notice that \( P(\cdot) \) and \( P_S(\cdot) \) denote the channel power spectrum with and without the LOS path, respectively, for isotropic antenna patterns. The joint and separate spectra should be distinguished according to the parameters within (\cdot).
Later, similar notations $P'(\cdot)$ and $P'_S(\cdot)$ will be introduced to represent the channel spectra for nonisotropic antenna patterns.

Next, the power delay spectrum (PDS, or power delay profile) and the power DOD–DOA spectrum, respectively, can be derived from $P(\tau, \Omega_t, \Omega_r)$ according to

$$P(\tau) = \oint \mathcal{P}(\tau, \Omega_t, \Omega_r) d\Omega_t d\Omega_r$$

$$= \left[ E \left\{ |h_0|^2 \right\} \delta(\tau) + \oint \mathcal{P}_S(\tau, \Omega_t, \Omega_r) d\Omega_t d\Omega_r \right] \mathcal{P}_S(\tau)$$

$$= \left[ E \left\{ |h_0|^2 \right\} \delta(\tau) + \oint \mathcal{P}_S(\tau, \Omega_t, \Omega_r) d\Omega_t d\Omega_r \right] \mathcal{P}_S(\tau)$$

where $d\Omega = \sin(\theta) d\theta d\phi$ is a solid angle, and $\mathcal{P}_S(\tau)$ and $\mathcal{P}_S(\Omega_t, \Omega_r)$ are the PDS and DOD–DOA spectrum of the scattered waves, respectively. In addition, the separate power DOD and DOA spectra, respectively, can be defined by

$$\mathcal{P}_S(\Omega_t) = \oint \mathcal{P}_S(\Omega_t, \Omega_r) d\Omega_r$$

$$\mathcal{P}_S(\Omega_r) = \oint \mathcal{P}_S(\Omega_t, \Omega_r) d\Omega_t$$

If the total power of the channel is normalized, i.e.,

$$\sum_{n=0}^{N} E \left\{ |h_n|^2 \right\} = 1$$

then the SNR in the receiver is $\rho = (E_s/N_0)$ when isotropic antennas are applied and the following equations are valid:

$$\oint \oint P(\tau, \Omega_t, \Omega_r) d\Omega_t d\Omega_r = \oint P(\tau) d\tau$$

$$= \oint \oint \mathcal{P}(\Omega_t, \Omega_r) d\Omega_t d\Omega_r$$

$$= \oint \mathcal{P}(\Omega_t) d\Omega_t$$

$$= 1$$

$$\oint \oint \mathcal{P}_S(\tau, \Omega_t, \Omega_r) d\Omega_t d\Omega_r = \oint \mathcal{P}_S(\tau) d\tau$$

$$= \oint \oint \mathcal{P}_S(\Omega_t, \Omega_r) d\Omega_t d\Omega_r$$

$$= \oint \mathcal{P}_S(\Omega_r) d\Omega_r$$

$$= \frac{1}{K + 1}.$$  

Here, $1/(K + 1)$ is the power of the scattered waves, and $K$ is the ratio between the average powers contributed by the LOS path and the scattered paths, i.e.,

$$K = \frac{E \left\{ |h_0|^2 \right\}}{E \left\{ \sum_{n=1}^{N} |h_n|^2 \right\}}.$$  

The parameter $K$ is usually called the Rician $K$-factor and is used to characterize the Rician fading channel. In addition, the RDS of the channel is calculated by

$$\sigma_r = \sqrt{\frac{\int \int \mathcal{P}(\tau) d\tau}{\int \int P(\tau) d\tau} - \left( \frac{\int \int P(\tau) d\tau}{\int \int P(\tau) d\tau} \right)^2}$$

$$= \sqrt{\tau^2 - \tau_r^2}$$

where $\tau = (\int \int \mathcal{P}(\tau) d\tau / \int \int P(\tau) d\tau)$ is the mean excess delay, and $\tau_r^2 = (\int \int \mathcal{P}(\tau) d\tau / \int \int P(\tau) d\tau)$ is the second moment of the delay spectrum $P(\tau)$. The RDS $\sigma_r$ is generally used to characterize the time dispersion of the channel.

### B. Impact of Antenna Pattern on Radio Channel

When nonisotropic antennas are applied in the channel, the joint power delay–DOD–DOA spectrum becomes $P(\tau, \Omega_t, \Omega_r) A_t(\Omega_t, \Psi_t) A_r(\Omega_r, \Psi_r)$, and the separate spectra can be accordingly obtained. In particular, the PDS becomes

$$P'(\tau) = \oint \oint P(\tau, \Omega_t, \Omega_r) A_t(\Omega_t, \Psi_t) A_r(\Omega_r, \Psi_r) d\Omega_t d\Omega_r$$

$$= E \left\{ |h_0|^2 \right\} A_t(\Omega_t, \Psi_t) A_r(\Omega_r, \Psi_r) \delta(\tau) + P'_S(\tau)$$

where the delay spectrum of scattered waves is

$$P'_S(\tau) = \oint \oint P'_S(\tau, \Omega_t, \Omega_r) A_t(\Omega_t, \Psi_t) A_r(\Omega_r, \Psi_r) d\Omega_t d\Omega_r.$$  

An explicit expression of $P'_S(\tau)$ can be derived when the antenna patterns and the power delay angular spectrum $P'_S(\tau, \Omega_t, \Omega_r)$ are given.

To investigate the impact of antenna patterns on the transmission system and channel, we consider the change of the Rician $K$-factor, the RDS, and the change of the SNR caused by nonisotropic antenna patterns. In specific, the following parameters are defined for the purpose of analysis: the gain of the Rician $K$-factor

$$G_K = \frac{K'}{K}$$

the gain of the SNR

$$G_\rho = \frac{\rho'}{\rho}$$
where \( \rho \) stands for the SNR in the receiver, and the relative reduction of RDS

\[
R_{\sigma_r} = 1 - \frac{\sigma_r}{\sigma'}.
\]

(19)

Here, the two parameter sets \( \{ K, \rho, \sigma_r \} \) and \( \{ K', \beta, \sigma_r' \} \) are for the channels configured with isotropic and nonisotropic antennas, respectively. These parameters are defined to formulate the impact of antenna patterns on propagation channels and, thus, are useful for the purpose of system design.

Here, we derive explicit expressions of the impact parameters. Notice that when nonisotropic antenna patterns are used in the channel, the channel power of the LOS path \( (K/(K+1)) \) is scaled by the TX and RX antenna pattern gains \( A_t(\Omega_{t,0}, \Psi_t) \) and \( A_r(\Omega_{r,0}, \Psi_r) \) along the LOS direction \( \Omega_{x,0} = (\theta_{x,0}, \phi_{x,0}) \). Further, the power angular spectrum of scattered waves becomes

\[
P'_S(\Omega_t, \Omega_r) = P_S(\Omega_t, \Omega_r)A_t(\Omega_t, \Psi_t)A_r(\Omega_r, \Psi_r)
\]

(20)

which can be integrated to obtain the power of the scattered waves. Consequently, the power gain of the scattered waves due to TX–RX antenna patterns can be derived as

\[
E_A = (K+1) \int \int P_S(\Omega_t, \Omega_r) \cdot A_t(\Omega_t, \Psi_t)A_r(\Omega_r, \Psi_r) d\Omega_t d\Omega_r.
\]

(21)

Now the Rician \( K \)-factor gain and the SNR gain can be readily obtained as

\[
G_K = \frac{A_t(\Omega_{t,0}, \Psi_t)A_r(\Omega_{r,0}, \Psi_r)}{E_A}.
\]

(22)

\[
G_\rho = \frac{K}{K+1} A_t(\Omega_{t,0}, \Psi_t)A_r(\Omega_{r,0}, \Psi_r) + \frac{1}{K+1} E_A
\]

(23)

\[
= \beta E_A
\]

where \( \beta = (K'G_K + 1)/(K+1) \). In addition, following the definition in (14), the reduction of RDS can be derived as

\[
R_{\sigma_r} = 1 - \sqrt{\frac{\tau'^2 - \tau^2}{\tau'^2 - \tau^2}}
\]

(24)

where the mean excess delay \( \tau' = (\int \tau P'(\tau) d\tau / \int P'(\tau) d\tau) \), and the second moment of the PDS \( P'(\tau) \) is \( \tau'^2 = (\int \tau^2 P'(\tau) d\tau / \int P'(\tau) d\tau) \).

Clearly, for a certain power delay–DOD–DOA spectrum and antenna patterns, the impact of nonisotropic antennas on the channel can be analytically studied. Notice that the Rician \( K \)-factor gain and the SNR gain are independent of the PDS, and for a fixed orientation of the antenna, the SNR gain \( G_\rho \) only depends on the \( K \)-factor and the gain of the scattered waves. In addition, the RDS reduction is determined by the first and second moments of the power delay spectra before and after nonisotropic antennas are applied. These moments are related to the \( K \)-factor and the parameter \( E_A \).

III. EXTENSION TO MULTIANTELLA BEAMFORMING

The purpose of applying directional antennas in many applications is to satisfy the link budget requirement in the receiver and, at the same time, to reduce the multipath effect on data transmission. However, besides the involvement of adjusting the main beam to a certain direction, the antenna pattern beamwidth cannot be designed as narrow as we like due to the finite size of the antenna, which results in a reduced directivity. In comparison, multiple antennas can be applied to adaptively form a desired beam pattern having its maximum gain along the desired direction. In this regard, adaptive multiantenna beamforming becomes a better solution to increase the mobility of a transceiver system, to further increase the directivity, and to reduce the multipath effect. To this end, this section will focus on the impact of multiantenna beamforming on radio transmission.

A. MIMO Channel Model

Without losing generality, here we consider the uniform linear arrays (ULAs) used at the transmitter and receiver sides. The antenna arrays are positioned in the same coordinate system as shown in Fig. 1. The first element is positioned at the origin, and the array direction is represented by \( \Upsilon_x = (\vartheta_x, \varphi_x) \) with \( x \in \{t, r\} \), as shown in Fig. 2. Assuming locally plane waves at the transmitter and receiver, the \( n \)th multipath wave propagation between any pair of transmitting and receiving elements can be modeled to have experienced the same amplitude attenuation but different phases due to path length differences.

For the antenna arrays composed of \( P \) antenna elements and \( Q \) antenna elements at the TX and RX sides, respectively, the multipath multiply-input–multiple-outout (MIMO) channel response matrix can be described by

\[
\mathbf{H}(\tau, \Omega_t, \Omega_r) = \sum_{n=0}^{N} \mathbf{H}_x \delta(\tau - \tau_n) \
\]

(25)

\[
\cdot \delta(\Omega_t - \Omega_{t,n}) \delta(\Omega_r - \Omega_{r,n})
\]
where

$$H_n = h_n a_r(\Omega_{x,n}, \Psi_r) a_t^H (\Omega_{x,n}, \Psi_t)$$  \hspace{1cm} (26)$$

is the channel matrix of the nth path, the superscript $H$ represents the Hermitian operation, and $a_x = a_x(\Omega_{x,n}, \Psi_x)$ is the array response vector of the direction $\Omega_{x,n}$. The array response at either the transmitter or receiver side can be expressed by

$$a(\Omega, \Psi) = [e^{j\varepsilon} \ldots e^{j(M-1)\varepsilon}]^T$$  \hspace{1cm} (27)$$

where the superscript $T$ denotes the transpose operation, the relative phase difference between elements

$$\varepsilon = \frac{2\pi d}{\lambda} (\sin \theta \sin \vartheta \cos[\phi - \varphi] + \cos \theta \cos \vartheta)$$  \hspace{1cm} (28)$$

$\lambda$ is the wavelength, $d$ is the antenna element spacing, and $M \in \{P, Q\}$ is the number of elements. Here, for convenience, the subscripts $x \in \{t, r\}$ was omitted for $a_x, \Omega_x,$ and $\Psi_x$.

B. Multiantenna Beamforming

Suppose that ULA arrays with nonisotropic elements are applied, and a narrowband beamforming is performed at the TX and RX sides. All the elements are assumed to have the same orientation, i.e., $\Psi_x$ is the same for all the elements at the TX or RX side. Therefore, the weighted output of the beamformer in the receiver is written as

$$y'(t) = \sum_{n=0}^{N} h_n \frac{A_r(\Omega_{x,n}, \Psi_r) w_r^H a_r}{\sqrt{C_r(\Omega_{x,n}, \Psi_r)}}$$

$$\cdot \frac{A_t(\Omega_{x,n}, \Psi_t) a_t^H w_t s(t - \tau_n) + w_r^T n}{\sqrt{C_t(\Omega_{x,n}, \Psi_t)}}$$  \hspace{1cm} (29)$$

where the total transmit power is equally allocated to each element, i.e., $E[|s(t)|^2] = (E_s/P)$, the weights satisfy $w_t^H w_t = P$ and $w_r^H w_r = Q$, and the elements of the noise vector $n = [n_1(t), n_2(t), \ldots, n_Q(t)]^T$ in the receiver are independently and identically distributed AWGN with variance $N_0$. The phase information of $w_r^T a_r$ and $a_t^H w_t$ has been included in the channel impulse response $h_n$, which will not affect the following derivations. The synthesized power pattern $C$ is merely the product of the antenna pattern $A$ and the array pattern $B$, i.e.,

$$C(\Omega, \Psi, \Psi_t) = A(\Omega, \Psi) B(\Omega, \Psi_t)$$  \hspace{1cm} (30)$$

where the array pattern is written as

$$B(\Omega, \Psi) = |a_t^H w_r|^2.$$  \hspace{1cm} (31)$$

Notice that the signal model (29) is exactly the same as the model (1) of the single-antenna case by replacing the antenna pattern $A$ by the synthesized pattern $C$. Therefore, the joint impact of the element pattern and the multiantenna beamforming on the channel can be analyzed by the same approach as in Section II-B. Keep in mind that the computation of impact factors here is always relative to the case of the single-input–single-output channel configured with isotropic antennas. Particularly, the $K$-factor gain $G_K$ and the RDS reduction $G_B$, may be obtained by simply replacing the antenna pattern $A_x(\Omega_{x,n}, \Psi_x)$ by the synthesized pattern $C_x(\Omega_{x,n}, \Psi_x, \Psi_r, \Psi_t)$ into (22) and (24), respectively. However, the expression of the SNR gain here is somewhat different. Bearing in mind that the transmit power in each element is $1/P$ times the total transmit power and that the total receiver noise is $Q$ times the noise power at each element, the SNR gain $G_\rho = (\rho'/\rho)$ is calculated as

$$G_\rho = \frac{\frac{E_x}{P_0} \cdot \left( \frac{K}{K+1} C_t(\Omega_{t,0}, \Psi_t, \Psi_r) C_r(\Omega_{r,0}, \Psi_r, \Psi_t) + \frac{1}{K+1} E_C \right)}{Q N_0 \cdot \rho}$$

$$= \frac{\beta E_C}{PQ}$$  \hspace{1cm} (32)$$

where $\rho = (E_2/N_0)$, and $\beta = (KG_B + 1)/(K + 1)$. The Rician $K$-factor gain is given by

$$G_K = \frac{C_t(\Omega_{t,0}, \Psi_t, \Psi_r) C_r(\Omega_{r,0}, \Psi_r, \Psi_t)}{E_C}$$  \hspace{1cm} (33)$$

and the power gain of the scattered waves $E_C$ is given by

$$E_C = (K + 1) \iint P_S(\Omega_t, \Omega_r) C_t(\Omega_t, \Psi_t, \Psi_r) C_r(\Omega_r, \Psi_r, \Psi_t) d\Omega_t d\Omega_r$$  \hspace{1cm} (34)$$

for the synthesized pattern. Note that the results in Section II-B for single TX and RX elements are merely a special case in this section.

IV. ASSUMPTIONS ON CHANNEL AND ANTENNA

As shown in Section II, by knowing the power distributions of radio waves in the time and angular domains, the impact of directional antennas and multiantenna beamformers on the channel can be analyzed. When isotropic antennas are used, the power distributions of radio waves will be very dependent on the propagation environment. Many researchers have conducted channel measurements to study the joint delay–angular spectra in certain environments [21]–[25]. The measured delay–angular spectra can be applied to study the impact of antennas on channels. Moreover, statistical models for the joint channel power spectrum $P(\tau, \Omega_t, \Omega_r)$ can be applied as an input to study the impact of antennas and beamformers. However, it is arduous to find a general form or an explicit function for describing the joint multidimensional information of radio channels. In this regard, the integration in (16) is not a trivial task for the purpose of analytical formulation. To solve this limitation, a general approach is to assume that the joint power delay–angular spectrum can be decomposed into separate spectra in the time and angular domains [22], [23]. Based on the decomposition, the integration in (16) could be relaxed, as shown in Section V, since statistical models for separate delay spectra and angular spectra have been widely studied and are available in the literature.
A. Separability of Joint Spectrum in a Single Cluster Model

Assuming that the joint power spectrum $P_S(\tau, \Omega_t, \Omega_r)$ of the scattered waves is densely distributed in delay and angles, and that the joint spectrum is proportional to the angular spectrum at a specific time delay and proportional to the delay spectrum at a specific direction [22], i.e.,

$$P_S(\tau, \Omega_t, \Omega_r)|_{\tau} \propto P_S(\Omega_t, \Omega_r)P_S(\tau, \Omega_t, \Omega_r)|_{\Omega_t, \Omega_r} \propto P_S(\tau)$$  \hspace{1cm} (35)

then the spectrum can be decomposed as the product of delay spectrum and angular spectrum as

Decomposition 1: $P_S(\tau, \Omega_t, \Omega_r) = c_1 P_S(\tau)P_S(\Omega_t, \Omega_r)$  

(36)

where the constant $c_1 = K + 1$ can be determined from (6)–(12). The decomposition has been experimentally validated for typical outdoor urban channel environments in [22]. In indoor environments, scattered waves become even denser in the angular region of antennas and beamformer on channels can be analytically treated. In addition, it is reasonable to assume that the angular spectra of the DOD and DOA, and thus, the decomposition could be valid.

Taking the separate spectra into (33), (32), and (24), the impact of the DOD and DOA, respectively, then the decomposition could be valid.

Decomposition 2: $P_S(\Omega_t, \Omega_r) = c_2 P_S(\Omega_t)P_S(\Omega_r)$  

(37)

where the constant $c_2 = K + 1$. Combining (36) and (37) leads to the decomposition

$$P_S(\tau, \Omega_t, \Omega_r) = (K+1)^2 P_S(\tau)P_S(\Omega_t)P_S(\Omega_r).$$  \hspace{1cm} (38)

With the decomposition in (38), the delay spectrum of scattered waves in (16) becomes

$$P'_S(\tau) = F_{t,C} F_{r,C} P_S(\tau)$$  \hspace{1cm} (39)

due to the synthesized pattern (30). Here, the total gain of scattered waves $E_C = F_{t,C} F_{r,C}$ is the product of the gains separately contributed by the synthesized patterns at the TX and RX sides, where

$$F_{x,C} = (K+1) \int P_S(\Omega_x)C_x(\Omega_x, \Psi_x, \Upsilon_x)d\Omega_x.$$  \hspace{1cm} (40)

Taking the separate spectra into (33), (32), and (24), the impact of antennas and beamformer on channels can be analytically obtained.

B. Power Distribution in Angular Domain

If the scattered waves are densely and uniformly distributed in the angular region

$$U_x = (\theta_x \in [\theta_x^l, \theta_x^H], \phi_x \in [\phi_x^l, \phi_x^H])$$  \hspace{1cm} (41)

with $x \in \{t, r\}$ for the DOD and DOA, respectively, then the angular spectra of the scattered waves can be expressed by

$$P_S(\Omega_x) = \begin{cases} \frac{1}{(K+1)(\phi_x^H - \phi_x^l)(\cos \theta_x^H - \cos \theta_x^l)}, & \Omega_x \in U_x \\ 0, & \text{others} \end{cases}$$  \hspace{1cm} (42)

Now, the gain of the scattered waves becomes

$$F_{x,C} = \frac{\oint_U C_x(\Omega_x, \Psi_x, \Upsilon_x)d\Omega_x}{(\phi_x^H - \phi_x^l)(\cos \theta_x^H - \cos \theta_x^l)}$$  \hspace{1cm} (43)

which is a constant for the waves distributed in a certain region. In the following, two special cases are presented for uniform angular distribution.

1) Uniform Angular Distribution in a Sphere: The channel power of the scattered waves is uniformly distributed in a sphere for DOD and DOA, i.e., $U_x = (\theta_x \in [0, \pi], \phi_x \in [-\pi, \pi])$. Then, the gain of the scattered waves caused by the synthesized pattern (30) becomes

$$F_{x,C} = \frac{1}{4\pi} \int C_x(\Omega_x, \Psi_x, \Upsilon_x)d\Omega_x.$$  \hspace{1cm} (44)

In particular, the gain caused by an antenna pattern is $F_{x,A} = 1$, which is independent of the orientation and type of antenna, since the antenna pattern always satisfies $A(x, \Omega_x) = 0$.

2) Uniform Angular Distribution in the Azimuth Plane: The power of the scattered waves is uniformly distributed in the azimuth plane, i.e., $U_x = (\theta_x \mapsto (\pi/2), \phi_x \in [-\pi, \pi])$. The gain of the scattered waves caused by the synthesized pattern (30) can be obtained by

$$F_{x,C} = \lim_{\phi_x^l, \phi_x^H \to \pi} \frac{\int_{-\pi}^{\pi} C_x(\phi_x, \psi_x, \varphi_x) \sin(\theta_x)d\theta_xd\phi_x}{2\pi (\cos \theta_x^H - \cos \theta_x^l)}$$  \hspace{1cm} (45)

where $C_x(\phi_x, \psi_x, \varphi_x)$ is the pattern in the azimuth plane. In particular, for a cosine-shaped antenna power pattern $A$ that will be introduced in (48), the gain is equal to

$$F_{x,A} = \frac{1}{2\pi} \int_{-\pi}^{\pi} 2(2q + 1) \cos^{2q} \phi_x d\phi_x = \frac{\Gamma\left[\frac{1}{2} + q\right]}{\sqrt{\pi}\Gamma[1 + q]}$$  \hspace{1cm} (46)

in case the main lobe direction is in the azimuth plane, where $\Gamma[\cdot]$ is the Gamma function.

C. Shape of Delay Spectrum

It can be seen from (24) that the reduction of RDS that is caused by nonisotropic antennas depends on the first and second moments of the power delay spectra before and after introducing nonisotropic antennas. Under the decomposition of (38), the delay spectrum shape of the scattered waves will not be changed by the use of nonisotropic antennas. Therefore, if the spectrum shape is known, the reduction of RDS can be readily obtained.
computed. For an exponentially decaying shape, the PDS can be expressed by

\[
P(\tau) = \begin{cases} 
0, & \tau < 0 \\
\frac{K}{K+1} \delta(\tau), & \tau = 0 \\
P_s(\tau), & \tau > 0 
\end{cases} \tag{47}
\]

where \(P_s(\tau) = \gamma e^{-\gamma \tau}/(K + 1)\) is the PDS of scattered waves, and \(\gamma\) is the decay exponent.

D. Power Patterns of Antenna and Beamformer

The antenna power pattern is a 3-D representation of the power radiation properties of an antenna and is generally described by a complicated function depending on the type of antenna [26], [27]. Directivity and half-power beamwidth (HPBW) are two of the most important parameters to describe an antenna pattern. Here, we introduce the cosine-shaped power pattern of antenna elements that will be used in Section V. Throughout this paper, the applied antennas are considered to be single polarized.

1) Cosine-Shaped Antenna Pattern: For a cosine-shaped antenna pattern positioned in the spherical coordinate system (see Fig. 1) with the main lobe direction aligned with the \(X\)-axis, i.e., \(\Psi = ((\pi/2), 0)\), the 3-D power pattern is expressed by

\[
A(\theta, \phi) = 2(2q + 1)(\sin \theta \cos \phi)^{2q} \tag{48}
\]

with \(\theta \in [0, \pi]\) and \(\phi \in [-\pi/2, \pi/2]\). The parameter \(q \geq 0\) is used to adjust the pattern shape and can be related to the HPBW of the pattern. For such an antenna pattern, the HPBWs on the principal azimuth and elevation planes are the same and are expressed by

\[
\sigma_A = 2 \arccos 2^{-\frac{1}{2q}}. \tag{49}
\]

The cosine-shaped pattern has no sidelobes but is a good approximation of the power patterns for many types of elementary antennas, such as horn, patch, and dipole antennas [27].

2) Beam Pattern of Conventional Beamformer: In Section III-B, a general approach has been described for the multiantenna beamforming of ULA arrays. For a conventional beamformer applied in the multipath MIMO channel (25), the main beams at the TX and RX sides are steered to the direction of the direct path by adjusting the phase of the weight at each antenna element. Particularly, the weight equals the conjugate of the direct path by adjusting the phase of the weight at each element. In addition, the beamwidth of the synthesized pattern \(\sigma_C\) depends not only on the antenna pattern but also on the array pattern that is related to the number of elements and the positioning of the array. In practice, to have a sufficient radio coverage, the antenna pattern generally has a much wider beam than the array pattern, and in this case, the beamwidth of the synthesized pattern can be approximated by \(\sigma_C \approx \sigma_B\) [28], where \(\sigma_B\) denotes the HPBW of the array pattern \(B\).

V. IMPACT ANALYSIS AND ILLUSTRATIVE EXAMPLES

Directivity and beamwidth are two important parameters to characterize a directional antenna and have a significant effect on the channel. Therefore, it is interesting to quantitatively relate the antenna pattern parameters with their impact on the channel. Based on the channel and antenna models in the previous section, the impact of single-antenna and multiantenna beamformers on the channels is analytically formulated and illustrated by examples in this section.

A. Impact Analysis on the Channel

Suppose that the joint channel spectrum is decomposable as in (38), and the angular spectra are uniformly distributed either in a sphere or in the azimuth plane. Consider the conventional beamforming of a ULA array with the orientation \(\Upsilon = (\upsilon, (\pi/2))\). Applying the synthesized pattern \(C(\theta, \phi, \upsilon)\) in (50) to (33), (32), and (24), respectively, results in the \(K\)-factor gain, SNR gain, and RDS reduction of the channel due to the conventional beamforming, i.e.,

\[
G_K = \frac{P^2 Q^2 A(\theta_t, \phi_t, \upsilon_t) A(\theta_r, \phi_r, \upsilon_r)}{F_{t,c} F_{r,c}} \tag{53}
\]

\[
G_\rho = \frac{\beta F_{t,c} F_{r,c}}{PQ} \tag{54}
\]

\[
R_{\sigma_r} = 1 - \frac{1}{\beta} \sqrt{\frac{\beta \eta - 1}{\eta - 1}}. \tag{55}
\]
Here
\[ F_{x,C} = \frac{1}{4\pi} \int_{-\pi}^{\pi} \int_{0}^{\pi} C_x(\theta, \phi, \vartheta) \sin \theta d\theta d\phi \] (56)
or
\[ F_{x,C} = \frac{1}{2\pi} \int_{-\pi}^{\pi} C_x \left( \frac{\pi}{2}, \phi, \vartheta \right) d\phi \] (57)
are the gains of scattered waves distributed in a sphere or in the azimuth plane, respectively. The parameter
\[ \eta = \frac{\tau_2}{\tau_2^2} \] (58)
is the ratio between the second moment and the squared first moment of the PDS for channels with isotropic antennas. For the exponentially decaying delay spectrum in (47), the ratio \( \eta = 2(K + 1) \).

B. Illustrative Examples

Given the Rician channel \( K \)-factor, the antenna pattern, and the number of elements, in the following, the statistical change of \( K \)-factors, SNR delay spread, and RDS in the receiver will be predicted by using (53)–(55) for the exponential decaying PDS.

1) Impact of a Single Directional Element: Consider a scenario where an isotropic antenna is applied at the transmitter side and a directional antenna is applied at the receiver side. The \( K \)-factor gain, the SNR gain, and the reduction of RDS are predicted and plotted in Fig. 3 versus the RX beamwidths. Here, the thick and thin lines are the results for the uniform waves distributed in a sphere or in the azimuth plane, respectively. From these figures, we have the following observations.

- When the arrival direction of the LOS path is perfectly aligned with the main lobe direction at \( \Omega_{t,0} = (90^\circ, 0^\circ) \) (solid lines), the impact factors decrease with the HPBW, which means that it is preferable to have the HPBW as small as possible. In addition, the SNR gain and the reduction of RDS are more significant for channels with a larger Rician \( K \)-factor.

- However, when the main lobe is misaligned with the LOS path (dash lines), e.g., \( \Omega_{t,0} = (90^\circ, 10^\circ) \), the received power can significantly drop, and for a narrow beam antenna, the power is mainly contributed by scattered waves. As a result, the \( K \)-factor gain and the RDS reduction can only be effectively achieved when the HPBW of the antenna beam is sufficiently large. It is also noticed from Fig. 3(b) that if the waves are concentrated in the azimuth plane (thin lines), the drop of the SNR gain caused by the misalignment does not go deeper as the beamwidth narrows because the directivity is so large that the gained power from the scattered waves exceeds the power from the LOS wave.

- For the scattered waves distributed in a sphere, the \( K \)-factor gain and the RDS reduction are larger than those in the azimuth plane, whereas the SNR gain is slightly

![Fig. 3. With an isotropic antenna at the TX side. (a) the \( K \)-factor gain, (b) the SNR gain, and (c) the reduction of RDS, over the RX antenna beamwidth. The arriving directions of the LOS path considered here are \( \phi_0 = 0^\circ \) and \( 10^\circ \).](image-url)
lower. However, as $K > 1$, the SNR gain becomes less sensitive to wave distribution. The impact difference is due to the fact that the waves distributed in a sphere are suppressed in a larger extent than those in the azimuth plane.

Theoretically, the largest $K$-factor gain and RDS reduction can be achieved at a certain beamwidth for the misalignment $\phi_0 \neq 0$ between the main lobe and the LOS path. By computing $(\partial G_K/\partial \sigma_A) = 0$ and $(\partial R_{\sigma_A}/\partial \sigma_A) = 0$, the optimum HPBW for a small misalignment $\phi_0$ can be approximated by

$$\sigma_A^{[\text{opt}]} \approx 1.67\phi_0$$  \hspace{1cm} (59)

$$\sigma_A^{[\text{opt}]} \approx 2.35\phi_0$$  \hspace{1cm} (60)

for the scattered waves in a sphere and in the azimuth plane, respectively (see Appendix A). As for the SNR gain, the optimum SNR gain $G_\rho$ is achieved at $\sigma_A \approx 1.67\phi_0$ for the case of scattered waves in a sphere, whereas for the case in the azimuth plane, the gain $G_\rho$ is not a strictly convex function.

2) Impact of Conventional Beamforming: When designing a multiantenna beamforming system, the requirements with regard to radio coverage and SNR gain are important issues to take into account. The radio coverage is related to the individual antenna pattern beamwidth, and the SNR gain depends not only on the directivity of elements but also on the array configuration, e.g., the number of elements. The impact factors in (53)–(55) can be taken as the criteria for selecting the antenna pattern and the number of elements.

By way of illustration, we consider a TX–RX beamforming with isotropic elements at the TX side and directional elements at the RX side. The numbers of elements are $(P, Q) = (1, 1), (2, 2), (3, 3), (4, 4), (5, 5), \text{ and } (6, 6)$; the TX and RX arrays are positioned in the direction at $\Upsilon_x = (90^\circ, 90^\circ)$; and the LOS wave at the TX side is always in the direction of $\Omega_{t,0} = (90^\circ, 0^\circ)$. Fig. 4 depicts the $K$-factor gain, SNR gain, and RDS reduction versus the RX antenna beamwidth for the two cases of $\Omega_{r,0} = (90^\circ, 0^\circ)$ and $(90^\circ, 10^\circ)$, respectively. The Rician channel with $K = 1$ is considered for the computation of SNR gain and RDS reduction. In addition, to show the scanning range of the array, Fig. 5 depicts the impact factors over the scanning angle $\phi_{r,0} \in [-90^\circ, 90^\circ]$ for the RX element beamwidth $\sigma_A = 95^\circ$.

For a specific design requirement, the number of elements and antenna beamwidth can be determined, and the statistical impact of this configuration on the channel can be checked from these figures. For instance, the link budget requirement of 20-dB gain in the channel with $K = 1$ can be satisfied by using an antenna array with $(P, Q) = (6, 6)$ with the RX element beamwidth $\sigma_A = 95^\circ$ [see Fig. 4(b)]. This configuration leads to a 3-dB scan range that is about the same as the RX element beamwidth [see Fig. 5(b)]. This observation confirms the analysis in Appendix B that a 3-dB azimuth scan range can be approximated by the element beamwidth

$$\phi_{\text{scan}} \approx \sigma_A$$  \hspace{1cm} (61)

for a fairly large $K$-factor and a large number of elements. It is further observed that within the 3-dB scan range, the $K$-factor gain is about 22.5 dB, and the reduction of RDS is about 87.5%.

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![Fig. 4. For isotropic and directional antenna elements at the TX and RX sides, (a) the $K$-factor gain, (b) the SNR gain, and (c) the RDS reduction caused by conventional beamforming over the RX element beamwidth for various (TX, RX) = $(P, Q)$ configurations.](image-url)
C. Discussion

The impact of the radiation pattern on the considered channels is predicted here without taking into account some practical issues, such as antenna cross polarizations and sidelobes. When both the vertical- and horizontal-polarized field components exist in the wave transmission, a similar approach as in Section II can be used to predict the impact of antennas on the channel, but the antenna gain patterns and the channel power spectra have to be separately considered [15], [29]. The existence of sidelobes in the antenna pattern will lead to a reduced directivity, and as a result, the Rician $K$-factor gain and the RDS reduction become less effective.

It is shown in Section IV that the assumption about a decomposable channel spectrum leads to an easier analysis in this section. For further study, it is interesting to model the joint distribution of channel power in time delay and angular domain, as conducted in [30] for urban environments, and to investigate the decomposability of realistic channels. In addition, in practical propagation channels, the scattered waves are often cluster-wise distributed in time and space, and the departing and arriving directions are typically not uniformly distributed. It is yet not known how much the impact on realistic channels is different from those obtained in this section and which one of the assumptions about the exponentially decaying PDS and uniform PAS will give the most significant effect on the differences. This analysis needs to be conducted in the future.

VI. Conclusion

In this paper, the impact of directional antennas and multi-antenna beamformers on radio transmission has been analytically formulated for multipath Rician channel environments. By way of illustration, a hypothetical antenna with the cosine-shaped power pattern was applied to show the impact on the channel with an exponential PDS and uniform power angle spectra. It was found, for instance, that in the case of misalignment between the antenna main lobe and the LOS wave, the optimal HPBW of the antenna is equal to about twice the misaligned angle. By using a directional antenna at one side of the radio link, the Rician $K$-factor and the SNR gain can range up to 16 dB, and the RDS reduction may be more than 80%. If multipath beamformers are used at both sides of the radio link, the Rician $K$-factor gain, SNR gain, and RDS reduction will be even higher. Further, it was found that for conventional beamforming, the 3-dB scan range can be approximated by the antenna element HPBW.

APPENDIX A

APPROXIMATION OF THE OPTIMUM HPBW FOR MAIN LOBE MISALIGNMENT

A. Uniform PAS in the Azimuth Plane

Suppose that the scattered waves are uniformly distributed in the azimuth plane. In the case of the misalignment between the LOS path and the main lobe direction, the optimum HPBW
concerning the largest $K$-factor and RDS reduction can be achieved by solving
\[
\psi \left[ \frac{1}{2} + q \right] - \psi [1 + q] = \ln \cos^2 \phi \tag{62}
\]
which is obtained by computing \((\partial G_K / \partial \phi_A) = 0\) and \((\partial R_{\phi_0} / \partial \phi_A) = 0\). Here, \(\psi[z] \) is the Digamma function [31]. Although the closed-form solution cannot be carried out, a simple relationship between the optimum HPBW and the misalignment \(\phi_0\) can be found for a small misalignment in an approximate way.

Since the first-order derivative of the Digamma function \(\psi[q] (q \geq 0)\) is a decreasing function and goes to 0 in the infinity, the limit
\[
\lim_{q \to +\infty} \left( \psi \left[ \frac{1}{2} + q \right] - \psi [1 + q] \right) = \lim_{q \to +\infty} \left( \psi [q] - \psi \left[ \frac{1}{2} + q \right] \right) = 0 \tag{63}
\]
is valid. It can be seen that if the misalignment \(|\phi_0| \to 0\), the parameter \(q\) must be \(q \to +\infty\) for the equality in (62) to be valid. Next, according to the property of the Digamma function \(\psi[z + 1] = \psi[z] + (1/z)\), we have
\[
\left( \psi \left[ \frac{1}{2} + q \right] - \psi [1 + q] \right) = - \left( \psi [q] - \psi \left[ \frac{1}{2} + q \right] \right) - \frac{1}{q}. \tag{64}
\]
Using (63), the relationship in (64) can be approximated by
\[
\psi \left[ \frac{1}{2} + q \right] - \psi [1 + q] \approx - \frac{1}{2q} \tag{65}
\]
for a sufficiently large value of \(q\). Combining the relationships (49), (62), and (65), the following approximation is achieved:
\[
\cos \frac{\sigma_{A[\text{opt}]}^{\phi_0}}{2} \approx \cos \phi_0^{2 \ln 2}. \tag{66}
\]

Last, using \(\cos^n \phi_0 \sim (1 - (n \phi_0^2/2))\) for \(|\phi_0| \to 0\), the optimum HPBW is related to a small misalignment \(\phi_0\) by the following approximation:
\[
\sigma_{A[\text{opt}]} \approx 2\sqrt{2 \ln 2} \phi_0 \approx 2.35 \phi_0. \tag{67}
\]

Fig. 6 depicts the theoretical relationship (62) and its approximate (67) between the optimum HPBW and the misalignment \(\phi_0\), respectively, which indicates that (67) is a fairly good approximation in a large misalignment range.

### B. Uniform PAS in a Sphere

If the scattered waves are uniformly distributed in a sphere, the optimum HPBW concerning the largest $K$-factor and RDS reduction can be achieved by solving
\[
\ln \cos \frac{\sigma_{A[\text{opt}]}^{\phi_0}}{2} = \ln \cos^{\ln 2} \phi_0 + \ln \cos \phi_0 \tag{68}
\]
which is obtained by computing \((\partial G_K / \partial \phi_A) = 0\), \((\partial G_{\phi_0} / \partial \phi_A) = 0\), and \((\partial R_{\phi_0} / \partial \phi_A) = 0\). Using \(\ln \cos \phi_0 \sim - (\phi_0^2/2)\) for \(|\phi_0| \to 0\), we have
\[
\sigma_{A[\text{opt}]} \approx 2\sqrt{2 \ln 2} \phi_0 \approx 2\sqrt{2 \ln 2} \phi_0 \approx 1.67 \phi_0. \tag{69}
\]

Fig. 6 depicts the theoretical relationship [see (68)] and its approximate [see (69)] between the HPBW and the misalignment \(\phi_0\), respectively, which indicates that (69) is a fairly good approximation in a large misalignment range.

### APPENDIX B

#### AZIMUTH SCAN RANGE AND ELEMENT BEAMWIDTH

Here, we only investigate the relationship between the 3-dB beam scan range in the azimuth plane and the antenna element beamwidth at the receiver side. The following results are also true for the scan range at the transmitter side. If the departure direction of the LOS wave is fixed at \(\Omega_{r,0}\), then from (53) and (54), the maximum gains of the $K$-factor and SNR, respectively, can be achieved as
\[
\max \{G_K\} = \frac{P^2 Q^2 A(\Omega_{t,0}) A(\tilde{\tau}, 0)}{F_{t,C} F_{r,C}}. \tag{70}
\]
\[
\max \{G_{\rho}\} = \frac{(K \cdot \max \{G_K\} + 1) F_{t,C} F_{r,C}}{P Q (K + 1)} \tag{71}
\]
when the LOS wave arrives in the receiver at \(\Omega_{r,0} = ((\pi/2), 0)\). Now, the 3-dB scan range in the azimuth plane can be derived as
\[
\phi_{\text{scan}} = |\phi_{r,0}^U - \phi_{r,0}^L| \tag{72}
\]
where \(\phi_{r,0}^U\) and \(\phi_{r,0}^L\) are the solutions to \(G_{\rho} = (1/2) \max \{G_{\rho}\}\) that is simplified as
\[
\frac{A(\tilde{\tau}, \phi_{r,0}) - A(\tilde{\tau}, \phi_{r,0})}{A(\tilde{\tau}, 0)} = \frac{1}{2} - X \tag{73}
\]
where \( X = 1/(2K \max \{G_K \}) \). It can be seen in (73) that the azimuth scan range is never larger than the element HPBW because of
\[
\frac{\pi/2}{\phi_{\max}} = \frac{1}{1/2} = \frac{\pi/2}{\phi_{\min}} = \frac{1}{1/2}.
\]

Fig. 4(a) shows that for a fairly large number of antenna elements, a large \( K \)-factor gain can be achieved, which leads to \( X \ll (1/2) \) for a fairly large \( K \)-factor. In this case, the azimuth scan range is approximated by the element beamwidth, i.e.,
\[
\phi_{\text{scan}} \approx \sigma_A. \quad (74)
\]

ACKNOWLEDGMENT

The authors would like to thank all the anonymous reviewers for their valuable comments.

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