

MASTER

Formal comparison of separation kernel models GWV separation versus Rushby's non interference

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TECHNISCHE UNIVERSITEIT EINDHOVEN

MASTER THESIS

**Formal Comparison Of Separation
Kernel Models: GWV Separation Versus
Rushby's Non Interference**

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for the degree of Master in Computer Science and Engineering.*

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TECHNISCHE UNIVERSITEIT EINDHOVEN

Abstract

Department of Mathematics and Computer Science

Master in Computer Science and Engineering.

Formal Comparison Of Separation Kernel Models: GWV Separation Versus Rushby's Non Interference

by Adrian GARCIA RAMIREZ

In this document we investigate how formal verification methods can be used to compare and classify separation kernel architectures.

The separation kernels are an integral part of the Multiple Independent Levels of Security (MILS) design pattern. Consisting of relatively small components that run directly over the hardware and whose main task is to create separation or isolation between the different processes running within the host device.

The two main formal models of separation kernels are the one proposed by Greves, Wilding and Vanfleet (GWV) and the one proposed by John Rushby.

In the first part of this dissertation we formalize the original version of the GWV and Rushby models in the Isabelle/HOL theorem prover. Moreover, we present that to our knowledge is the first formal comparison of the aforementioned models.

In the second part, we propose a mapping between the elements conforming both models, and later we use this mapping to compare the security definitions presented in them.

Finally In the last part we present two examples that illustrate the main differences between the Rushby Non Interference and GWV separation models.

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Abbreviations

CC	Common Criteria
EAL	Evaluation Assurance Levels
GWV	Greve Wilding Vanfleet separation model
MILS	Multiple Independent Levels of Security
MLS	Multiple Levels of Security
NSA	National Security of Agency (from the United States of America)
NSA	National Institute of Standards and Technology
SKPP	Separation Kernel Protection Profile

A mis padres que me han dado el tesoro más valioso que se puede dar a un hijo, amor. Para ellos que no escatimado ningún esfuerzo y han sacrificado gran parte de su vida por sus hijos.

A mi esposa Claudia que ha compartido mis alegrías y preocupaciones, por animarme a superarme todos los días, por su apoyo incondicional y ayuda. En Claudia he encontrado la fuerza necesaria para llegar hasta el final.

Esta tesis está dedicada a ellos.

Chapter 1

Context

There are several security models proposals born hand in hand with the military security classification model [1]. Multiple Levels of Security Models (MLS), correspond to multiple mandatory access control policies[2], in which the data are classified into security levels.

In MLS systems the access to a resource is granted according to the authorization level of the subject trying to access it. The MLS approach has also been called data flow model, because it allows to control the flow of data between different security levels. The MLS best known models are the Bell-La Padula [3] and Biba [4] models.

Multiple Independent Levels of Security (MILS) is an architectural design pattern capable of implementing multi-level security in a simple and adequate manner. The objective of MILS is to ensure the security for high reliability or mission-critical systems.

Figure 1.1 exemplifies the MILS architecture pattern. The main MILS security mechanism, is the separation kernel [5]. The idea behind security kernels consists in isolating all processes and make them appear independent, as if they run on different machines, so they cannot interfere with each other. Interaction between different security levels is only allowed through channels previously defined.

More background information about MILS and separation kernels can be found in the next Chapter.

Motivation and Contribution

Motivation

Separation kernel is a key element to achieve multiple-level security in MILS systems.

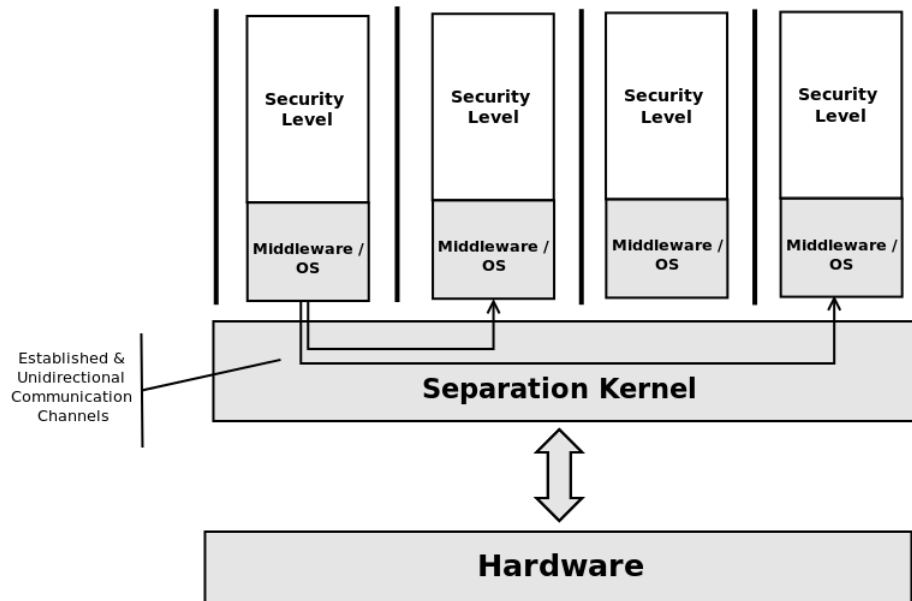


FIGURE 1.1: MILS Architecture Diagram

Formal verification is a fundamental process to ensure the correctness of systems such as separation kernels. However, there is no guideline on how to select the most appropriate separation kernel model.

The two main formal separation kernels models are the GWV model proposed by Greve, Wilding and Vanfleet [6], and the model proposed by John Rushby [7].

The GWV model contains a separation property that can be used to represent the isolation between the separation kernel partitions. Whereas, the Rushby model provides the basis to satisfy a non-interference security policy.

The differences between GWV and Rushby separation kernel models have previously been informally discussed [8]. However, a formal comparison of the concepts in both models has never been performed.

The lack of a formal comparison between the GWV and Rushby models makes it impossible to determine with certainty which of the two proposed security definitions is stronger and what is the exact relationship between the different elements and definitions of both models.

In the present document we do not only formalize the security definition of the GWV and Rushby models, but we also compare the security properties offered by them against each other.

Research Question

The objective of this thesis is to use formal methods to determine the differences between GWV and Rushby's models and to classify these models in terms of their strength and

features offered. A model is stronger if it accepts less systems as “secure”. A secondary goal is to determine under which conditions a system would be considered secure under both security definitions. Therefore, the main research question to be answered in this thesis is:

Research Question: *“What are the exact differences and similarities between the GWV separation Model and the non-interference model proposed by Rushby?”.*

To reach this objective, the following sub research questions need to be answered:

- How can we map the concepts of the two models?
- What conditions does the GWV model need to be considered secure under Rushby non-interference definition?
- Which Rushby conditions can be derived from the GWV security definition?
- Can Rushby model ensure security under the GWV definition?
- Is possible to find counterexamples to show the differences of the two models?

Our approach method to answer these questions is to construct a formal proof relating the GWV and Rushby models.

Contribution

The primary contributions of this dissertation can be summarized as follows:

In Chapters 3 and 4, we formalize the original GWV and Rushby Models and reproduce the proofs of the original models in the Isabelle/HOL theorem prover.

Our first four sub-research questions are covered in Chapter 5. In this chapter we provide a mapping between the main elements and functions of both models and we use them to formalize Rushby’s reference monitor conditions using the GWV concepts and elements. Later, we prove the relation between Rushby’s transitive and intransitive models and GWV.

Our main contribution is pictured in Figure 1.2. This picture illustrates the relation between the different GWV and Rushby elements, line in the figure indicate a relation between definitions, whereas the numbers indicate the Section where the proof of such relation can be found.

As we can see GWV separation definition and one extra condition named “*GWVcond1*” implies Rushby’s step consistency definition. Whereas, step consistency implies GWV security (we assume that the action executed in the active partition are the same). In the

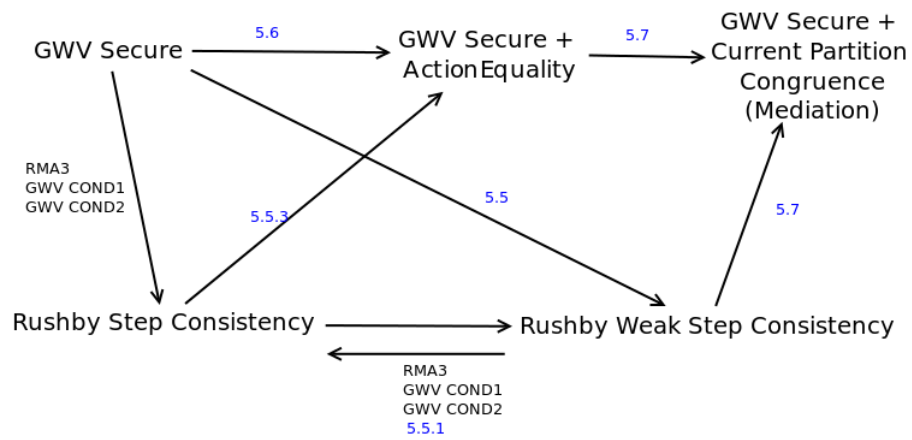


FIGURE 1.2: Relation Among the GWV and Rushby Security definitions

case of intransitive policies we show that the GWV separation definition implies weakly step consistency, while Rushby's definition can only ensure the property of *mediation* proposed in the original GWV model.

In Chapter 6 we answer the last sub-research question. In this chapter we first present an example that illustrates the need of *GWVcond1* for GWV to be considered secure in the Rushby model. Later, a second example shows that Rushby weakly step consistency cannot ensure GWV security.

Finally, in Chapter 7 the conclusions and some recommendations for further research are described.

Chapter 2

Preliminaries

2.1 Information Security Overview

Information Security is considered a key factor within organizations. However, it has many interpretations and encompasses many different concepts. In a broad context information security is responsible for providing secure and reliable conditions for data processing systems.

The goals of information security are to ensure that information systems resources are available when needed, and to guarantee that access and modification of the information contained in them is only possible within the limits defined by the organization security policies.

The objectives of information security[9] can be summarized by the following principles:

- Confidentiality: Organizations need to protect the privacy of the data stored and processed in computer systems.
- Integrity: A secure system must ensure that the data contained in them can only be modified in appropriate ways, by appropriate people, and that users can rely on the accuracy of the information contained in the system.
- Availability: This refers to continuity of access to the elements of a computer system. Based on this principle, information security must ensure that the services or information supplied by the system are available when required.

2.2 Formal Verification

Commonly, the term verification is used to name the process that aiming at ensuring that a design satisfies the properties that express correct operation of a given system. The formal and precise aspect is achieved by describing the system and its properties in a mathematical language. Verification is the process that ensures, to a certain extent, whether a system meets its desired properties [10].

Formal verification can be useful to prove the correctness of a wide range of systems such as: communication protocols, digital circuits and software. In order to verify a system we need to provide a formal proof of an abstract mathematical model of the system, and demonstrate the correspondence between the mathematical model and the system being developed.

An approach to formal verification is theorem proving[11].

Theorem proving is a technique where the system and its desired properties are expressed in mathematical logic[12]. This logic is given a set of axioms. The theorem proving is then the process of finding a proof of a property using these axioms and inference rules.

Proofs can be obtained by hand, but in recent years there has been an increasing use of theorem provers such as [ACL2](#)[13], [PVS](#)[14], [Coq](#)[15] and [Isabelle/HOL](#)[16]. Theorem provers can be used as an assistant in the proving process.

Theorem provers vary according to their degree of automation, from fully automatic to interactive provers. The latter, require interaction with a person. On the one hand, human interaction makes them more susceptible to errors. On the other hand, it increases the power of the prover thanks to the contribution that can be made by a human intelligence.

Theorem proving approach requires the user to understand in detail why the system operates properly, and transmit this information to the verification system, either in the form of a sequence of theorems to be proved or in the form of system components specifications.

2.3 Multiple Independent Levels of Security

Multiple independent levels of Security (MILS) is a security model promoted by The Air Force Research Laboratory, in cooperation with the National Security Agency (NSA), Department of Defence contractors, academia and software suppliers, with the goal of ensuring security of systems performing mission-critical functions.

Principles of NEATness

MILS is based on the concepts of separation and information flow control. The goal of this design pattern is that the security mechanisms meet the following properties, appropriately represented by the acronym NEAT [17]:

- **Non-Bypassable:** A security mechanism must be impossible to bypass. Each process by a security mechanism must be obligatorily executed.
- **Evaluatable:** It must be possible to show that the security solution was implemented properly. To comply with this principle it should be possible for the MILS designer to demonstrate that the defined security mechanisms functions properly, this can be achieved by using techniques such as code inspection or formal verification
- **Always Invoked:** Security functions are invoked on every execution of the system.
- **Tamper proof:** A security mechanism cannot be modified without authorization. This principle avoids the inclusion of mechanism that could introduce malicious mechanisms to the system.

2.4 The Role of Separation in MILS

Typically the common way to implement security into a system is to add additional elements above the operating system and applications. In contrast, the MILS approach is just the opposite. Systems become secure by simplifying the protection, and as the systems are simpler we can trust them to work properly. Simple means secure [18].

MILS places particular emphasis on the principle of least privilege formulated by Saltzser[19], which states that: *“every program and every user of the system should operate using the least set of privileges necessary to complete the job.”*

To apply the least privilege security principle the designers of MILS compliant systems are required to decompose the obligations of the system. Each obligation is later placed into separate components, in such a way that the resulting components are as simple as possible. This approach involves the advantage that each component can be evaluated and verified in a simple manner.

MILS is a layered approach where the low-level layers provide security services to the upper layers. Under this approach each layer is responsible for the security services only in their own domain.

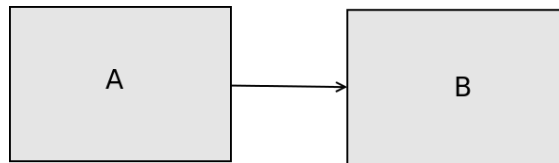


FIGURE 2.1: Simple Security Policy

Imagine for example, a simple security policy like the one shown in Figure 2.1. This policy requires that component A can only send data to B if it has been previously encrypted. Component B should not be able to transmit any data to A.

In the real world policies like this are not as easy to implement as it may seem. As Figure 2.2 shows, components of simple system like this can be very complicated. The only way to ensure that a policy like this is satisfied, is if each one of the elements in A and B have been previously assessed and verified against accidental or malicious mechanisms that can subvert the policy. Therefore we can conclude that to ensure a simple policy in a relatively simple system, is required to verify the security of operating systems, protocols and application software. The costs of such an effort can be really prohibitive.

Now imagine that instead of allowing direct communication between A and B we have a system composed of three different elements connected by specific communication paths as shown in Figure 2.3. In this case the complexity of ensuring the security of the system is simplified, since *crypto* may be a dedicated component whose correctness has been previously verified.

Taking this into consideration it can be said that one way to protect the information from corruption, misuse or unauthorized disclosure is through the separation of the system in different security domains and maintaining the control of information flows between such domains.

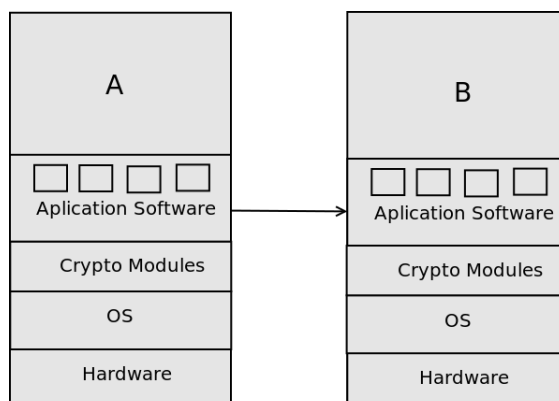


FIGURE 2.2: “Real world” Simple Security Policy



FIGURE 2.3: Simple Security Policy with Duty Separation

Separation is relatively easy to implement if there is an actual physical distance between each of the components, ie each component is really a separate physical device. However, this task is more complex if the system is deployed on a single machine and each component makes use of a single shared processor and resources. Therefore, is duty of MILS designers to establish the mechanisms required to achieve this separation.

2.5 Separation Kernels

From the security standpoint of view, the creation of various independent containers within a single device, enables the possibility of resource isolation. This separation is extremely important for systems requiring multiple levels of security (i. eg. military System) or systems that simultaneously host critical processes along with others applications that may not have been properly verified, may contain errors or even present malicious behaviour.

The idea of splitting a single system on different “virtual” machines to increase their security, was originally proposed by Madnick in 1972 [20]. Nevertheless, existing virtualization systems have not been designed with this goal in mind and cannot ensure the complete separation of the systems hosted in them [21].

Separation kernels were initially proposed by John Rushby [5] as an integral part of the Multiple Independent Levels of Security (MILS) [22] architecture pattern. This special type of security kernel consists of relatively small components that run directly over the hardware and whose main task is to create separation or isolation between the different processes running within the host device.

Jonas Frid identified [23] some attractive features of separation kernels:

Flexibility: using separation kernels it is possible to create systems that range from a few partitions to hundreds of them. Systems can easily be modified by adding more partitions.

Isolation of Security Critical Functions: Owing to the possibility of having secure separated modules, it is possible to extract the security critical functions and allocate

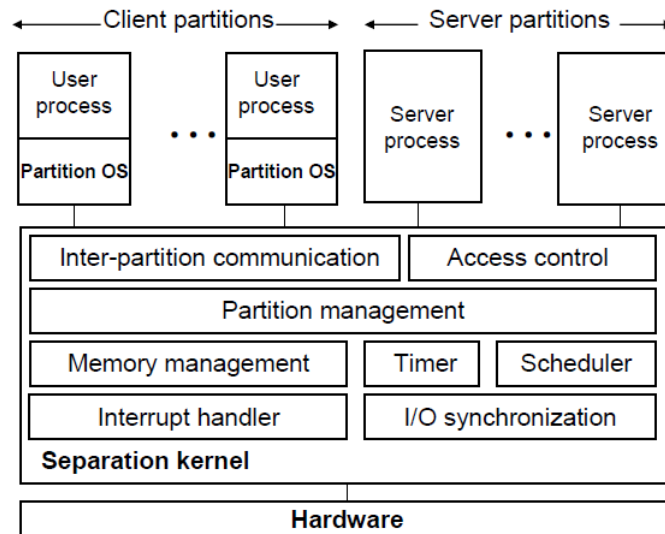


FIGURE 2.4: Architecture of separation-kernel-based system. Figure taken from [24]

them into separate partitions. In consequence security functions can be simpler and specific which leads to easier verification because the modules are smaller.

Figure 2.4 illustrates the general architecture of separation kernels. In a separation kernel, isolation is accomplished through the creation of different security partitions. A certain number of memory segments are assigned to each partition. The processes running within each partition are only allowed to read and write in the segments that correspond to their assigned partition. Meanwhile, the kernel is responsible for controlling the flow of information between the different partitions.

Kei Kawamorita et al. defined three main requirements to ensure the protection of memory in a security kernel[24] that can be listed as follows:

- The memory space of each partition must be isolated from the other partitions, in other words a process being executed in a partition should not be able to access the memory space from other partitions.
- The memory area containing the separation kernel must be only accessible by the same kernel.
- The memory space that contains the operating system of each partition should not be accessible to the user-initiated processes.

Separation kernels are in charge of providing multilevel secure operation on general-purpose systems by creating an indistinguishable environment from that provided by

a physically distributed system: to the internal processes each partitions appears as it were a separate, isolated machine.

One of the main advantages of separation kernels is that they can increase the security of the whole system by denying the ability of the processes to interfere with any resource outside their assigned security partition.

To ensure that a separation kernel provides an appropriate level of protection, and presents all its desired properties, it should be possible for the kernel developer to demonstrate that the kernel functions properly, this can be achieved by using techniques such as code inspection or formal verification.

A verifiable secure kernel improves the trustworthiness of the entire system. Separation kernels should be small enough for mathematical verification. This principle removes all superfluous functionality from the kernel, removing with it the problems of complexity and potential security flaws.

The small size and relative simplicity of separation kernels makes them obvious candidates for formal verification thus increasing the trustworthiness of the entire system.

2.5.1 Common Criteria Certification

The Common Criteria (CC) provides a standardized framework (methodology, notation and syntax) to specify and verify security functional requirements to be met by IT systems and assurance measures applied to them, in their different stages of life-cycle.

Common Criteria originated from three standards: ITSEC [25], TCSEC [26] and CTCPEC [27]. The standard ITSEC is an European standard. The TCSEC standard formerly known as the Orange book (DoD 5200.28 Std) was a work of the NSA and NBS (now NIST). The CTCPEC standard was published in Canada.

CC consists of a regulatory framework, adopted as an international standard by ISO in 1999 (ISO 15408) for the security assessment. Common Criteria certification comes in seven predefined assurance packages, which are called Evaluation Assurance Levels (EAL). Table 2.1 offers a small description of each EAL level. As EAL level increases, time, resources and technical requirements needed to achieve the certification also increase.

EAL	Description	Target
EAL 1	Product functional assay	Demonstrate proper operation of the product by independent testing, reviewing the applicability of threats not public domain.
EAL 2	Product structural test	It adds more active cooperation of the developer in terms of product delivery and test results.
EAL3	Test methodical and product validation	In addition to the above, it provides high security guarantee in the product design phase.
EAL4	Methodical design, testing and product validation	To provide a high assurance of safety practices implementation in the development and testing phase of the product. Level up and products suitable for commercial environments.
EAL5	Semi-formal design and product testing	Provides high assurance rigorous application of safety practices in the phase of product development and testing at both the developer how independent.
EAL6	Semi - formally verified design and product testing	Demonstrates proficiency in asset protection against significant threats, where the value of the assets justifies the additional costs of development.
EAL7	Formal design and product testing verified	Provides maximum protection guarantee high-value assets, based on a formal analysis of the product development and testing level.

TABLE 2.1: Description of Objectives for Each EAL.

2.5.2 Separation Kernel Protection Profile

Common criteria establishes a common language where users can specify their security needs. With this language users can specify what functionality should have the products to meet their needs. User security needs are specified in documents called Protection Profiles.

In 2007, the U.S. National Security Information Security Agency (NSA) released a Separation Kernel Protection Profile (SKPP) [28], that contains a specification of the security requirements for separation kernels. The SKPP describes the fundamental properties of separation kernels and defines the security requirements for their under Common Criteria certification.

The SKPP defines a separation kernel as:

”Hardware and/or firmware and/or software mechanisms whose primary function is to establish, isolate and separate multiple partitions and control information flow between the subjects and exported resources allocated to those partitions”.

Although the fulfilment of SKPP requirements does not imply that the evaluated kernel is immediately certified under Common Criteria, the requirements defined by the document were designed to provide an assurance level EAL 6 augmented. Among the main requirements of this protection profile we can find the obligation to present a formal model that describes the functionality of the separation kernel.

Chapter 3

Rushby's Non Interference Formalization

In this chapter we describe the notion of Security (non-Interference) for separation Kernels originally formulated by John Rushby [7]. This chapter has been divided in two sections:

In this Section we present the notion of non-interference for transitive security policies. First, we formalize the system model proposed by Rushby. Next, we discuss the notion of security (non-interference) used to evaluate the security of this model. Later, we prove that the system model proposed by Rushby complies with the notion of non interference. Finally we consider the relation between non-interference and access control formulations, and we identify the “Rushby’s reference monitor assumptions” that play a key role to ensure non-interference in access control systems.

3.1 Transitive Non-Interference

An information flow policy defines the types of information that a system can have, and how information can flow between these classes. An information flow policy can be used to express a multi-level security models.

The concept of Non-interference is a very abstract formalization aimed at solving the problem of confidentiality in computer systems. The definition of non-interference was introduced by Goguen and Meseguer in 1982 [29], and later refined by John Rushby [7]. According to the concept of non-interference. A security domain does not interfere with another if the actions executed in the first domain have no effect on what the second can see. In other words, it is as if the first security domain does not exist for the second.

3.1.1 System Model

Non-Interference security policy was defined by Rushby over a system modeled with a finite state automaton (state machine), composed by:

- States. A state contains all the values stored in the machine.
- Actions. An action can be seen as an “input” or “commands” supplied to the machine.
- Outputs. An output is the result returned by the system after feeding it with an action.

With an initial State s_0 which represents the state of the machine before the execution of any action. In Isabelle/HOL, this model is formalized as follows:

```
fixes s0 :: 'State
```

The aforementioned state machine includes functions *step* and *output*, defined as follows:

```
fixes step :: 'Action => 'State => 'State
```

```
fixes output :: 'State => 'Action => 'Output
```

Please note that from this point on, the first letters of the alphabet (a, b, \dots) are used to denote actions, the letters s, t, \dots to represent states and the letters of the Greek alphabet α, β, \dots to indicate sequences of actions.

Function $step(a, s)$ returns the state of the machine after action a has been executed in a given state s . Function $output(a, s)$ returns the output of the machine after applying the action a over the state s

We make use of an Isabelle/HOL parametrized type *'Domain* to represent these security domains.

Function *dom* returns the domain associated with the action given as a parameter.

```
fixes dom :: 'Action => 'Domain
```

Figure 3.1 shows a representation of the system model proposed by John Rushby, as we can notice, the system is divided in several domains, each action feed in the system is related with a domain

Function *run* represents a sequence of actions applied to the initial state of the machine, and is equivalent to an execution trace.

```
primrec run :: 'Action list => 'State => 'State where
```

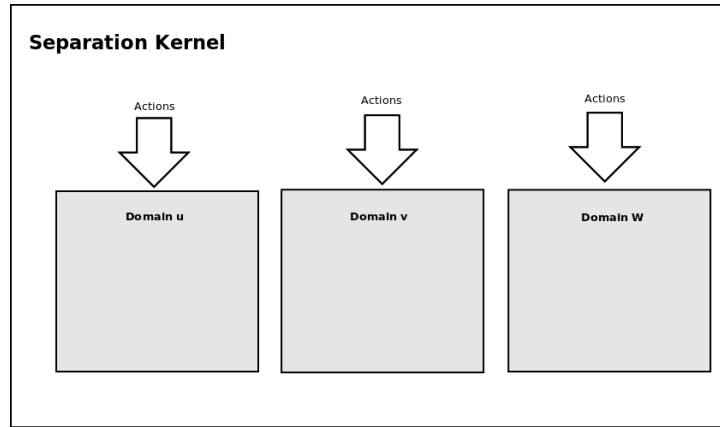


FIGURE 3.1: John Rushby's System Model

```
runEmpty  : run [] s = s|
RunActions : run (a#α) = run α ◦ step a
```

Because of the frequent use of expressions like $output(run(s0, \alpha), a)$ and $run(s0, \alpha)$, Rushby defined functions *do* and *test* as a convenient way to abbreviate these forms:

```
fun do :: 'Action list => 'State where
  do (α) = run α s0
fun test :: 'Action list => 'Action => 'Output where
  test α a = output (do α) a
```

3.1.2 Security Policy

The core component of Rushby's Security Definition is the introduction of a policy that restricts the flow of information among the different security domains.

This security policy is denoted with two reflexive relations: \rightsquigarrow called "Interference" and \rightsquigarrow^c that denotes the complement relation "Non-Interference", formally defined as:

$$\rightsquigarrow^c = (\text{Domain} \times \text{Domain}) \setminus \rightsquigarrow$$

Where \setminus denotes set difference.

These relations can be formalized in Isabelle/HOL as follows:

```
consts interference :: "'Domain => 'Domain => bool" ("( _  $\rightsquigarrow$  _)")
```

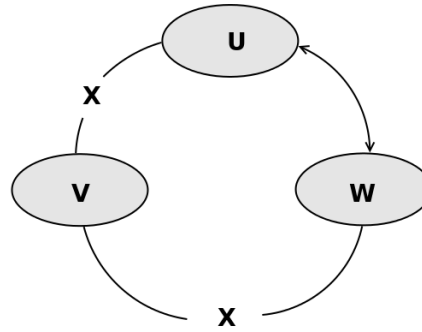


FIGURE 3.2: Information flow Security Policy.

syntax nonInterference :: "'Domain => 'Domain => bool" ("(_ \ \rightsquigarrow _)")

translations "u \ \rightsquigarrow v" \Leftrightarrow " $\neg (u \rightsquigarrow v)$ "

Intuitively two domains u and v have an “Interference” relation ($u \rightsquigarrow v$) if u is allowed to interact with v (the information can flow from one domain to the other). If information is not allowed to flow between these domains they have a “non-Interference” relation ($u \not\rightsquigarrow v$).

Using the interference (\rightsquigarrow) and non-Interference ($\not\rightsquigarrow$) relations we can model information flow policies between different security domains.

Figure 3.2 illustrates a policy that can be expressed by:

$$u \rightsquigarrow w$$

$$w \rightsquigarrow u$$

$$v \not\rightsquigarrow u$$

$$v \not\rightsquigarrow w$$

This policy allows domains u and w to interact, and restricts any interaction of these domains with domain v .

3.1.3 Purge Function

For a domain v and an action sequence α , we define function $purge(\alpha, v)$. This function returns a subsequence of α , resulting of deleting all the actions of the domains that are not allowed to interact with v . In other words, it removes all actions of domains u that have a “non-Interference” relation with v ($u \not\rightsquigarrow v$).

primrec purge :: 'Action list => 'Domain => 'Action list **where**

PurgeemptyCase: purge [] v = []

PurgeDefList: purge (a# α) v = (if (dom a) \rightsquigarrow v then a#(purge α v)

else purge α v)

3.1.4 Security Definition

John Rushby[7] defines a system as secure for the policy \sim if:

definition secure::bool **where**

$$\text{secure} \equiv (\forall \alpha \text{ a.} (\text{test } \alpha \text{ a}) = (\text{test } (\text{purge } \alpha \text{ (dom a)}) \text{ a}))$$

Under this definition, for a system to be considered as secure, no action performed in a security domain can affect the outputs of any other domain on which the interaction is not allowed.

3.1.5 Conditions to Guarantee Security

Rushby defines several conditions that individual systems have to satisfy to guarantee security.

A system is **view-partitioned** if, for each domain, there is an equivalence relation $\overset{u}{\sim}$ on the states.

consts equivalenceRelation :: "State => Domain => State => bool" ("(_ ~ _ ~ _)")

As we are defining an equivalence relation it must be transitive symmetric and reflexive. We can model these properties in Isabelle/HOL as follows:

definition eqvRelTransitive::bool **where**

$$\begin{aligned} \text{eqvRelTransitive} &\equiv \forall \text{ a b c u. } (a \sim u \sim b) \wedge (b \sim u \sim c) \\ &\longrightarrow (a \sim u \sim c) \end{aligned}$$

definition eqvRelSymmetric::bool **where**

$$\text{eqvRelSymmetric} \equiv \forall \text{ s u t. } (s \sim u \sim t) \longrightarrow (t \sim u \sim s)$$

definition eqvRelReflexive::bool **where**

$$\text{eqvRelReflexive} \equiv \forall \text{ a u. } (a \sim u \sim a)$$

The equivalence relations are said to be **output consistent** if:

definition outputConsistent ::bool **where**

$$\text{outputConsistent} \equiv (\forall \text{ s t a. } ((s \sim (\text{dom a}) \sim t) \longrightarrow \text{output s a} = \text{output t a}))$$

Informally, two states are considered output consistent for domain u if their outputs are the same for any sequence of actions α applied on domain u . This property ensures

that the outputs of two states s and t that seem equivalent to a domain u are really indistinguishable no matter what actions are performed on u .

Rushby proved [7] that given a policy \sim and a view-partitioned, output consistent system such that

$$do(\alpha) \stackrel{u}{\sim} do(purge(\alpha, u)).$$

Then such system is secure for \sim

This lemma can be proven in Isabelle/HOL as follows:

```

lemma lemma1:
  assumes 1:  $\forall u \alpha. ((do \alpha) \sim u \sim (do (purge \alpha u)))$ 
  and 2: outputConsistent
  shows 3:secure
proof -
  from assms show ?thesis
  unfolding outputConsistent-def secure-def test.simps
  by simp
qed

```

3.1.6 Security for Single Step Transitions.

Rushby also defines the conditions the single step transitions have to fulfill in order to comply with the security definition described as follows:

Let a system be a view-partitioned system and \sim a policy. We say that the system locally respects \sim if:

definition LocalRespects :: bool **where**

$$\text{LocalRespects} \equiv (\forall a u s. ((\text{dom } a) \setminus \sim u) \longrightarrow (s \sim u \sim (\text{step } a s)))$$

System M is step consistent if:

definition stepConsistent :: bool **where**

$$\text{stepConsistent} \equiv \forall a u s t. (s \sim u \sim t) \longrightarrow ((\text{step } a s) \sim u \sim (\text{step } a t))$$

“**Locally respects**” means that if an action is executed in a domain with non-Interference relation with u then domain u cannot distinguish the states before and after the execution of the action.

Finally “**step consistency**” requires that if two states are equal for a domain u and we execute the same action on both states, the outputs will still be same after the execution of the action.

After defining step consistency and locally respects rushby proves that any system that is step consistent and locally respects a policy is also secure.

Theorem 1 (Unwinding Theorem) Let \rightsquigarrow be a policy in a view-partitioned system that is

- output consistent,
- step consistent, and
- locally respects \rightsquigarrow .

Then the system is secure for \rightsquigarrow .

This theorem can be formalized in Isabelle/HOL as follows:

theorem simple-noninterference:

assumes outputConsistent:outputConsistent

and stepConsistent: stepConsistent

and LocalRespects: LocalRespects

The following premises are included to include the properties of the equivalence relations

and eqvRelSymmetric:eqvRelSymmetric

and eqvRelTransitive:eqvRelTransitive

and eqvRelreflexive:eqvRelreflexive

shows 5:secure

3.1.7 Rushby Model and Access Control Interpretation

The original Rushby model describes the conditions that an abstract system has to comply to be considered secure. However to consider non-Interference in actual systems he recognized the necessity to provide the system with a more elaborated state structure (*Structured State System*).

First we can consider that partitions will be composed of several memory locations called by Rushby as objects. Each one of these object stores a value.

We use two Isabelle/HOL parametrized types to represent this inner structure:

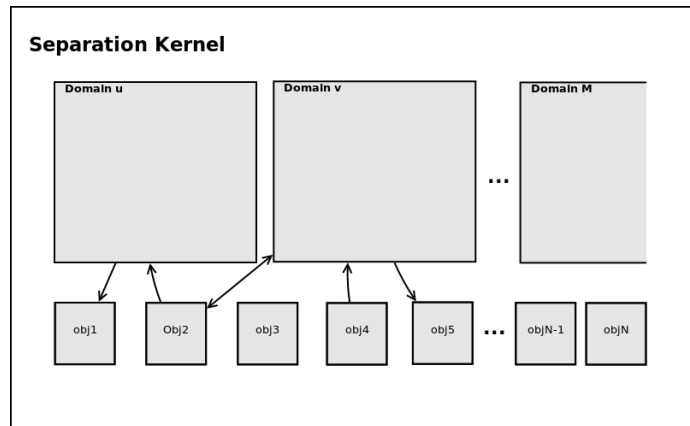


FIGURE 3.3: John Rushby's Structured State System

- 'Object
- 'Value

The system also defines a function *contents* which returns the value of a object in a given state, formalized as:

```
fixes contents :: 'State => 'Object => 'Value
```

3.1.8 Access Control Security Policy

The information flow is controlled with functions *observe* and *alter*, that determine the objects on which a given domain is capable to read or write. Function *observe* returns the set of objects that can be read by the domain given as a parameter.

This function can be modeled with the following expression:

```
fixes observe::'Domain => 'Object set
```

Function *alter* returns the set of objects that can be modified by the domain given as a parameter.

```
fixes alter::'Domain => 'Object set
```

Functions *alter* and *observe* are used to encode an "Access Matrix" used to represent the security policy of the system. Figure 3.3 depicts a graphical representation of a Structured State System with a security policy encoded by the Table 3.1.

D/O	Obj1	Obj2	Obj3	Obj4	Obj5
Domain u	w	r			
Domain v		rw		r	w

TABLE 3.1: John Rushby's Structured System Access Matrix

For a domain u and two states s and t , Rushby defines relation $\overset{u}{\sim}$ by the following formalization:

assumes acRelation:

$$\forall s \ u \ t. (s \sim u \ t) \leftrightarrow (\forall n \in \text{observe } u. \text{contents } s \ n = \text{contents } t \ n)$$

It is easy to prove that $\overset{u}{\sim}$ have the Transitive, Symmetry and Reflexive properties from the equivalence relations:

lemma acRelationisTransitive:

shows eqvRelTransitive

proof –

from acRelation

show ?thesis

unfolding eqvRelTransitive-def **by** auto

qed

lemma acRelationIsSymmetric:

shows eqvRelSymmetric

proof –

from acRelation

show ?thesis

unfolding eqvRelSymmetric-def **by** auto

qed

lemma acRelationIsReflexive:

shows eqvRelreflexive

proof –

from acRelation

show ?thesis

unfolding eqvRelreflexive-def **by** auto

qed

3.1.9 Access Control Reference Monitors.

A State Structured System enforces a security policy when the following conditions are satisfied:

1. The outputs of an action a must depend only of the objects that can be read by the domain u , thus is required that:

definition(in AC) $rma1 :: \text{bool}$ **where**

$$rma1 \equiv (\forall s t a. ((s \sim (\text{dom } a) \sim t) \longrightarrow \text{output } s \ a = \text{output } t \ a))$$

This condition can be seen as an interpretation of the “output consistency” property for state structured systems. This condition requires that for a domain u the values stored in the objects are the same for any sequence of actions α applied on domain u . This property ensures that the values of two states s and t that seem equivalent to a domain u are really indistinguishable no matter what actions are performed on u .

2. When an action is applied to the system, the values of all the modified objects must depend only of the values on the object on which $\text{dom}(a)$ has read access:

definition $rma2 :: \text{bool}$ **where**

$$\begin{aligned} rma2 \equiv (\forall s t a n. (& (s \sim (\text{dom } a) \sim t) \\ & \wedge (\text{contents } (\text{step } a \ s) \ n \neq (\text{contents } s \ n) \\ & \vee \text{contents } (\text{step } a \ t) \ n \neq (\text{contents } t \ n)) \\ \longrightarrow & (\text{contents } (\text{step } a \ s) \ n = \text{contents } (\text{step } a \ t) \ n))) \end{aligned}$$

This condition requires that if one object have the same value for two different states s and t for a domain u . If we execute an action a in both states, the value of the object shall be modified in the same way in the resulting states.

3. If an action a changes the value of object n then $\text{dom}(a)$ must have alter access to n :

definition $rma3 :: \text{bool}$ **where**

$$\begin{aligned} rma3 \equiv (\forall a n s. (\text{contents } (\text{step } a \ s) \ n) \neq (\text{contents } s \ n) \\ \longrightarrow n \in \text{alter } (\text{dom } a)) \end{aligned}$$

Rushby names this three conditions the “Reference Monitor Assumptions” and states a theorem to relate the non-Interference relation and the Access Control System we just described.

Theorem: A system with structured state that satisfies the Reference Monitor Assumptions and the following two conditions.

- $1 \ u \rightsquigarrow v \supset \text{observe}(u) \subseteq \text{observe}(v)$, and

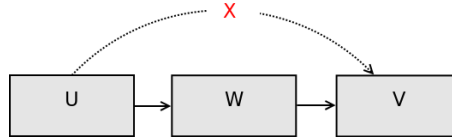


FIGURE 3.4: John Rushby Security Policy Representation

- $2 \ n \in \text{alter}(u) \wedge n \in \text{observe}(v) \supset u \rightsquigarrow v$.

Is secure for the policy \rightsquigarrow .

This theorem can be formalized in Isabelle/HOL as follows:

theorem accessControlSystemIsSecure:

assumes 1: $\forall u \ v. ((u \rightsquigarrow v) \longrightarrow \text{observe } u \subseteq \text{observe } v)$

and 2: $\forall u \ v \ n. ((n \in \text{alter } u) \wedge (n \in \text{observe } v)) \longrightarrow (u \rightsquigarrow v)$

and rma1:rma1

and rma2:rma2

and rma3:rma3

shows secure

On this proof we have formalized Rushby intransitive non-interference model for access control systems. In the next Chapter we will study the GWV separation model.

3.2 Intransitive Non-Interference

The notion of basic non-Interference discussed in Section 2.5.2 is excessively restrictive in some cases; Imagine for example that we have a security policy like the one represented by Figure 3.4 and composed by the following assertions:

$$1. u \rightsquigarrow v$$

$$2. u \rightsquigarrow w$$

$$3. w \rightsquigarrow v$$

Expression 1 ($u \rightsquigarrow v$) forbids the communication between domains u and v and requires that there is no way for domain v to observe any change on the system caused by the actions applied to u . However, this condition is too restrictive on this case and would consider the assertions 2 and 3 as insecure, because the domain v could observe changes caused by actions of u through w .

This kind of policies can be useful for applications such as the one illustrated by Figure 3.5. In this Figure the right arrows connecting the “Downgrader” domain represent intransitive information flows because, although the information can flow without restriction from the lower levels to the higher level, they need to use the “Downgrader” to send the information the other way around.

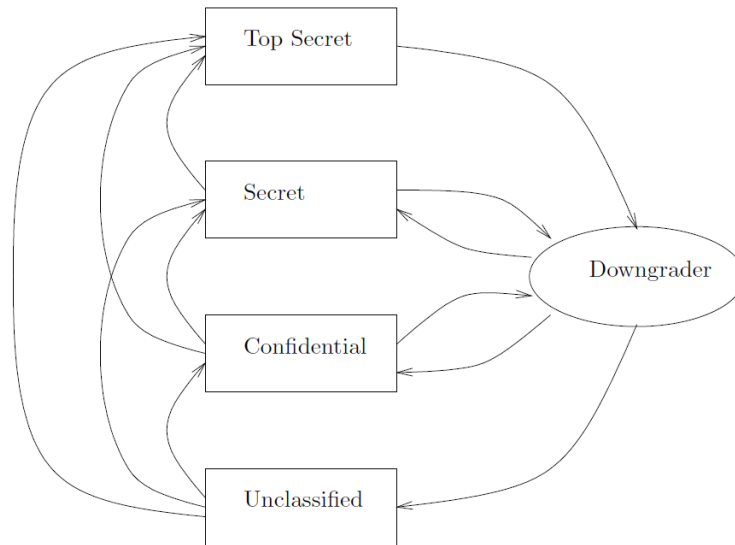


FIGURE 3.5: John Rushby [7]. Controlled Downgrading

To solve this kind of problems Haigh and Young [30] proposed a variant of intransitive non Interference based on an “intransitive purge” function which was later refined by John Rushby [7].

Rushby intransitive policies are defined on the same state machine we described in Chapter 3 with some additional elements we describe in the next sections.

3.2.1 Sources Function

Rushby specify a *sources* function. *sources* receives a list of actions “ α ” and a domain U as parameters, and returns a set of domains. *sources* function is formally defined as follows:

```

primrec sources :: 'Action list => 'Domain => 'Domain set where
  SourcesEmptyCase:sources [] u = {u}
  | SourcesDefList :sources (a# $\alpha$ ) u = (if ( $\exists v. v \in (sources \alpha u) \wedge ((dom a) \rightsquigarrow v)$ )
    then (sources  $\alpha$  u)  $\cup$  {dom a}
    else sources  $\alpha$  u)
  
```

The goal of *sources* function is to determine the Security domains that are allowed to interfere with the domain given as a parameter. In other words $U \in sources(\alpha, V)$ either means that $U = V$ or that there is a subsequence of steps in α such that $U \rightsquigarrow D_1 \rightsquigarrow D_2 \dots \rightsquigarrow D_n \rightsquigarrow V$. It is important to point out that the order on which the actions are executed is important for the sources function. Consider for example the following intransitive security policy:

$$A \rightsquigarrow B$$

$$B \rightsquigarrow C$$

$$A \rightsquigarrow C$$

Defined for a system with a set of actions $\{a, b\}$ such that $dom(a) = A$, $dom(b) = B$. If we apply *sources* function to the two step sequences $\alpha_1 = \{a, b\}$ and $\alpha_2 = \{b, a\}$ for the domain C we would notice that:

$$sources(\alpha_1, C) = \{A, B, C\}, \text{ while}$$

$$sources(\alpha_2, C) = \{B, C\}$$

The reason for this difference is that an α_2 action a is executed after action b . In intransitive policies like this C should not be able to notice changes from A that has not been followed by an action on B .

3.2.2 Ipurge Function

Using *sources* function it is possible to define an *ipurge* function. *ipurge* represents an intransitive version of *purge* function we described in Section 3.1.3.

ipurge can be defined as follows:

```

primrec ipurge :: 'Action list => 'Domain => 'Action list where
  iPurgeEmptyCase:ipurge [] u = [] |
  iPurgeDefList :ipurge (a #  $\alpha$ ) u = (if ((dom a)  $\in$  (sources (a #  $\alpha$ ) u)) then
    a # (ipurge  $\alpha$  u)
    else ipurge  $\alpha$  u)

```

The goal of *ipurge* function is to return a subsequence of α , resulting of deleting all the action that are not allowed to interact with u .

3.2.3 Security Definition for Intransitive Policies.

John Rushby defines an intransitive machine as secure for the policy \rightsquigarrow if:

```

definition isecure::bool where
  isecure  $\equiv$  ( $\forall$   $\alpha$  a. (test  $\alpha$  a) = (test (ipurge  $\alpha$  (dom a) ) a))

```

Under this definition, for a system to be considered secure, no action performed in a security domain can affect the outputs of any other domain on which the interaction is not allowed by a direct interference relation $U \rightsquigarrow V$ or by a intransitive policy ($A \rightsquigarrow B, B \rightsquigarrow C$).

Rushby showed that given an intransitive policy \rightsquigarrow and a view-partitioned, output consistent system such that

$do(\alpha) \stackrel{u}{\sim} do(ipurge(\alpha, u))$.

Then such system is secure for \sim

This lemma can defined in Isabelle/HOL as follows:

```

lemma lemma2:
  assumes  $\forall u \alpha. ((do \alpha) \sim u \sim (do (ipurge \alpha u)))$ 
  and outputConsistent
  shows isecure
proof - {
  from assms show ?thesis
  unfolding outputConsistent-def isecure-def test.simps
  by auto}
qed

```

Rushby defines a new equivalence relation. Given a set of security domains C relation and two states s and t $s \stackrel{C}{\approx} t$ is defined as follows:

```

definition equivalenceRelation :: 'State => 'Domain set=> 'State => bool ((-  $\approx$  - -))
  where equivalenceRelation  $s \ c \ t \equiv \forall u \in c. (s \sim u \sim t)$ 

```

Informally the relation is true when the states s and t look the same for all the members of C .

3.2.4 Weakly step consistency

Intransitive policies requires a weaker version of the step consistency condition we described in Section 3.1.6. A system is weakly step consistent if the states that result from executing an action in equivalent states are equivalent.

Weakly step consistency can be defined as follows:

$$s \stackrel{u}{\sim} t \wedge s \stackrel{dom(a)}{\sim} t \supset step(a, s) \stackrel{u}{\sim} step(a, t)$$

Isabelle/HOL

```

definition weaklyStepConsistent:: bool
  where weaklyStepConsistent  $\equiv$ 
     $\forall s \ u \ t \ a. (s \sim u \sim t) \wedge (s \sim (dom \ a) \sim t) \longrightarrow ((step \ a \ s) \sim u \sim (step \ a \ t))$ 

```

Weak step consistency [31]: can be described informally as follows: If two states look equal to the evaluated partition (u), and also look the same to the partition executing the action ($dom(a)$), then resulting states must also look the same to the evaluated partition (u).

3.2.5 Security of Weak Step Consistent Systems for Intransitive policies

Rushby defines three lemmas to prove the security of weak step consistent systems.

A formal verification of the lemmas has been performed using Isabelle/HOL. The Isabelle/HOL file containing the following proofs can be found in [URL]. The mechanically checked proof of Rushby's Lemmas 3 to 5 and Theorem 7 follow the original approach very closely.

Lemma 3 Let \rightsquigarrow be a policy and M a weakly step consistent view-partitioned system, and locally respects \rightsquigarrow . Then

$$s \stackrel{\text{sources}(a \circ \alpha, u)}{\approx} t \supset \text{step}(s, a) \stackrel{\text{sources}(a \circ \alpha, u)}{\approx} \text{step}(s, t)$$

This lemma can be formalized in Isabelle/HOL as follows:

lemma lemma3:

assumes *weaklyStepConsistent:weaklyStepConsistent*

and *LocalRespects:LocalRespects*

and *equivRelSymmetric:equivRelSymmetric*

and *equivRelTransitive:equivRelTransitive*

shows

$$\forall s a \alpha u t. (s \approx (\text{sources } (a \# \alpha) u) \approx t) \longrightarrow ((\text{step } a s) \approx (\text{sources } \alpha u) \approx (\text{step } a t))$$

Rushby basically proves that in weakly step consistent system, if all the Domains that can modify a domain U are equal in two states s and t , They are going to remain equal after executing the same action in both states.

Lemma 4 Let \rightsquigarrow be a policy and M a view-partitioned system that locally respects \rightsquigarrow . Then

$$\text{dom}(a) \notin \text{sources}(a \circ \alpha, u) \supset s \stackrel{\text{sources}(\alpha, u)}{\approx} \text{step}(a, s)$$

This lemma can be formalized in Isabelle/HOL as follows:

lemma lemma4:

assumes *LocalRespects:LocalRespects*

shows $\forall a \alpha s u. ((\text{dom } a) \notin \text{sources}(a \# \alpha) u) \longrightarrow (s \approx (\text{sources } \alpha u) \approx (\text{step } a s))$

The purpose of this lemma is to show that if the domain of an action a is not allowed to alter a domain u , then the values of all the domains that alter u will remain the same after performing the action a , In other words domain U will be able to observe any action perform by domains that are not allowed to interact with it.

Lemma 5 Let \rightsquigarrow be a policy and M a view-partitioned system which is weakly step consistent, and locally respects \rightsquigarrow . Then

$$s \stackrel{\text{sources}(\alpha, u)}{\approx} \text{step}(a, s) \supset \text{run}(\alpha, s) \stackrel{u}{\sim} \text{run}(\text{ipurge}(\alpha, u)t)$$

We formalized this lemma in Isabelle/HOL as follows:

lemma *lemma5*:

assumes *weaklyStepConsistent:weaklyStepConsistent*
and *LocalRespects:LocalRespects*
and *equivRelSymmetric:equivRelSymmetric*
and *equivRelTransitive:equivRelTransitive*
shows $\forall \alpha s t u. (s \approx (\text{sources } \alpha \ u) \approx t) \longrightarrow ((\text{run } \alpha \ s) \sim u \sim (\text{run } (\text{ipurge } \alpha \ u) \ t))$

Using lemmas 3 to 5, John Rushby proves that the proposed intransitive model is secure

Theorem 7 (Unwinding Theorem for Intransitive Policies) Let \rightsquigarrow be a policy and M a view-partitioned system that is

1. is output consistent,
2. weakly step consistent, and
3. locally respects \rightsquigarrow .

Then M is secure for \rightsquigarrow .

We formalized this theorem in Isabelle/HOL as follows:

theorem *Theorem7*:

assumes *outputConsistent:outputConsistent*
and *weaklyStepConsistent:weaklyStepConsistent*
and *LocalRespects:LocalRespects*
and *equivRelSymmetric:equivRelSymmetric*
and *equivRelTransitive:equivRelTransitive*
and *equivRelreflexive:equivRelreflexive*
shows *isecure*

3.2.6 Security of Intransitive Access Control Systems

Finally, John Rushby proved that the access control system described in Section 3.1.7 works for intransitive noninterference policies as well as for transitive ones.

Theorem 8 Let M be a system with structured state that satisfies the Reference Monitor Assumptions and the condition

$$n \in \text{alter}(u) \wedge n \in \text{observe}(v) \supset u \rightsquigarrow v$$

is secure for \rightsquigarrow .

The aforementioned theorem is translated in Isabelle/HOL as follows:

theorem *Theorem8*:

assumes $1:\forall n u v. (n \in \text{alter } u \wedge n \in \text{observe } v) \longrightarrow (u \rightsquigarrow v)$
and *rma1:rma1*

and *rma2:rma2*
and *rma3:rma3*
shows *isecure*

Chapter 4

GWV Security Policy

In this chapter we describe the Greve, Wildling, Vanfleet (GWV) separation Kernel Formal Security Policy[6]. The original GWV model was formalized in ACL2. In this dissertation we translate the original formalization into Isabelle/HOL.

ACL2 and Isabelle/HOL support different styles of specification and proof. The ACL2 logic is unquantified and untyped, Isabelle/HOL is not only quantified but higher-order (it allows quantification over functions and predicates, not just individuals). However, we were able to successfully translate the original security definition and show that GWV model presents the properties of Exfiltration, Mediation and Infiltration.

4.1 System Model

The GWV formal security policy describes an abstract model of a Separation Kernel. Such model divides a state machine in several memory segments and ensures its separation by controlling the flow of information between them. Figure 4.1 depicts the main components of the GWV system model.

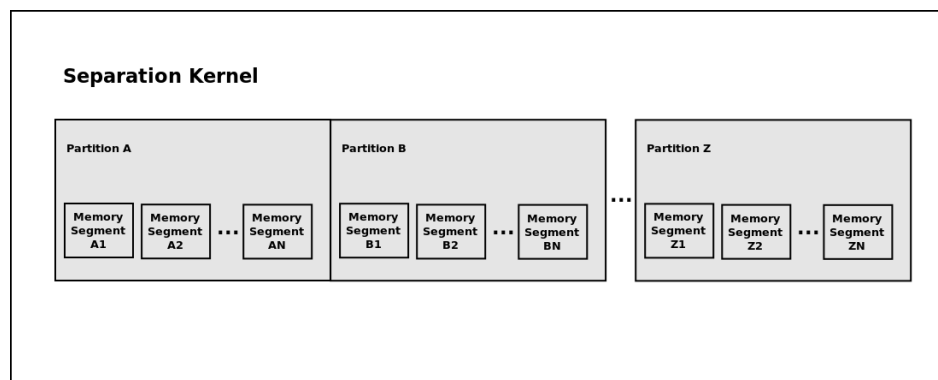


FIGURE 4.1: GWV Separation kernel main components

It is worth pointing out that states in the GWV model are not completely equivalent to the ones described in the Rushby model. In the Rushby model an action a is applied to a state s to change the current state. Whereas, the GWV model does not define a concept for actions. Thus, we consider that a GWV state is composed by a Rushby State and an Action.

As it was mentioned before the GWV security policy is defined over a machine that supports several partitions, with one of them defined as the current partition. Function *current* returns the current active partition given a memory state as parameter.

fixes *current* :: ('State, 'Action) memorystate \Rightarrow 'Domain

Each partition has several memory segments associated with it. Function *segs* takes a partition as parameter and returns the memory segments associated with it. (Note that function *segs* that segments associated to a partition are not modified with current memory state of the machine).

fixes *segs* :: 'Domain \Rightarrow 'Object set

The values stored in a memory segment are extracted by function *select*. *Select* takes two arguments: a segment and a machine memory state and returns all the values stored in the memory segment in the given memory state.

fixes *select* :: ('State, 'Action) memorystate \Rightarrow 'Object \Rightarrow 'Value

The change between memory states is modeled with function *next*, that represents a computation on the state machine. This function takes as an argument a memory state and returns the new memory state of the machine after the execution of a single execution step.

fixes *Next* :: ('State, 'Action) memorystate \Rightarrow ('State, 'Action) memorystate

4.2 Clarification of Next and Current Functions

The way the states are defined within the model GVW can be a bit confusing at first. However, Alvez [8] offers a clarification about the correct interpretation of the *Current* and *Next* functions.

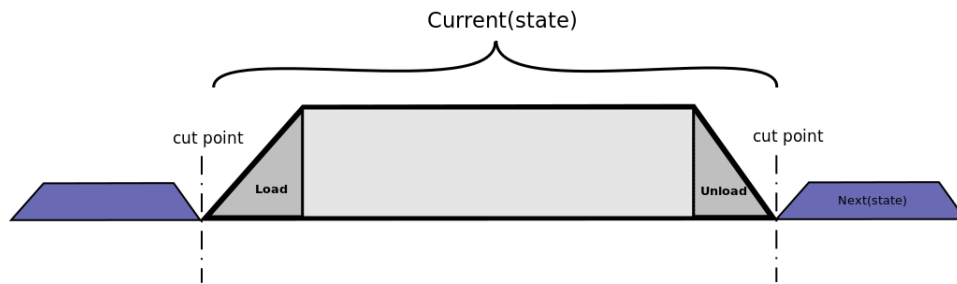


FIGURE 4.2: GWV state change

Figure 4.2 illustrates how the change of states is performed in the GWV model. As it can be seen, when the Next function is executed the kernel invokes, what the author calls a cut point. The cut point is the time the previous state of the kernel has already been saved in memory, but the values of the current state are not yet loaded into the kernel work area. It is at this time when the security policy is evaluated.

When the next function is executed, the separation kernel has the function to execute several steps. First, the values of the current state are loaded to the Kernel working area. Once the data is loaded, the action that corresponds to the current state is executed. When the task is completely executed the partition status is saved to memory. Finally the kernel work area is cleaned before loading the next state.

4.3 Security Policy (Separation)

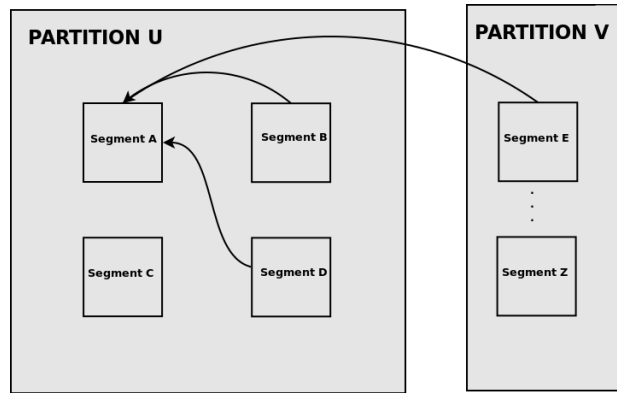
The GWV Separation Kernel model enforces a communication policy between memory segments. The basic idea is to control the information flow between memory segments. This policy is modeled with function “Direct Interaction Allowed” *dia*, which takes as an argument a memory segment and returns a list of memory segments that are allowed to interact with it.

fixes *dia* :: 'Object \Rightarrow 'Object set

Figure 4.3 illustrates how GWV security policies are defined using *dia*. It's worth notice that the only segments which can effect segment *A* are those returned from *dia*, on this case:

$$dia(A) = \{B, E, D\}$$

Finally function *equals* is defined to test if the values of a given set of segments match for two different memory states. Please notice that this function is not present in the

FIGURE 4.3: Information Flow Defined with *dia*

original model. However it greatly increases the readability of the separation lemma described later.

fun equals :: 'Object set \Rightarrow ('State, 'Action) memorystate \Rightarrow ('State, 'Action) memorystate \Rightarrow bool

where

equals A sa sb = (\forall a \in A. select sa a = select sb a)

The security policy requires that any arbitrary memory segment *seg* is only affected by the set of memory segments that are allowed to interact with *seg* and at the same time are associated with the current partition.

definition GWV-secure:: bool **where**

GWV-secure $\equiv \forall$ st1 st2 seg.

current st1 = current st2 \wedge

select st1 seg = select st2 seg \wedge

equals ((*dia* seg) \cap (segs (current st1))) st1 st2

\rightarrow (select (Next st1) seg = select (Next st2) seg)

GWV security Policy states that for any given segment, *seg*, the values of the segment are only affected by memory segments that are allowed to communicate with it and that are part of the currently executing partition. If the separation assumption is preserved, then the only apparent way that a given segment could change is from interaction with segments that are allowed to affect it and that are in *dia*(*seg*).

4.4 Relationship with other formalizations

It is proven [6] that any system that meets the requirements for the *separation* security policy also present three desired properties of the separation kernels, namely Exfiltration,

Mediation and Infiltration. In this section, these properties are presented and proved under the assumption that *separation* holds:

4.4.1 Exfiltration.

Lemma *exfiltration* states that when a step is executed in the current partition, the memory segments can only be affected in a way that is consistent with the communication policy expressed with function *dia*.

lemma exfiltration:

assumes GWV-secure

shows \forall st1 st2 seg. current st1 = current st2 \wedge
 $\text{select st1 seg} = \text{select st2 seg} \wedge$
 $(\text{dia seg}) \cap (\text{segs (current st1)}) = \{\}$
 $\longrightarrow \text{select (Next st1) seg} = \text{select (Next st2) seg}$

proof –

from assms **show** ?thesis **unfolding** GWV-secure-def **by** auto

qed

For this lemma we assume that *dia* for a considered memory segment does not intersect with the segments of the current partition

4.4.2 Infiltration

Lemma *infiltration* states that the values in the current partition are not affected by the data in the segments associated with other partitions.

lemma infiltration:

assumes GWV-secure

shows \forall st1 st2 seg. current st1 = current st2 \wedge
 $\text{seg} \in \text{segs (current st1)} \wedge$
 $\text{equals (segs (current st1)) st1 st2}$
 $\longrightarrow \text{select (Next st1) seg} = \text{select (Next st2) seg}$

proof –

from assms **show** ?thesis **unfolding** GWV-secure-def **by** auto

qed

4.4.3 Mediation

When a process is executed in the current partition, the effect on a segment does not depend on anything else than the segment's original value and the values of the current partition.

lemma mediation:

assumes GWV-secure

shows \forall st1 st2 seg.

current st1 = current st2 \wedge

select st1 seg = select st2 seg \wedge

equals (segs (current st1)) st1 st2

\longrightarrow

select (Next st1) seg = select (Next st2) seg

proof –

from assms **show** ?thesis **unfolding** GWV-secure-def **by** auto

qed

We have proven that our formalization of the GWV separation model holds the *exfiltration*, *infiltration* and *mediation*. properties In the next Chapter we will compare the models we just described to find their main similarities and differences.

Chapter 5

Non-Interference vs GWV

The structure of this chapter is illustrated in Figure 5.1. First we present a mapping between the concepts of the GWV and Rushby models, the mapping includes a definition of the Rushby reference monitor conditions in GWV terms. Next, we use this mapping to check if we can derive the original reference monitor definitions from the GWV versions. Later, we prove that a system with the GWV reference monitors complies with the non-Interference security definition. After that, we show that GWV security definition implies weakly step consistency.

Once we have showed that GWV secure implies weakly step consistency we can use this proof to show that a GWV secure system can be Rushby secure for the transitive and intrasitive Rushby security definitions.

Finally, we show that Rushby's step consistency (transitive model) implies GWV security (with action equality), but Rushby weak step consistency (intransitive model) only implies one of the properties of GWV security known as *Mediation*.

5.1 Mapping Between GWV and Rushby Concepts

The first problem while trying to compare "GWV" and Rushby basic "non-Interference" is that the concepts and components of the two models are not equivalent. In this section we try to find the similarities between these elements and map these equivalences. Table 6.1 presents the mappings between GWV and Rushby functions.

One of the most important similarities between the two models is the way the system is divided. The two models provide separation between processes on different security levels. However, such division is achieved by defining *Partitions* in GWV and security *Domains* in Rushby model. For the rest of this document we consider these concepts as equivalent.

We define function $GWVoutput-f$ which takes a GWV memory state as input and returns the output of that state.

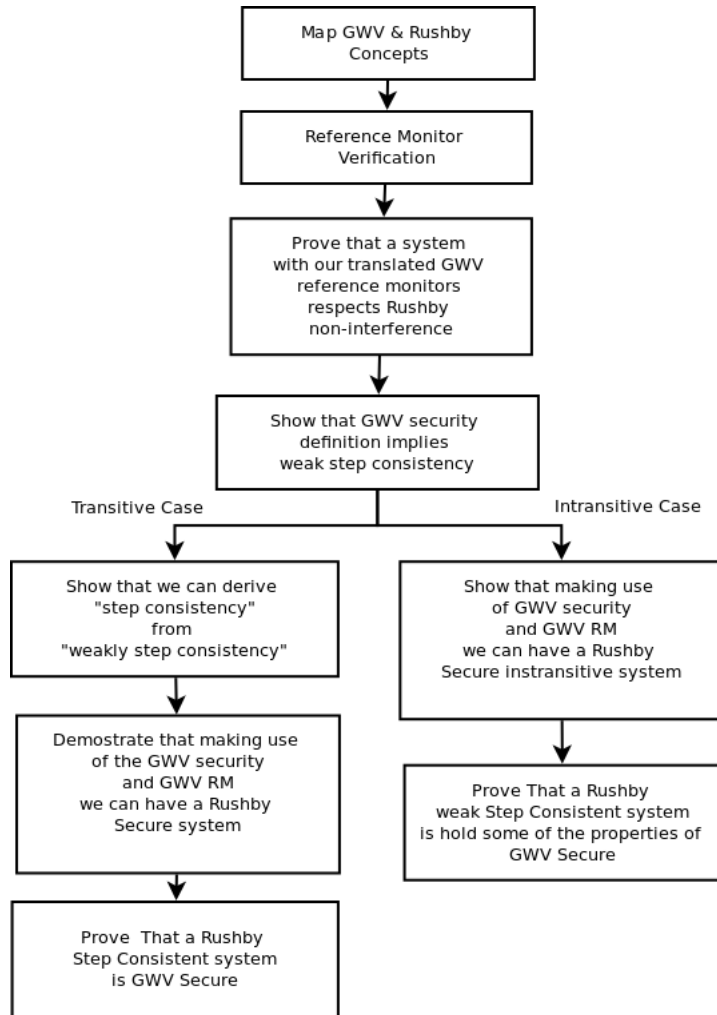


FIGURE 5.1: Overview of the proofs in Chapter 5

fixes $\text{GWVoutput-f} :: ('State, 'Action) \text{memorystate} \Rightarrow 'Output$

GWV does not define an interference relation at the level of partitions. It defines dia , which returns pairs of interfering segments. We now provide a definition of an interference relation in the world of GWV.

definition $\text{GWV}ia :: 'Domain \Rightarrow 'Domain \Rightarrow \text{bool}$ **where**

$$\text{GWV}ia\ u\ v \equiv (\exists\ s\ s'.\ s \in \text{segs}\ v \wedge s' \in \text{dia}\ s \wedge s' \in \text{segs}\ u)$$

We define the mapping between $\text{GWV}ia$ and Rushby's interference relation. This definition basically reads, there is an interference from u to v , if there are two objects s and s' such that s is a segment of v , s' is a segment of u , and s' is allowed to directly interfere with s . In other words, two partitions have an interference relation if they have interfering segments.

definition $\text{intMapping} :: \text{bool}$ **where**

$$\text{intMapping} \equiv \forall\ u\ v.\ (u \rightsquigarrow v) \longleftrightarrow \text{GWV}ia\ u\ v$$

GWV	Rushby	Comments
('State, 'Action) mem- rystate	state	GWV states are not equiv- alent to Ruhsby states. States in GWV contain the Rushby state and the ac- tion to be executed.
Partition	Domain	
Segment	Object	
GWVoutput_ f	Output	We define a new function GWVoutput_ f to represent the output of the machine in a given state.
('State, 'Action) memo- rystate	action	GWV states contains the action that is going to be performed when the next function is called.
$current(segment)$	$dom(dimension)$	
$segs(partition)$	$alter(domain)$	
$select(State, Segment)$	$contents(State, Object)$	
$next(State)$	$step(State)$	
$segs(u)$	$observe(u)$	
$GWVvpeq(s, u, t)$	$s \stackrel{u}{\sim} t$	We define the $GWVvpeq$ function to represent the “view partitioned” equiva- lence relation.
$GWVvia(u, v)$	$u \rightsquigarrow v$	$GWVvia$ function provides a definition of interference relation in the world of GWV.

TABLE 5.1: Mapping between the elements of GWV and Rushby models

In Rushby's model, the equivalence relation "view partitioned" plays a central role. There is no similar relation defined in the context of GWV. Therefore we define such a relation with function *GWVveq*

definition *GWVveq* :: ('State, 'Action) memorystate =>
 'Domain => ('State, 'Action) memorystate => bool
where
GWVveq s p t ≡
 (∀ seg ∈ segs p. select s seg = select t seg)
 ∧ Action s = Action t

According to John Rushby, function "*observe(u)* is the set of locations whose values can be observed by domain *u*." [7]. Whereas in the GWV model, a *partition* is able to read from all the segments assigned to it.

The new definition *observeMapping* maps the Rushby's observe function in the terms of GWV model.

definition *observeMapping*:: bool **where** *observeMapping* ≡ ∀ u. observe u = segs u

In the GWV context a partition can modify ("*alter*") all its assigned partitions.

definition *alterMapping*:: bool **where** *alterMapping* ≡ ∀ u. alter u = segs u

We assume that the values stored in a segment *n* in the GWV state *s* are equal to the values stored in a similar state in the Rushby model.

definition *selectMapping*:: bool **where**
selectMapping ≡ (∀ n memoryState.
 select memoryState n = contents (State memoryState) n)

A mapping between the Rushby *output* and the GWV *GWVoutput-f* functions is defined as follows:

definition *outputMapping*::bool **where**
outputMapping ≡ (∀ memoryState.(GWVoutput-f memoryState) =
 (output (State memoryState) (Action memoryState)))

The active partition returned by function *current* for a state *s*, is equal to the domain returned by the Rusby function *dom* for the state *s*

definition *currentMapping*::bool **where**
currentMapping ≡ ∀ memoryState. current memoryState
 = dom (Action memoryState)

The state obtained after executing the GWV function *next* on a state *s* will be equal to the one obtained from the Rushby *step* function for the action contained within the GWV state.

definition stepMapping::bool **where**

$$\text{stepMapping} \equiv \forall s. \text{State} (\text{Next } s) = \text{step} (\text{Action } s) (\text{State } s)$$

5.2 Equivalence Relation Mapping

We define a equivalent to the Rushby state equivalence relation in GWV terms as follows:

definition GWVvpeqtoRelation::bool **where**

$$\begin{aligned} \text{GWVvpeqtoRelation} &\equiv \forall s \ u \ t. \text{GWVvpeq } s \ u \ t \\ &\longleftrightarrow ((\text{State } s) \sim u \sim (\text{State } t)) \end{aligned}$$

Rushby's $s \stackrel{u}{\sim} t$ relation denotes an equivalence relation. We prove that the GWV mapping holds the *transitivity*, *symmetry* and *reflexivity* properties

definition GWVvpeq-transitive::bool **where**

$$\begin{aligned} \text{GWVvpeq-transitive} &\equiv \forall a \ b \ c \ u. (\text{GWVvpeq } a \ u \ b) \wedge (\text{GWVvpeq } b \ u \ c) \\ &\longrightarrow (\text{GWVvpeq } a \ u \ c) \end{aligned}$$

lemma GWVvpeqIstransitive:

shows GWVvpeq-transitive

proof –

show ?thesis

unfolding GWVvpeq-def GWVvpeq-transitive-def **by** auto

qed

definition GWVvpeq-symmetric::bool **where**

$$\text{GWVvpeq-symmetric} \equiv \forall a \ b \ u. (\text{GWVvpeq } a \ u \ b) \longrightarrow (\text{GWVvpeq } b \ u \ a)$$

lemma GWVvpeqIsSymmetric:

shows GWVvpeq-symmetric

proof –

show ?thesis **unfolding** GWVvpeq-def GWVvpeq-symmetric-def **by** auto

qed

definition GWVvpeq-reflexive::bool **where**

$$\text{GWVvpeq-reflexive} \equiv \forall a \ u. (\text{GWVvpeq } a \ u \ a)$$

lemma GWVvpeqIsReflexive:

shows GWVvpeq-reflexive

proof –

show ?thesis **unfolding** GWVvpeq-def GWVvpeq-reflexive-def **by** auto
qed

5.3 Reference Monitor Mappings

Now that we have mapped all the Rushby concepts to GWV concepts, we can start phrasing Rushby's *accessControlSystemIsSecure* obligations and reference monitor conditions in terms of GWV concepts.

Theorem *accessControlSystemIsSecure* have 3 reference monitor obligations to be discharged.

The first reference monitor:

$$s \stackrel{dom(a)}{\sim} t \supset output(s, a) = output(t, a)$$

Can be expressed in GWV terms, by simply replacing *GWVia*. as follows:

definition GWVrma1::bool **where**

$$\begin{aligned} GWVrma1 &\equiv \forall s t. (GWVvpeq s (current s) t) \\ &\longrightarrow GWVoutput-f s = GWVoutput-f t \end{aligned}$$

The second reference monitor defined as:

$$\begin{aligned} s \stackrel{dom(a)}{\sim} t &\wedge (contents(step(s, a), n) \neq contents(s, n) \\ &\vee contents(step(t, a), n) \neq contents(t, n)) \\ &\supset contents(step(s, a), n) = contents(step(t, a), n). \end{aligned}$$

Can be expressed in GWV terms with the following definition:

definition GWVrma2::bool **where**

$$\begin{aligned} GWVrma2 &\equiv \forall s t n u. ((GWVvpeq s u t) \\ &\wedge (select (Next s) n \neq select s n \\ &\vee select (Next t) n \neq select t n)) \\ &\longrightarrow select (Next s) n = select (Next t) n \end{aligned}$$

Finally the third reference monitor:

$$contents(step(a, s), n) \neq contents(step(a, t), n) \supset n \in alter(dom(a)).$$

can be formalized in the GWV world as follows:

definition GWVrma3::bool **where**

$$GWVrma3 \equiv \forall n s. select (Next s) n \neq select s n \longrightarrow n \in segs (current s)$$

The *accessControlSystemIsSecure* theorem additionally defines two extra conditions that systems must comply to be considered secure:

- 1 $u \rightsquigarrow v \supset \text{observe}(u) \subseteq \text{observe}(v)$, and
- 2 $n \in \text{alter}(u) \wedge n \in \text{observe}(v) \supset u \rightsquigarrow v$.

The aforementioned conditions are expressed with the following definitions:

definition `GWVcond1::bool` **where**

$$\text{GWVcond1} \equiv \forall u v. \text{GWVia } u v \longrightarrow \text{observe } v \supseteq \text{observe } u$$

definition `GWVcond2::bool` **where**

$$\text{GWVcond2} \equiv \forall u v n. (n \in \text{alter } u) \wedge (n \in \text{observe } v) \longrightarrow \text{GWVia } u v$$

5.4 Reference Monitor Verification

In this section we verify the mappings between GWV and Rushby reference monitor obligations, proving that the new GWV definitions can be translated into the ones defined by Rushby.

First we prove the translation of the proof obligation 1. The goal of this lemma is to demonstrate that if a domain "u" can alter the values of other domain v , then that all objects observable by u are also observable by v

lemma `proofobligation1Mapping`:

assumes `GWVcond1:GWVcond1`

and `intMapping:intMapping`

shows $\forall u v. (u \rightsquigarrow v) \longrightarrow \text{observe } v \supseteq \text{observe } u$

proof –

from `GWVcond1` **and** `intMapping` **show** `?thesis`

unfolding `intMapping-def` `GWVcond1-def` **by** `metis`

This lemma is proven directly from the definition of the first condition and the mappings

qed

Now we verify the mapping for proof obligation 2. The purpose of this lemma is to prove that if an object can be written by a domain u and read by a domain v then we have an interference relation $u \rightsquigarrow v$ between u and v

lemma `proofobligation2Mapping`:

assumes `GWVcond2:GWVcond2`

and `intMapping:intMapping`

shows

$$\forall u v n. ((n \in \text{alter } u) \wedge (n \in \text{observe } v)) \longrightarrow (u \rightsquigarrow v)$$

proof –

We use the mappings to replace the GWV terms with the Rushby ones

thm GWVcond2-def

from GWVcond2 **and** GWVia-def **and** intMapping **show**

?thesis

unfolding intMapping-def GWVcond2-def **by** auto

The lemma is proven from the mapping and the definition of *GWVcond2*

qed

The next step is to prove the GWV reference monitor for the Rushby proof obligation 3. We have separated this proof in two lemmas:

lemma *proof-obligation3* proves that *GWVrma1* can be mapped to an intermediate expression similar to *rma1* but using GWV states.

lemma GWVproofobligation3:

assumes GWVrma1:GWVrma1

and outputMapping:outputMapping

and currentMapping:currentMapping

and GWVvpeqtoRelation:GWVvpeqtoRelation

shows $\forall s t. ((\text{State } s) \sim \text{dom } (\text{Action } s) \sim (\text{State } t))$

$\longrightarrow \text{output } (\text{State } s) (\text{Action } s) = \text{output } (\text{State } t) (\text{Action } s)$

proof –

{

fix s t::('State, 'Action) memorystate

We make use of the definition of *GWVrma1* and the mappings to get the intermediate expression.

from assms

have $((\text{State } s) \sim (\text{dom } (\text{Action } s)) \sim (\text{State } t)) \longrightarrow$

$\text{output } (\text{State } s) (\text{Action } s) = \text{output } (\text{State } t) (\text{Action } s)$

unfolding GWVrma1-def GWVvpeqtoRelation-def currentMapping-def

outputMapping-def GWVvpeq-def **by** metis

}

then show ?thesis **by** (metis select-convs(1) select-convs(2))

qed

The second lemma *GWVrma1ToRma1* invokes *proof-obligation3* to prove that *GWVrma1* implies the First Rushby's reference monitor (*rma1*) making use of the new intermediate expression.

lemma GWVrma1ToRma1:

assumes GWVrma1:GWVrma1

```

and    outputMapping:outputMapping
and    currentMapping:currentMapping
and    GWVvpeqtoRelation:GWVvpeqtoRelation
shows rma1
rma1 states that two equivalent states have the same output
proof -
{
  from assms and GWVproofobligation3 have
     $\forall (s::'State) (t::'State) (a::'Action).$ 

      ((State (|State = s, Action = a|)) ~
       dom (Action (|State = s, Action = a|)) ~
       (State (|State = t, Action = a|)))

       $\longrightarrow$  output (State (|State = s, Action = a|)) (Action (|State = s, Action = a|))
      = output (State (|State = t, Action = a|)) (Action (|State = s, Action = a|))

by metis
}
The proof directly follows from the intermediate definition.
then show rma1
unfolding rma1-def
by (metis select-convs(1) select-convs(2))
qed

```

In a similar way, we can prove that our new definition implies the second Rushby's reference monitor, separating this proof in two lemmas:

lemma *proof-obligation4* proves that *GWVrma2* can be mapped to an intermediate expression similar to *rma2* but using GWV states.

```

lemma proof-obligation4:
  assumes GWVrma2:GWVrma2
  and    selectMapping:selectMapping
  and    stepMapping:stepMapping
  and    GWVvpeqtoRelation:GWVvpeqtoRelation

  shows ( $\forall (s::('State, 'Action) \text{memorystate}) (t::('State, 'Action) \text{memorystate})$ 
n.( ((State s) ~ (dom (Action s)) ~ (State t))
     $\wedge$  (contents (step (Action s) (State s)) n  $\neq$  contents (State s) n)
     $\vee$  (contents (step (Action t) (State t)) n  $\neq$  contents (State t) n)
     $\longrightarrow$  contents (step (Action s) (State s)) n)

```

```

      = contents (step (Action t) (State t)) n
    )
proof -
  {
    fix s t::('State, 'Action) memorystate
    fix n :: 'Object

    from assms have
      (((State s) ~ (dom (Action s)) ~ (State t)) ^
       (contents (step (Action s) (State s)) n ≠ contents (State s) n
        ∨ contents (step (Action t) (State t)) n ≠ contents (State t) n))
      →
        contents (step (Action s) (State s)) n
      = contents (step (Action t) (State t)) n
    We prove this lemma simply by using the definition of the GWVrma2 and
    the mappings
    unfolding GWVrma2-def selectMapping-def stepMapping-def
      GWVvpeqtoRelation-def
    by auto

  }
  then show ?thesis by auto
qed

```

The second lemma *GWVrma2ToRma2* uses *proof-obligation4* to show that *GWVrma2* implies the second Rushby's reference monitor (*rma2*) making use of the new intermediate expression.

lemma *GWVrma2ToRma2*:

```

  assumes GWVrma2:GWVrma2
  and    selectMapping:selectMapping
  and    stepMapping: stepMapping
  and    GWVvpeqtoRelation:GWVvpeqtoRelation
shows rma2

```

proof -

This expression will be used to transform the *GWVrma2* into the conclusion of *proof-obligation4* lemma.

from assms **and** *proof-obligation4* **have**

$(\forall (s::\text{State}) (t::\text{State}) (a::\text{Action}) (n::\text{Object}).$

$$\begin{aligned} & ((\text{State } (\text{State} = s, \text{Action} = a)) \sim \\ & (\text{dom } (\text{Action } (\text{State} = s, \text{Action} = a))) \sim \\ & (\text{State } (\text{State} = t, \text{Action} = a))) \\ & \wedge (\text{contents } (\text{step } (\text{Action } (\text{State} = s, \text{Action} = a))) \\ & \quad (\text{State } (\text{State} = s, \text{Action} = a))) n \\ & \quad \neq \text{contents } (\text{State } (\text{State} = s, \text{Action} = a))) n \\ & \vee \text{contents } (\text{step } (\text{Action } (\text{State} = t, \text{Action} = a))) \\ & \quad (\text{State } (\text{State} = t, \text{Action} = a))) n \\ & \quad \neq \text{contents } (\text{State } (\text{State} = t, \text{Action} = a))) n \\ & \longrightarrow \text{contents } (\text{step } (\text{Action } (\text{State} = s, \text{Action} = a))) \\ & \quad (\text{State } (\text{State} = s, \text{Action} = a))) n \\ & = \text{contents } (\text{step } (\text{Action } (\text{State} = t, \text{Action} = a))) \\ & \quad (\text{State } (\text{State} = t, \text{Action} = a))) n \\ &) \end{aligned}$$

unfolding selectMapping-def stepMapping-def **by** metis

Then the proof falls directly from this transformation and the mappings
from this and selectMapping **and** stepMapping **and** select-conv(1) **and** select-conv(2)

show ?thesis

unfolding currentMapping-def selectMapping-def rma2-def stepMapping-def
by auto

qed

Finally we prove that the mapping for the Third reference monitor is correct, by making use of a similar strategy to the previous two monitors.

lemma *proof-obligation5* shows that $GWVrma3$ can be mapped to an intermediate expression similar to $rma3$ with GWV states.

lemma proof-obligation5:

assumes GWVrma3:GWVrma3

and selectMapping:selectMapping

and stepMapping:stepMapping

and alterMapping:alterMapping

and currentMapping:currentMapping

shows $\forall a n s. \text{contents } (\text{step } (\text{Action } s) (\text{State } s)) n \neq \text{contents } (\text{State } s) n$
 $\longrightarrow n \in \text{alter } (\text{dom } (\text{Action } s))$

```

proof -
{
  fix s t::('State, 'Action) memorystate
  fix n :: 'Object

```

We prove the intermediate expression by making use of the mappings and the

GWVrma3 definition

```

from GWVrma3 and selectMapping and stepMapping and currentMapping
and alterMapping

```

```

have

```

```

contents (step (Action s) (State s)) n ≠ contents (State s) n
  → n ∈ alter (dom (Action s))

```

```

unfolding GWVrma3-def selectMapping-def stepMapping-def currentMapping-def
alterMapping-def
by (metis (full-types))

```

```

}

```

```

then show ?thesis by (metis (mono-tags) select-convs(1) select-convs(2))

```

```

qed

```

The lemma *GWVrma3ToRma3* uses *proof-obligation5* to show that *GWVrma3* implies the last Rushby's reference monitor (*rma3*).

lemma *GWVrma3ToRma3*:

```

assumes GWVrma3:GWVrma3
and   selectMapping:selectMapping
and   stepMapping:stepMapping
and   alterMapping:alterMapping
and   currentMapping:currentMapping

```

shows *rma3*

```

proof -

```

```

{

```

We define a transformation expression to convert *GWVrma3* into *rma3* by invoking the *proof-obligation5* lemma.

```

from assms and proof-obligation5

```

```

have

```

```

∀ (s::'State) (a::'Action) (n::'Object).
  contents (step (Action (|State = s, Action = a|))
    (State (|State = s, Action = a|))) n

```

```

≠ contents (State (State = s, Action = a)) n
→ n ∈ alter (dom (Action (State = s, Action = a)))
unfolding GWVrma3-def
by metis
}

```

The proof directly follows from the mapping and this transformation expression

```

from this show ?thesis unfolding rma3-def
by (metis select-convs(1) select-convs(2))
qed

```

We now show that a system that satisfies GWV reference monitors we just formulated can be considered secure under Rushby's definition.

lemma GWVmapsAreRushbySecure:

We use the definitions for the GWV reference monitors

```

assumes GWVrma1:GWVrma1
and GWVrma2:GWVrma2
and GWVrma3
and GWVcond1
and GWVcond2

```

And we use the mappings

```

and selectMapping:selectMapping
and stepMapping:stepMapping
and outputMapping:outputMapping
and alterMapping:alterMapping
and currentMapping:currentMapping
and GWVvpeqtoRelation:GWVvpeqtoRelation
and GWVvpeqtoRelation:GWVvpeqtoRelation
and intMapping

```

shows secure

proof –

```

from assms
and GWVrma1ToRma1
and GWVrma2ToRma2
and GWVrma3ToRma3
and proofobligation1Mapping
and proofobligation2Mapping

```

We just invoke the Rushby's *accessControlSystemIsSecure* lemma to complete the proof



FIGURE 5.2: Relation Between GWV secure and Weakly Step Consistency definitions.

```

and accessControlSystemIsSecure show secure by auto
qed

```

5.5 Proof of GWV Step Consistency

In the previous section we shown that a system modeled with with GWV components can be considered secure under Rushby "non-Interference" definition. Figure 5.2 illustrates the relation between the GWV security and Rushby's step consistency definitions. We show that the GWV definition of security *GWV-secure* implies Rushby "Weak Step Consistency" (*weaklyStepConsistent*).

lemma GWV-WeakStepConsitent:

```

assumes GWV-secure:GWV-secure
and currentMapping:currentMapping
and ActionStep: $\forall s\ t\ u. GWVvpeq\ s\ u\ t \longrightarrow Action\ (Next\ s) = Action\ (Next\ t)$ 
shows  $\forall s\ u\ t. GWVvpeq\ s\ u\ t \wedge GWVvpeq\ s\ (current\ s)\ t \longrightarrow GWVvpeq\ (Next\ s)\ u\ (Next\ t)$ 

```

proof (auto)

{

fix s t::('State, 'Action) memorystate

fix u::'Domain

assume uEquiv:GWVvpeq s u t

assume currentEquiv:GWVvpeq s (current s) t

show GWVvpeq (Next s) u (Next t)

unfolding GWVvpeq-def

proof {

From the definition of *GWVvpeq* we need to prove 2 goals:

GWVvpeq (Next s) u (Next t) 1. $\forall seg \in segs\ u. select\ (Next\ s)\ seg = select\ (Next\ t)$
 seg 2. $Action\ (Next\ s) = Action\ (Next\ t)$

show $\forall n \in segs\ u. select\ (Next\ s)\ n = select\ (Next\ t)\ n$

proof {

fix n::'Object

assume observe:n \in segs u

show select (Next s) n = select (Next t) n

this is the conclusion of the *GWV-secure* definition

proof – {

We get each one of the premises of *GWV-secure*

from GWV_{vpeq} relation and the mappings.

from currentEquiv **and** currentMapping **have** sec1:current s = current t
unfolding $GWV_{\text{vpeq}}\text{-def}$ currentMapping-def **by** auto

from currentEquiv **and** observe **have** sec2:select t n = select t n
unfolding $GWV_{\text{vpeq}}\text{-def}$ **by** auto

from currentEquiv **have** sec3:Action s = Action t
unfolding $GWV_{\text{vpeq}}\text{-def}$ **by** auto

from currentEquiv **and** observe
have sec4:equals (dia n \cap segs (current s)) s t
unfolding $GWV_{\text{vpeq}}\text{-def}$
by auto

the proof of this goal, then directly follows the above facts and
GWV_ssecure

from sec1 sec2 sec3 sec4 **and** *GWV-secure*
and observe currentEquiv $GWV_{\text{vpeq}}\text{-def}$
show select (Next s) n = select (Next t) n
unfolding *GWV-secure-def* $GWV_{\text{vpeq}}\text{-def}$
by (metis $GWV_{\text{vpeq}}\text{-def}$ uEquiv)

} qed

} qed

next

The proof of the second goal is trivial from our ActionStep assumption.

from currentEquiv **and** ActionStep **show** Action (Next s) = Action (Next t)
unfolding $GWV_{\text{vpeq}}\text{-def}$ **by** auto

}

qed

}

qed

Now we prove that Weak Step Consistency (under GWV terms) can also be transformed into an expression under Rushby terms.

lemma `GWV-RushbyWeakStepConsistent`:
assumes `GWV-secure: GWV-secure`
and `currentMapping:currentMapping`
and `ActionStep:∀ s t u . GWVvpeq s u t ⟶ Action (Next s) = Action (Next t)`
and `GWVvpeqtoRelation:GWVvpeqtoRelation`
and `stepMapping:stepMapping`
shows `weaklyStepConsistent`

5.5.1 “Strengthening” Weakly Step Consistency.

Figure 5.3 shows the relation between Rushby’s “step consistency” and “weak step consistency” definitions. As the following lemma shows is trivial to prove that step consistency implies “weakly step consistency”.

lemma
assumes `stepConsistent`
shows `weaklyStepConsistent`
proof –
from `assms` **show** `?thesis`
unfolding `stepConsistent-def` **and** `weaklyStepConsistent-def`
by `auto`
qed

To show the reverse implication we propose the following lemma.

Lemma: A Weakly Step Consistent system that satisfies the third Reference Monitor Assumption we described in Section 3.1.9, and the following two conditions (originally proposed by Rushby).

- 1 $u \rightsquigarrow v \supset \text{observe}(u) \subseteq \text{observe}(v)$, and
- 2 $n \in \text{alter}(u) \wedge n \in \text{observe}(v) \supset u \rightsquigarrow v$.

is also step Consistent.

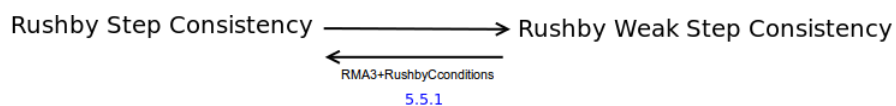


FIGURE 5.3: Relation Between Weakly Step Consistency and Step Consistency definitions.

In the next proof we demonstrate this lemma by separating the proof in two steps; first we prove the case when there is no change in the values of the state after executing the a step in the state machine, the proof for this case is trivial and fall directly from the equality properties of the state equivalence relation. For the second case we have a change in the values of the evaluated memory segment, for this case we use the third reference monitor $\forall a n s . (contents (step a s) n) \neq (contents s n) \longrightarrow n \in alter (dom a)$ ” to prove that having this additional condition we can ansure step consistency.

lemma weakStepConsistencyToStepConsistent:

assumes 1: $\forall u v. ((u \rightsquigarrow v) \longrightarrow observe\ u \subseteq observe\ v)$
and 2: $\forall u v n. ((n \in alter\ u) \wedge (n \in observe\ v)) \longrightarrow (u \rightsquigarrow v)$
and weaklyStepConsistent:weaklyStepConsistent
and rma3:rma3
shows stepConsistent

proof –{

fix a::'Action
fix s t::'State
fix u::'Domain
fix n::'Object

—To prove step consistency we can rewrite its definition as:

have $((s \sim u \sim t) \wedge (n \in observe\ u)) \longrightarrow$
 $(contents (step a s) n = contents (step a t) n)$

To prove this expression we have two cases to consider:

proof (case-tac $contents (step a t) n = contents\ t\ n$
 $\wedge contents (step a s) n = contents\ s\ n$) {

{

{

—for the first case:

$contents (step a t) n = contents\ t\ n$
 $\wedge contents (step a s) n = contents\ s\ n,$

we have $contents\ s\ n = contents\ t\ n$ then the proof of this case is trivial

assume case1: $contents (step a t) n = contents\ t\ n$
 $\wedge contents (step a s) n = contents\ s\ n$

show $((s \sim u \sim t) \wedge (n \in observe\ u))$

$\longrightarrow (contents (step a s) n = contents (step a t) n)$

proof {

assume hyp:($s \sim u \sim t$) \wedge ($n \in \text{observe } u$)
from hyp **and** acRelation **have** contents $s \ n =$ contents $t \ n$ **by** auto
from this **and** case1
show (contents (step a s) n) $=$ (contents (step a t) n) **by** simp
}qed
}
next
{
—In the second case we have a change in any of the states after a step is executed
assume case2: \neg (contents (step a t) $n =$ contents $t \ n$
 \wedge contents (step a s) $n =$ contents $s \ n$)
show (($s \sim u \sim t$) \wedge ($n \in \text{observe } u$))
 \longrightarrow contents (step a s) $n =$ contents (step a t) n
proof {
assume hyp:($s \sim u \sim t$) \wedge ($n \in \text{observe } u$)
—This case can be rewritten as follows for simplicity:
($\text{contents (step } a \ t) \ n \neq \text{contents } t \ n$)
 \vee ($\text{contents (step } a \ s) \ n \neq \text{contents } s \ n$)
from case2 **have**
case2Rew:(contents (step a t) $n \neq$ contents $t \ n$)
 \vee (contents (step a s) $n \neq$ contents $s \ n$)
by simp

—From the third reference monitor we have $n \in \text{alter } (\text{dom } a)$
from this **and** rma3 **have** $n \in \text{alter } (\text{dom } a)$
unfolding rma3-def **by** auto

—Using the first and second conditions of the theorem we
have that : $\text{observe } (\text{dom } a) \subseteq \text{observe } u$
from this **and** 1 **and** 2 **and** hyp
have $\text{observe } (\text{dom } a) \subseteq \text{observe } u$ **by** metis

—Then we have that ($s \sim u \sim t$) implies $s \sim (\text{dom } a) \sim t$
from this **and** acRelation **and** hyp **have** $s \sim (\text{dom } a) \sim t$ **by** auto

—finally using the weak Step Consistency definition we finish the
proof for this case.
from this **and** weaklyStepConsistent


```

      show contents (step a s) n = contents (step a t) n
      unfolding weaklyStepConsistent-def
      by (metis acRelation hyp)
    } qed end of the second case
  }
}
}
qed end of the step consistency proof
}
from this and acRelation show ?thesis unfolding stepConsistent-def
by smt
qed

```

Using this lemma we show Weakly Step Consistency can be “strengthen” to the original Step Consistency definition if we use some of the other conditions on the Rushby Intransitive model.

5.5.2 Security of Weak Step Consistent Systems for Transitive Policies

Using previous lemma we can show that:

Theorem: A Weakly Step Consistent system with structured state that satisfies the third Monitor Assumption and the following two conditions.

- 1 $u \rightsquigarrow v \supset \text{observe}(u) \subseteq \text{observe}(v)$, and
- 2 $n \in \text{alter}(u) \wedge n \in \text{observe}(v) \supset u \rightsquigarrow v$.

Is secure for the policy \rightsquigarrow .

We prove this lemma in Isabelle/HOL as follows:

theorem weakStepConsistentSystemIsSecure:

```

  assumes 1:  $\forall u v. ((u \rightsquigarrow v) \longrightarrow \text{observe } u \subseteq \text{observe } v)$ 
  and     2:  $\forall u v n. ((n \in \text{alter } u) \wedge (n \in \text{observe } v)) \longrightarrow (u \rightsquigarrow v)$ 
  and     rma1:rma1
  and     weaklyStepConsistent:weaklyStepConsistent
  and     rma3:rma3
  shows secure

```

proof –

To prove this theorem we need to show that our assumptions imply *outputConsistent*, *stepConsistent* and *LocalRespects*

Output consistency (*outputConsistent*) can be proven directly from the first reference monitor *rma1*

```
from rma1 have outputConsistent:outputConsistent
unfolding rma1-def and outputConsistent-def by auto
```

To show that the system holds the locally respects condition (*LocalRespects*), we need to show: $(s \sim u \sim (\text{step } a \ s))$ that can be proven from the definition of $\overset{u}{\sim}$ and the third reference monitor (*rma3*)

```
have LocalRespects:LocalRespects
unfolding LocalRespects-def
proof (auto){
  fix a::'Action
  fix s::'State
  fix u::'Domain
  assume notInt:(dom a)  $\overset{u}{\sim}$  u
  from notInt show (s  $\sim$  u  $\sim$  (step a s))
  by (metis 2 acRelation rma3 rma3-def)
}
qed
```

to show step consistency we invoke the *weakStepConsistencyToStepConsistent* lemma

```
from assms have stepConsistent:stepConsistent using weakStepConsistencyToStepConsistent
by auto
```

Once we have proven that the AC system complies with the *outputConsistent*, *stepConsistent* and *LocalRespects* conditions, we simply invoke the *simple-noninterference* to show this system is secure.

```
from outputConsistent and LocalRespects and stepConsistent and
simple-noninterference
show ?thesis by auto
qed
```

5.5.3 Non-interference for GWV Secure Systems

Finally in the following theorem we prove a new version of Rusby's Theorem 2 (*accessControlSystemIsSecure*). For this Theorem we do not assume *GWVrma2* but we derive *stepConsistent* from *GWVsecure*, *Weak Step Consistency* and *GWVcond1*.

```
theorem GWVSystemIsSecure:
```

We use the definitions for the GWV reference monitors

assumes GWVrma1:GWVrma1
and GWV-secure:GWV-secure
and GWVrma3:GWVrma3
and GWVcond1:GWVcond1
and GWVcond2:GWVcond2
and ActionStep: $\forall s t u . \text{GWVvpeq } s u t \longrightarrow \text{Action (Next s) = Action (Next t)}$

And we use the mappings

and selectMapping:selectMapping
and stepMapping:stepMapping
and outputMapping:outputMapping
and alterMapping:alterMapping
and currentMapping:currentMapping
and GWVvpeqtoRelation:GWVvpeqtoRelation
and intMapping

shows secure

proof –

for this theorem we need to prove that the three GWV reference monitors and the two

additional conditions imply *outputConsistent*, *stepConsistent* and *LocalRespects*

we use the GWV reference monitor definitions and the mapping to get the original Rushby reference monitors

from assms **and** GWVrma1ToRma1 **have** rma1:rma1 **by** auto

from assms **and** GWVrma3ToRma3 **have** rma3:rma3 **by** auto

from assms **and** proofobligation2Mapping

have 2: $\forall u v n . ((n \in \text{alter } u) \wedge (n \in \text{observe } v)) \longrightarrow (u \rightsquigarrow v)$ **by** auto

from assms **and** proofobligation1Mapping

have 1: $\forall u v . ((u \rightsquigarrow v) \longrightarrow \text{observe } u \subseteq \text{observe } v)$ **by** auto

from assms **and** GWV-RushbyWeakStepConsitent **have**

weakStepConsistent:weaklyStepConsistent

by auto

Output consistency (*outputConsistent*) can be proven directly from the first reference monitor *rma1*

```
from rma1 have outputConsistent:outputConsistent
unfolding rma1-def and outputConsistent-def by auto
```

To show that the system locally respects condition (*LocalRespects*), we need to show: $(s \sim u \sim (\text{step } a \ s))$ that can be proven from the definition of $\overset{u}{\sim}$ and the third reference monitor (*rma3*)

```
have LocalRespects:LocalRespects
unfolding LocalRespects-def
  proof (auto){
    fix a::'Action
    fix s::'State
    fix u::'Domain
    assume notInt:(dom a)  $\overset{u}{\sim}$  u
    from notInt show (s  $\sim$  u  $\sim$  (step a s))
      by (metis 2 acRelation rma3 rma3-def)
  }
qed
```

Now we invoke the *weakStepConsistencyToStepConsistent* lemma to show step Consistency

```
from weakStepConsistent and 1 and 2 and rma3
have stepConsistent:stepConsistent
using weakStepConsistencyToStepConsistent
by auto
```

Once we have proven that we comply with the *simple-noninterference* is easy to show that the system is secure.

```
from acRelationisTransitive have eqvRelTransitive:eqvRelTransitive by auto
from acRelationIsSymmetric have eqvRelSymmetric:eqvRelSymmetric by auto
from acRelationIsReflexive have eqvRelreflexive:eqvRelreflexive by auto
```

```
from outputConsistent and LocalRespects and stepConsistent and simple-noninterference
and eqvRelTransitive and eqvRelSymmetric and eqvRelreflexive
show ?thesis by auto
```

qed

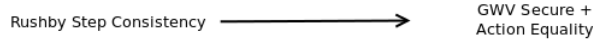


FIGURE 5.4: Relation Between Weakly Step Consistency and GWV secure definitions.

5.6 Comparing GWV Secure vs Rushby's Step Consistency

In this section we show that GWV security notion is contained by Rushby Step Consistency definition. In other words that a Step Consistent Rushby system is also GWV Secure. This relation is illustrated by Figure 5.4.

lemma *GWVstepConsistent* is used to translate Rushby step consistency $s \sim u \sim t \rightarrow (\text{step } a \ s) \sim u \sim (\text{step } a \ t)$ into an equivalent expression given under GWV terms: $GWVvpeq \ s \ u \ t \rightarrow GWVvpeq \ (\text{Next } s) \ u \ (\text{Next } t)$

One primary difference between the Rushby and GWV models, is result of the way of how their state machines are defined. On one hand, the Rushby model defines state transitions through *step* function:

-step : Action \times State \rightarrow State

On the other hand, GWV model defines state changes with *next* function:

-Next : State \rightarrow State

Taking a look on *Next* definition, we can notice that GWV states transitions are deterministic. In other words, A state s will always result in the same state s' after executing *next* function. Whereas, in the Rushby model an state can execute different actions, that will affect the outcome of the *step* function.

As a result of this difference, to deduce the GWV separation theorem from the Rushby model, we need to prove that the action executed by the states on GWV separation theorem is the same. This is impossible to prove because in the same current partition there can be different active tasks. To avoid it, we introduced a notion of action equality to GWV model.

definition GWV-secure-wAction:: bool **where**

GWV-secure-wAction $\equiv \forall \ st1 \ st2 \ seg.$

current st1 = current st2 \wedge

select st1 seg = select st2 seg \wedge

Action st1 = Action st2 \wedge

$$\begin{aligned} & \text{equals } ((\text{dia seg}) \cap (\text{segs } (\text{current st1}))) \text{ st1 st2} \\ & \longrightarrow (\text{select } (\text{Next st1}) \text{ seg} = \text{select } (\text{Next st2}) \text{ seg}) \end{aligned}$$

We define an Isabelle/HOL lemma to show that the original GWV secure definition implies our new formulation including action equality:

```

lemma GWVsecure-wAction-isSecure:
  assumes GWV-secure:GWV-secure
  shows GWV-secure-wAction
proof -
  from assms show ?thesis unfolding GWV-secure-def GWV-secure-wAction-def
  by auto
qed

```

We now prove that Rushby step consistency implies our new definition of GWV secure with action equality, for this theorem we needed to add an extra hypothesis named *hyp*:

$$\text{hyp: } \forall n. \exists p. n \in \text{segs } p \wedge (\forall n'. n' \in \text{segs } p \longrightarrow n' = n)$$

This extra hypothesis is composed by two parts $\forall n. \exists p. n \in \text{segs } p$ states that every partition should be assigned at least one partition, and $(\forall n'. n' \in \text{segs } p \longrightarrow n' = n)$ requires that every partition has (only) one memory segment assigned to it.

```

theorem stepConsistencyImpliesGWVSecure:
  assumes 1: stepConsistent
  and      2: stepMapping
  and      3: selectMapping
  and      4: observeMapping
  and      5: GWVvpeqtoRelation
  and      hyp:  $\forall n. \exists p. n \in \text{segs } p \wedge (\forall n'. n' \in \text{segs } p \longrightarrow n' = n)$ 

```

```

shows GWV-secure-wAction

```

```

proof -
  show ?thesis
  unfolding GWV-secure-wAction-def

  proof auto{
    fix st1 st2::('State, 'Action) memorystate
    fix seg::'Object
    we use the hypothesis of the GWV-secure definition.
  }

```

```

assume GWVhyp2:select st1 seg = select st2 seg
assume GWVhyp3:Action st1 = Action st2

```

```

show select (Next st1) seg = select (Next st2) seg
  proof–{

```

Using the *GWVstepConsistent* lemma and our premises we prove that having two equivalent states and a segment that belongs to a partition and we apply the same action to the states, then the values will remain the same after executing a step on the state machine.

```

have GWVstepconst:∀ u. GWVvpeq st1 u st2 ∧ seg ∈ segs u
  → (select (Next st1) seg = select (Next st2) seg)
using GWVstepConsistent and assms
unfolding GWVvpeq-def
by auto

```

The conclusion directly falls from the last fact and the action equality of the third GWV premise *GWVhyp3*

```

then show ?thesis using hyp GWVhyp2 GWVhyp3 unfolding GWVvpeq-def
by metis
  }
  qed
}qed
qed

```

As the reader can notice, so far we have proven the relation between the different formulations of security defined in transitive version of the GWV and Rushby models. now we proceed with the intransitive case.

5.7 Rushby Intransitive Non-Interference vs GWV

In this section we compare the Rushby intransitive non Interference described in Section 3.2 versus GWV security model.

As we proved in Section 5.5 GWV security definition implies weak step consistency, which is a key concept for Rushby's intransitive non Interference.

$$s \stackrel{u}{\sim} t \wedge s \stackrel{dom(a)}{\sim} t \supset step(a, s) \stackrel{u}{\sim} step(a, t)$$

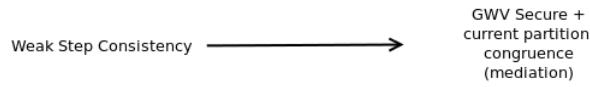


FIGURE 5.5: Relation Between GWV Mediation and Weakly Step Consistency definitions.

As consequence we can use the GWV security definition to show that a GWV secure system that complies with the other Rushby reference monitor conditions is secure for Rushby non interference:

theorem *GWVIsiSecure*:

We use the definitions for the GWV reference monitors

```

assumes  GWVrma1:GWVrma1
and      GWV-secure:GWV-secure
and      GWVrma3:GWVrma3
and      GWVcond2:GWVcond2
and      ActionStep: $\forall s\ t\ u . \text{GWVvpeq}\ s\ u\ t \longrightarrow \text{Action}(\text{Next}\ s) = \text{Action}(\text{Next}\ t)$ 

```

And we use the mappings

```

and      selectMapping:selectMapping
and      stepMapping:stepMapping
and      outputMapping:outputMapping
and      alterMapping:alterMapping
and      currentMapping:currentMapping
and      GWVvpeqtoRelation:GWVvpeqtoRelation
and      intMapping

```

shows isecure

Rushby Weak Step Consistency cannot really ensure GWV separation but a weaker property known as Mediation. The reason for this will be discussed in the next Chapter. Figure 5.5 shows the relation between Rushby step consistency and GWV mediation definitions. We add a definition for mediation (including equality of actions) to prove this.

definition *GWV-secureEPartition*:: bool **where**

```

GWV-secureEPartition  $\equiv \forall st1\ st2\ seg .$ 
  current st1 = current st2  $\wedge$ 
  select st1 seg = select st2 seg  $\wedge$ 
  Action st1 = Action st2  $\wedge$ 
  equals ((segs (current st1))) st1 st2
   $\longrightarrow$  (select (Next st1) seg = select (Next st2) seg)

```


Finally we can prove that Rushby weak step consistency implies our new definition of mediation.

theorem weaklyStepConsistencyImpliesGWVSecure:

assumes 1: weaklyStepConsistent

and 2: stepMapping

and 3: selectMapping

and 4:currentMapping

and 5: observeMapping

and 6: GWVvpeqtoRelation

and hyp: $\forall n. \exists p. n \in \text{segs } p \wedge (\forall n'. n' \in \text{segs } p \longrightarrow n' = n)$

shows GWV-secureEPartition

proof -

show ?thesis

unfolding GWV-secureEPartition-def

proof auto{

fix st1 st2::('State, 'Action) memorystate

fix seg::'Object

we use the hypothesis of the *GWV-secure* definition.

assume GWVhyp1:current st1 = current st2

assume GWVhyp2:select st1 seg = select st2 seg

assume GWVhyp3:Action st1 = Action st2

assume GWVhyp4: $\forall a \in \text{segs } (\text{current st2}). \text{select st1 } a = \text{select st2 } a$

show select (Next st1) seg = select (Next st2) seg

proof-{

Using the *GWVstepConsistent* lemma and our premises we prove that having two equivalent states and a segment that belongs to a partition and we apply the same action to the states, then the values will remain equal after executing a step on the state machine.

have GWVstepconst: $\forall u.$

GWVvpeq st1 u st2

\wedge GWVvpeq st1 (current st1) st2

\wedge seg \in segs u

\wedge Action st1 = Action st2

\longrightarrow (select (Next st1) seg = select (Next st2) seg)

using GWVWeaklyStepConsistent **and** assms

```
unfolding GWVvpeq-def
by auto

from GWVhyp4 and GWVhyp3 and GWVhyp1
have h2:GWVvpeq st1 (current st1) st2
unfolding GWVvpeq-def by simp

then show ?thesis using hyp GWVhyp2 GWVstepconst GWVhyp3
unfolding GWVvpeq-def by blast
}
qed
}qed
qed
```

So far we have proven the relation between the GWV and Rushby models. In the next Chapter we discuss about the differences between the two models and explain the need of the extra conditions we need to add into the original formulations.

Chapter 6

Discussion

There are several fundamental differences between the GWV and Rushby models. These differences complicate the task of comparing them.

Figure 6.1 recapitulates the relation between the security formulations in the GWV and Rushby models. In Chapter 5, we proved that GWV separation definition and one extra condition we named (GWVcond1) implies Rushby's non-interference step consistency definition. Whereas, step consistency implies GWV-secure (we assume that the action executed in the active partition are the same).

If we consider intransitive policies we show that GWV separation definition implies weakly step consistency, while Rushby's definition can only ensure the concept of mediation proposed in the original model GWV.

This kind of fundamental differences results in the existence of some cases where a policy is valid in a model but not for the other.

In this chapter we explore some of these instances, and discuss about the conditions that must be fulfilled by each model to avoid such cases.

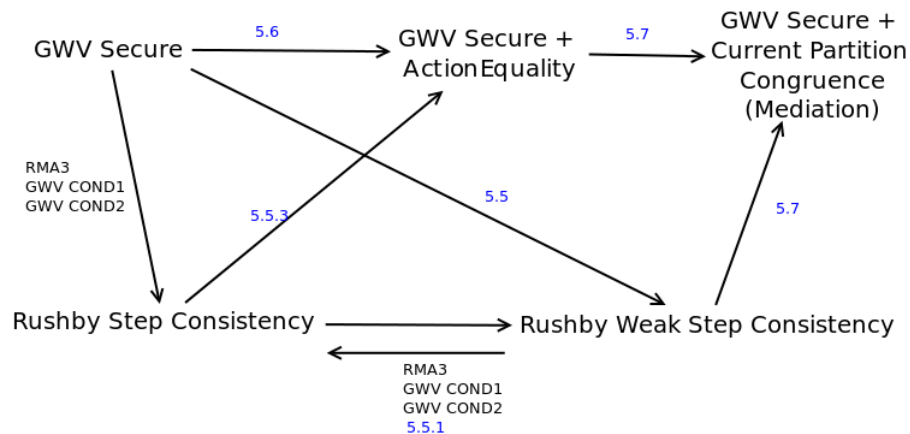


FIGURE 6.1: Relation Among the GWV and Rushby Security definitions

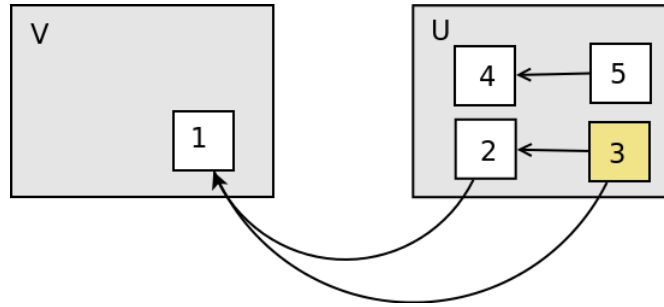


FIGURE 6.2: GWV Secure Policy

6.1 Example 1

For our first example we study one of the conditions added to the GWV model in Section 5.3:

definition $\text{GWVcond1}::\text{bool}$ where

$$\text{GWVcond1} \equiv \forall u v. \text{GWVvia } u v \longrightarrow \text{observe } v \subseteq \text{observe } u$$

Consider a system M as depicted in Figure 6.2. System M consists of two partitions U and V . These partitions have several memory segments assigned to them.

The sole purpose of partition V is to read information from the system. Partition V does not write any data. Partition V contains a memory segment "1", which is used to obtain information from partition U .

On the other hand, partition U has four assigned memory segments $\{2, 3, 4, 5\}$. Segment 1 can only be modified with information from segments 2 and 3. Meanwhile, segment 4 can only be modified with information from segment 5.

System M can be modelled using the following GWV security policy:

$$\begin{aligned} \text{segs}(V) &= \{1\} \\ \text{segs}(U) &= \{2, 3, 4, 5\} \\ \text{dia}(1) &= \{2, 3\} \\ \text{dia}(2) &= \{3\} \\ \text{dia}(4) &= \{5\} \end{aligned}$$

In this particular case, we assume system M is secure for the GWV separation definition. That is, M meets all the conditions of the Separation theorem we discussed in Section 4.3:

- (1) $\text{current } s = \text{current } t \wedge$
- (2) $\text{select } s \text{ seg} = \text{select } t \text{ seg} \wedge$
- (3) $\text{equals } ((\text{dia seg}) \cap (\text{segs } (\text{current } s))) \text{ } s \text{ } t$
 $\longrightarrow (\text{select } (\text{Next } s) \text{ seg} = \text{select } (\text{Next } t) \text{ seg})$

GWV separation theorem definition states that for any two states "s" and "t", and a given partition "seg" where the following conditions are met:

- (1)The Active partition is the same in both states.
- (2)The value of the segment "seg" is equal in the both states.
- (3)The values of the segments that can modify "seg" and are assigned to the active partition equal.

The value of "seg" will not be modified after performing a step on the state machine.

It is important to emphasize that according to GWV separation definition; a partition can read (observe) from all its assigned memory segments($segs(V)$) [8]. Furthermore, GWV security definition prohibits the information flow between segments that do not have a *dia* relation.

In this example, partition U can read from segments $\{2,3,4,5\}$, but the system can only change segment 1 with the information from segments 2 and 3. In other words, according to the GWV model, system M forbids the information flow from segments 4 and 5 to segments 1,2,3.

On the other hand, system M we just described would be defined in the Rushby model by the following sequence of statements:

$$\begin{aligned} Alter(U) &= \{1\} \\ Observe(U) &= \{2,3,4,5\} \\ Observe(V) &= \{1\} \\ Alter(V) &= \emptyset \end{aligned}$$

In this case, an interference relation between U and V ($U \rightsquigarrow V$) is implied by system M . Segment 1 can be modified by U and observed by V . However, if we observe carefully the Rushby **transitive** access control theorem 3.1.8:

Theorem: A system with structured state that satisfies the Reference Monitor Assumptions and the following two conditions.

- 1 $u \rightsquigarrow v \supset observe(u) \subseteq observe(v)$, and
- 2 $n \in alter(u) \wedge n \in observe(v) \supset u \rightsquigarrow v$.

Is secure for the policy \rightsquigarrow .

In particular the first theorem condition ($u \rightsquigarrow v \supset observe(u) \subseteq observe(v)$), states that when two partitions U and V have an interference relation, partition V must be able to read from all the segments that U can read.

As we can see, system M clearly violates the aforementioned condition. Partition U can read from the segments $\{2, 3, 4, 5\}$, and partition V can only read from segment 1.

In other words, in a system like this, not everything that can be observed by U can also be observed by the partition V . Thus violating the Rushby condition.

Intra-partition flow restrictions (like the one required for the partition U) are in practice complex and difficult to ensure. One reason for this, is that all memory segments assigned to the same partition are loaded in the same kernel working area, and can be read for all the processes running in the partition. Jim Alvez [8] discusses a possible attack on the GWV model consisting on modifying the value of a segment, and returning it to its previous value before the evaluation of the security policy (cut point).

A GWV system is expected to prevent the flow from segments $\{4, 5\}$ to segments $\{2, 3\}$. For commercial processors, this capability is too powerful. Custom made hardware is needed to provide the ability to restrict information flow from a specific memory segment to a particular destination segment.

For example, during a partition's execution an untrusted process could copy information from either segments $\{4, 5\}$ into the segments $\{2, 3\}$ and restore the previous value before the policy evaluation (cut-point). The only way to stop the copy from $\{4, 5\}$ is to label the information based on its original source and prevent the data flow during execution time.

May seem like this discrepancy could be caused by our choice to use a strict definition for the *observe* mapping. We considered to use a weaker definition: $\forall u. observe(u) = (\{s'. (\exists s. s \in segsu \wedge s' \in dia(s))\} \cup segs(u))$. To include not only memory segments assigned to a partition but also all segments having a *dia* relation with them. However, even with this expanded definition the difference between the models remains.

6.2 Example 2

In the next example we are going to explore the Rushby security condition, and describe one instance where a Rushby security definition allows valid memory change that violates GWV's separation notion.

Consider a system N like the one depicted in Figure 6.3. System N represents an implementation of an intransitive security policy composed by three classification domains: High, Downgrader and Low, enclosed in the partitions H , D and L respectively.

Partition H can read data from memory segment 1 and send information to partition D using the memory segments $\{2, 3\}$.

In this system, we assume that the Downgrader partition (D) has two specific goals. The first goal is to declassify the information obtained from the High H domain, and

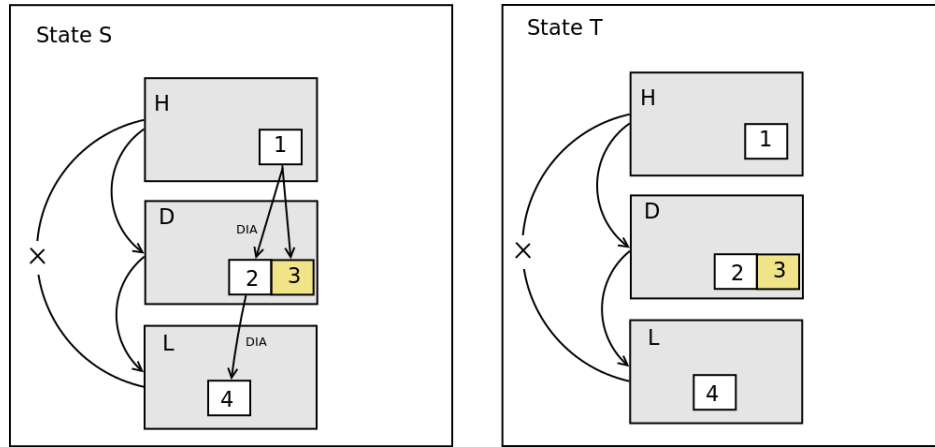


FIGURE 6.3: Policy expressed with GWV and Rushby Models

send the declassified information to partition L . The second goal is to store a copy of the original data for auditing purposes. Partition D stores the original data in segment 3, while, the declassified data are stored in segment 2, and sent to partition L using segment 4.

This kind of intransitive security policies can be written under Rushby terms as follows:

$$H \rightsquigarrow D$$

$$D \rightsquigarrow L$$

$$H \not\rightsquigarrow L$$

A possible implementation of this system can be made with the following object distribution:

$$\text{Observe}(H) = \{1\}$$

$$\text{Alter}(H) = \{2, 3\}$$

$$\text{Observe}(D) = \{2, 3\}$$

$$\text{Alter}(D) = \{4\}$$

$$\text{Observe}(L) = \{4\}$$

$$\text{Alter}(L) = \emptyset$$

Imagine that system N has two states s and t as illustrated in Figure 6.3. Segment 3 has a different value in states s and t ($\text{contents}(s, n) \neq \text{contents}(t, n)$).

Next suppose we execute an action a such that $\text{dom}(a) = \{D\}$ in both states. After executing action a , we evaluate the security policy for partition L in the resulting states s' and t' , where $s' = \text{step}(a, s)$ and $t' = \text{step}(a, t)$.

If we take a look at the definition of weakly step consistency for Rushby intransitive policies:

$$s \stackrel{l}{\sim} t \wedge s \stackrel{dom(a)}{\sim} t \longrightarrow step(a, s) \stackrel{l}{\sim} step(a, t)$$

As we can notice, expression $s \stackrel{dom(a)}{\sim} t$ is not true. The value of segment 3 is not equal in both states. In consequence, Rushby model does not guarantee that the value of Segment 4 remains identical in states s' and t' after executing a .

However, this situation does not violate the condition of weak step consistency. Moreover, the value of Segment 3 may change without implying that the system is insecure. On the other hand, if we consider the same policy implemented in GWV as follows:

$$\begin{aligned} segs(H) &= \{1\} \\ segs(D) &= \{2, 3\} \\ segs(L) &= \{4\} \\ dia(2) &= \{1\} \\ dia(3) &= \{1\} \\ dia(4) &= \{2\} \end{aligned}$$

Taking a closer look on the GWV separation theorem we discussed in section 4.3:

- (1) current s = current $t \wedge$
- (2) select s seg = select t seg \wedge
- (3) equals $((dia \text{ seg}) \cap (segs(\text{current } s))) s t$
 \longrightarrow (select (Next (s)) seg = select (Next (t)) seg)

If we evaluate the separation definition for the segment 4 ($seg = 4$) and the states s and t (with different values for segment 3), we can notice that all the GWV conditions are met:

- We apply the same action a to the states S and t . Hence, both states have the same current partition (D).
- The value of segment 4 is equal in the states s and t , thus the second condition is satisfied.
- The intersection of the $dia(4) \cap segments(D) = 2$ have the same value on the $s t$ states.

However, if the value of segment 4 is different after the execution of action a (as in the Rushby model). It would violate the GWV separation definition as we would have $(select(Next(s))seg \neq select(Next(t)))$.

From this example, we can conclude that the only way for an intransitive Rushby system to comply with the GWV security definition, is if all segments read by the active partition have the same value (not only the intersection with the dia function). This condition matches the *Mediation* definition of the original GWV model.

The Theorem `weaklyStepConsistencyImpliesGWVSecure` we discussed in Section [2.5.2](#) shows that *weakly step consistency* implies Mediation.

Chapter 7

Conclusions and Future Work

Summary and Conclusions

In this document we emphasized the importance of Multiple levels of Security models as an appropriate way to ensure Information Security in computer systems. We explored MILS architecture and concluded that it is a suitable way to implement MLS models. A key concept in the MILS architecture is the separation kernel. Separation kernels are in charge of providing and ensuring isolation between the different security domains in MILS compliant systems.

A Separation Kernel Protection Profile containing the security requirements for high robustness separation kernels was published by the NIST and the NSA. Among the requirements of the SPPK we can find the need to verify the correctness of the separation kernel by means of formal methods.

There are several formal models that can be used to verify security kernels. The best known models are GWV separation and Rushby non-Interference models. However, in the SKPP there is not any guideline on how to select the appropriate model.

This brought up the following question: “what are the exact differences and similarities between the GWV separation model and the non-interference model proposed by Rushby.”

This work contains to our knowledge, the first publicly available formal comparison among GWV and Rushby separation kernel models. The main results of this work is the creation of a mapping relating the concepts of the GWV and Rushby separation kernel models as well as the accompanying proofs relating the security definition in both models.

As we discussed in Chapter 5 we provided a mapping of the methods and properties between we found and proven the relation of the security definition in both models.

In conclusion, we can state that both models have a great number of similarities; both of them define security domains, and control the data flow between the such domains

according to a predefined security policy. However, they present a range of fundamental differences between them:

- GWV and Rushby models are composed of several components that despite being similar to one another are not completely equivalent.
- Rushby controls the flow of information between different security domains, while the GWV controls the flow between different memory segments. This results in a significant difference in the granularity of both models.

Although, none of the aforementioned differences imply an evident security issue, we could find cases where a system is considered secure for the GWV model but not under Rushby's model and vice versa.

Formally determine the differences between different separation kernel models could bring several practical advantages. For example:

- Find the similarities and differences between the two models can provide a starting point to identify the strengths and weaknesses of each model;
- clarify the strengths and weaknesses of each model can serve as a guide to ease the choice of the most suitable formal model in accordance to the specific needs of the separation kernel to be evaluated, and
- Serve as base to estimate if it is feasible to design a system that complies with both security definitions.

Future Work

In this document we have compared the original formulations for the Rushby and GWV separation kernel models. However, both models have suffered several revisions and refinements to extend and clarify its functionality. The coming of these new revisions and models open a promising and interesting field for further research to determine the exact relation between them.

On the one hand, Greve proposed a later revision of the GWV model called GWVr1 [32]. GWVr1 defines the notion of agents with the purpose of adding accountability properties into the original model. Another generalization called GWVr2[33] was subsequently defined to cover security policies for dynamic and distributed systems.

On the other hand, David Oheim proposed a generalization of the original Rushby non-interference model to cover non-deterministic state machines. While Eggert and Van der Meyden [34] argued that the classic notion of intransitive non-interference (*ipurge*)

allows some cases where a low security domain can infer information from higher security domains without the intermediation of the trusted downgraders and proposed a new definition of security named *TA – security*.

Appendix A

Isabelle/HOL

Isabelle [35, 36] is a generic system for interactive theorem proving. It was implemented in the functional programming language ML, and developed by Larry Paulson and Tobias Nipkow. It is available in `isabelle`(<http://isabelle.in.tum.de>).

Isabelle is based on tactics, characteristic inherited from the LCF system (Logic for Computable Functions)[37], which allows building tactics in order to simplify the mechanical application rules for the inference deduction process. Isabelle supports formal reasoning in First Order Logic (FOL) and Higher-Order logic (HOL).

In particular Isabelle/HOL [38] is the specialization of Isabelle for Higher-Order Logic. Isabelle/HOL is an interactive prover assistant, based on Gordon's HOL system[39], which implements an extension of Church's [40] Higher-Order logic. HOL has a large library of theories including set theory, real and complex numbers, abstract algebra, etc. Isabelle/HOL has been successfully used for formal reasoning in various areas of knowledge: Pure Mathematics, verification of computing systems, programming languages, etc.

An [Archive of Formal proofs](#) is available with a variety of theories and examples corresponding to scientific developments that have been formally verified in Isabelle and especially Isabelle/HOL.

Basic Elements of Isabelle/HOL

In this section we illustrate some important aspects of Isabelle/HOL described by Nipkow and Paulson [38]. Please note this document does not intend to completely describe the capacities and features offered by Isabelle/HOL and its multiple extensions, but to provide a quick overview of its main language components.

Theories

Isabelle/HOL formalizations are defined in theories. Theories are modules that contain definitions, terms, formulas, data types, functions, and theorems, etc., that describe the solution of a problem.

When we use Isabelle/HOL, we define theories as extensions of other theories and thus we “import” the data types and structures defined in the imported theories. Isabelle/HOL contains a *Main* theory that includes predefined basic theories, such as the arithmetic of natural numbers, lists and sets. The general syntax to define a theory is:

```

Theory
      import T1. . . Tn
begin
      Type declarations, function definitions and proofs
end

```

Where $T_1 \dots T_n$ are the names of existing theories for which the new theory is defined.

In the *declarations, definitions, and proofs* section we introduce new concepts used to solve a problem such as: types, functions, theorems, lemmas, and their respective proofs.

Sometimes it is useful to introduce, through declarations, new concepts to expand the theories already established. Functional programming needs datatypes and functions. Both of them can be defined in Isabelle/HOL.

Type Declarations

The general datatype syntax in Isabelle has the form

$$\mathbf{datatype} (\alpha_1 \dots \alpha_n) = C_1..C_n$$

Where α represents the name of the datatype and C_1 represents the constructors of the type.

Function Definition

In Isabelle/HOL We declare a definition by defining a name, a type, and a set of defining equations. Functions can be defined with the following keywords[41]:

definition: A function without recursion.

fun: For cases of recursion where termination can be automatically proved. For Isabelle automatically prove the completion of a function, it is necessary that the recursive calls

of the arguments of the function on the right side of each equation are strictly smaller than the arguments corresponding to the left.

primrec: For primitive recursion. In HOL all functions defined by *func* are fully recursive. When it is not possible to define a fully recursive function primitive recursion (**primrec**) must be used.

Isar Structured Testing

Isabelle/HOL can be used to prove lemmas and theorems, in this section we introduce the features of the ISAR (Intelligible semi-automated reasoning) proof environment. ISAR offers a framework for human readable structured proofs. This Section is based on [42], ISAR proofs examples can be found in <http://isabelle.in.tum.de/Isar/>.

The proof environment in ISAR makes use of the following syntax:

```

|lemma|theorem| [<name>:]

[assumes "formula"]

show "formula"
proof [method] statement qed | by method

method = (simp...)|(blast...)|(rule...)|...

statement =      fix variables |
                  assume prop(==>)|
                  [from fact+] (have|show) prop proof|
                  next (separates subgoals)

prop = [name:] "formula"

fact = name|name[OF fact+]|'formula'

```

Isabelle proofs starts with the *lemma* or *theorem* keywords, always followed by a goal to prove (*shows* formula). Please note that we only need to provide a name(label) to the lemma/theorem is we want to reference it in the future.

In ISAR syntax “*assumes*” keyword is used to specify the hypotheses of the statement we want to prove.

An ISAR a proof environment consists of a single method preceded by the *by* word or by a *proof* – *qed* block composed by zero or more statements. A block may optionally start

with the declaration of a method in order to indicate how start the test, for example, (*inductn*)

A statement consists of one of two kinds of propositions, a hypothesis together with your demonstration.

The optional word *from* indicates which facts or hypotheses are used in the demonstration. The intermediate propositions begin with the word *have* and the main proposition with *show*.

A statement can introduce new local variables with the keyword *fix*.

The propositions are formulas preceded optionally a name (label) that subsequently allows the formula to refer to corresponding an assertion preceded with the word *from*.

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